

A Simple Method for Determining Whether Absorption and Elimination Rate Constants Are Equal in the One-Compartment Open Model with First-Order Processes

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A simple method is presented by which one may determine if the absorption and the elimination rate constants are equal (in the one-compartment body model) using only plasma drug data. This method suggests the pertinent equation to calculate the relevant pharmacokinetic parameters.

KEY WORDS: first-order process; equal absorption and elimination rate constants; one-compartment body model.

In a one-compartment open body model with first-order processes, the determination of the absorption and elimination rate constants (k_a and k_e , respectively) using only plasma drug concentration data is dependent on the magnitude of the differences between k_a and k_e .

In the case where $k_a \gg k_e$, k_e can be determined from the slope of the terminal phase of the $\log C_b$ vs. t plot (C_b is concentration of the drug in the body and t is time) and k_a can be determined by the method of residuals (the "feathering" technique). Similarly, when $k_e \gg k_a$ (the so-called flip-flop case) k_a can be determined from the slope of the terminal phase of a $\log C_b$ vs. t plot and k_e can be determined by the method of residuals (1,2).

However, in the case where k_a is equal or close to k_e , absorption continues throughout the elimination phase, and the terminal slope of the $\log C_b$ vs. t plot is not linear and therefore cannot be used to determine a rate constant. Obviously the method of residuals cannot be used.

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In the special case where the absorption rate constant (k_a) is equal to the elimination rate constant (k_e), the general Bateman equation (equation 1) for a one-compartment body model with first-order absorption and elimination is indeterminable (mathematically cannot be determined) and therefore cannot be used to determine the relevant pharmacokinetic parameters (1,2).

$$C_b = \frac{FDk_a}{V(k_a - k_e)}(e^{-k_e t} - e^{-k_a t}) \quad (1)$$

where C_b is the concentration of drug in the body, D is the dose administered, F is the fraction of dose absorbed, and V is the apparent volume of distribution.

When $k_a = k_e = k$, the drug concentration in the body is characterized by equation 2 (1,2):

$$C_b = FDkt e^{-kt} / V \quad (2)$$

This communication presents a simple method for determining, from a single linear plot of C_b vs. t data following drug administration by any first-order processes e.g., oral, intramuscular, or sustained release administration, whether absorption and elimination rate constants are equal (assuming a one-compartment open body model).

From equation 2, relationships can be derived for the parameters t_{\max} (time of peak drug concentration) and $C_{b\max}$ (peak drug concentration) (1,2).

$$t_{\max} = 1/k \quad (3)$$

$$C_{b\max} = FD/Ve \quad e = \text{base of natural logarithms} \quad (4)$$

The product of $t_{\max} \cdot C_{b\max}$ is equal to AUC/e as is shown in equation 5:

$$t_{\max} \cdot C_{b\max} = FD/kVe = FD/CLe = AUC/e \quad (5)$$

where CL is total body clearance and AUC is the area under the curve of C_b vs. t .

From a plot of C_b vs. t , t_{\max} and $C_{b\max}$ can be determined by inspection and AUC can be calculated by the trapezoidal rule.

Thus, whenever $t_{\max} \cdot C_{b\max}$ can be shown to be equal to AUC/e , the rate constants k_a and k_e must be equal and the Bateman equation (equation 1) cannot be used; in this case, k can be calculated using equation 6, which is derived from equation 3:

$$k = k_a = k_e = 1/t_{\max} \quad (6)$$

This method is demonstrated in Fig. 1, where a hypothetical curve was

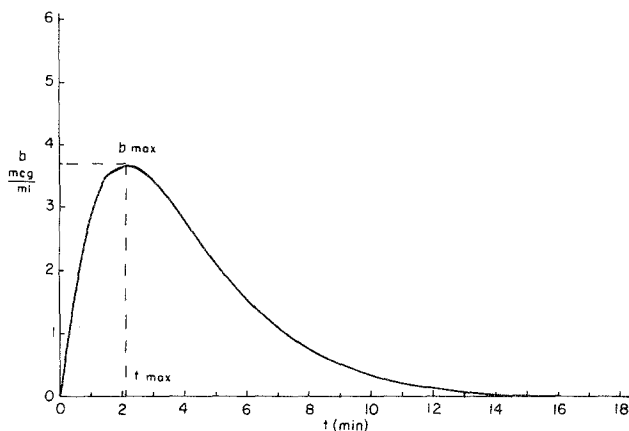


Fig. 1. Hypothetical curve generated by an analog computer.

generated by an analog computer (PACE model TR-9, Electronics Associated, Inc., Long Branch, New Jersey) with initial conditions set at $k_a = k_e = 0.5 \text{ min}^{-1}$.

By inspection, $t_{\max} = 2.1 \text{ min}$, $C_{b\max} = 3.7 \mu\text{g/ml}$, and AUC, calculated by the trapezoidal rule, was found to be $20.6 \mu\text{g}\cdot\text{min/ml}$.

The product $C_{b\max} \cdot t_{\max}$ equals $(2.1 \text{ min})(3.7 \mu\text{g/ml}) = 7.77 \mu\text{g}\cdot\text{min/ml}$. The quotient AUC/e equals $20.6 \mu\text{g}\cdot\text{min/ml}/2.718 = 7.58 \mu\text{g}\cdot\text{min/ml}$. The fact that these two values, as predicted by equation 5, are equal, demonstrates that k_a must be equal to k_e .

In summary, a simple scheme is suggested to determine the equivalence of k_a to k_e using only plasma drug data, which in turn determines which equation (equation 1 or equation 2) must be used to calculate the relevant pharmacokinetic parameters.

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