# Rotational Analysis of the Bal $C^{2} \Pi-X^{2} \Sigma^{+}(8,8)$ Band 

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#### Abstract

The BaI $C^{2} \Pi-X^{2} \Sigma^{+}(8,8)$ band has been measured and rotationally assigned using techniques of population-labeling optical-optical double resonance (PLOODR) and selectively detected laserinduced fluorescence (SDLIF). A weighted nonlinear least-squares fit has been carried out to model the positions of 891 transitions with $J^{\prime \prime}$ ranging from 13.5 to 271.5 , to a ${ }^{2} \Pi \Pi^{2} \Sigma^{+}$Hamiltonian which has 10 spectroscopic constants. Despite the fact that most of our data is from 6 out of the possible 12 rotational branches and is biased in favor of the $C^{2} \Pi_{1 / 2}-X^{2} \Sigma^{+}$subband, we are able to assign $J^{\prime \prime}$ quantum numbers unambiguously for all the observed transitions as well as derive the principal spectroscopic constants of the BaI $C^{2} \Pi$ and $X^{2} \Sigma^{+}$states for the ( 8,8 ) band. © 1991 Acadcmic Pross, Inc.


## 1. INTRODUCTION

The $C^{2} \Pi-X^{2} \Sigma^{+}$band system of the diatomic molecule BaI is centered at approximately 550 nm and is divided into two well-separated subbands by a large spin-orbit interaction ( $780 \mathrm{~cm}^{-1}$ ) in the $C^{2} \Pi$ state. Although there have been a number of spectroscopic studies of this molecule (1-12), including a rotational analysis of the $(0,0)$ vibrational band (1), a complete rovibrational analysis of this system is still to be carried out. In this paper we describe the rotational analysis of the $(8,8)$ band. This particular vibrational transition was chosen because the $X^{2} \Sigma^{+} v^{\prime \prime}=8$ level has significant population both from a thermal oven source and from the $\mathrm{Ba}+\mathrm{HI}$ reaction (13). The incentive to carry out this analysis was to provide a rotational assignment for the study of the dynamics of the reaction $\mathrm{Ba}+\mathrm{HI} \rightarrow \mathrm{BaI}\left(v^{\prime \prime}=8\right)+\mathrm{H}(13)$.

The BaI molecule was first identified in 1927 in an absorption spectrum recorded by Walters and Barratt (2). They observed bands from the $C^{2} I I-X^{2} \Sigma^{+}$transition and also noticed some absorption in the region of 380 nm . Later, Mesnage studied the bandheads ${ }^{4}$ of the two $C^{2} \Pi-X^{2} \Sigma^{+}$subbands, the $C^{2} \Pi_{3 / 2}-X^{2} \Sigma^{+}$at 538.3 nm and the $C^{2} \Pi_{1 / 2}-X^{2} \Sigma^{+}$at $561.2 \mathrm{~nm}(3)$. Patel and Shah analyzed the bandheads in the $C^{2} \Pi_{-}$ $X^{2} \Sigma^{+}$transition (4), and also recognized that the absorption in the region of 380 nm observed by Walters and Barratt (2) was caused by two other electronic band systems, the $E^{2} \Sigma^{+}-X^{2} \Sigma^{+}$transition at about 374 nm and the $D^{2} \Sigma^{+}-X^{2} \Sigma^{+}$transition at about

[^0]388 nm (4). Bradford et al. studied chemiluminescence of BaI formed by the reaction of Ba with $\mathrm{I}_{2}$ (5). They observed emission in the infrared which they determined to be caused by two previously unobserved electronic transitions, the $A^{2} \Pi-X^{2} \Sigma^{+}$and the $B^{2} \Sigma^{+}-X^{2} \Sigma^{+}(5)$. Recently Fernando et al. observed the $A^{\prime 2} \Delta$ state, which is the lowest known excited state, by using a high-resolution infrared Fourier transform spectrometer to resolve the laser-induced fluorescence from the $C^{2} \Pi$ state to the $A^{\prime 2} \Delta$ state (6).

Improved vibrational constants for the $C^{2} \Pi$ and $X^{2} \Sigma^{+}$states were obtained by Rao et al. (7) and a comprehensive study of the bandheads in the $C^{2} \Pi-X^{2} \Sigma^{+}, D^{2} \Sigma^{+}-$ $X^{2} \Sigma^{+}$, and $E^{2} \Sigma^{+}-X^{2} \Sigma^{+}$systems has been carried out by Patel (8). These studics of the vibrational structure of the $C^{2} \Pi-X^{2} \Sigma^{+}$transition show that in both subbands the vibrational bandheads are separated by about $6 \mathrm{~cm}^{-1}$ and that for low values of $v^{\prime \prime}$ the spectrum is dominated by the $\Delta v=0$ sequence, which has Franck-Condon factors close to unity. Analysis of transitions involving higher vibrational levels has been carried out by Johnson et al. using BaI molecules produced by various gas-phase reactions (9). High vibrational levels in the $C^{2} \Pi$ state were shown to predissociate ( $v^{\prime}>62$ for $C^{2} \Pi_{3 / 2}$ and $v^{\prime}>78$ for $C^{2} \Pi_{1 / 2}$ ).

The $C^{2} \Pi-X^{2} \Sigma^{+}$spectrum has very closely spaced rotational lines ( $<0.1 \mathrm{~cm}^{-1}$ separation) and overlapping vibrational bands which make a comprehensive measurement of a rotationally resolved spectrum very difficult. This is a consequence of two factors: first the reduced mass of the molecule means BaI has a small rotational constant ( $B^{\prime \prime}$ $\approx 0.026 \mathrm{~cm}^{-1}$ ) causing many levels to be populated under thermal conditions, and second the nature of the $C^{2} \Pi-X^{2} \Sigma^{+}$transition. The electron that is excited in this transition moves between two nonbonding orbitals, both of which are situated mainly on the Ba atom (15). This results in almost identical potential energy curves for the $C^{2} \Pi$ and $X^{2} \Sigma^{+}$electronic states, both in equilibrium bond length and in shape. The absence of $\Delta v= \pm 1$ transitions for low $v^{\prime \prime}\left(v^{\prime \prime}<10\right)$ provides evidence that the shape close to the bottom of the two potential wells is nearly identical. A consequence of this is that the vibrational constants of the two electronic states are also very similar and vibrational bands are only separated by about $6 \mathrm{~cm}^{-1}$. In addition each vibrational subband is divided into six rotational branches. Thus there is considerable overlap both between the different vibrational bands and between different rotational branches within one vibrational band. The rotational analysis of the $C^{2} \Pi-X^{2} \Sigma^{+}$transition therefore requires the use of narrow-band lasers and special techniques to obtain subDoppler resolution.

To illustrate this problem, we estimate the number of lines in the region of the $(8,8)$ band origin to be about $250 \mathrm{per} \mathrm{cm}^{-1}$ for a thermal population of BaI at the temperature of the oven source ( 1300 K ). This number does not take account of the hyperfine structure arising from the ${ }^{127} \mathrm{I}$ nucleus ( $I=5 / 2$ ) which would cause each rotational line to split into six hyperfine components. (The major isotope of Ba has no nuclear spin.) The hyperfine structure of the $\mathrm{BaI} X^{2} \Sigma^{+}$and $C^{2} \Pi$ states has been studied in detail by Ernst et al. (10) and its influence on the analysis of the $(8,8)$ band is discussed below.

The $C^{2} \Pi$ state of BaI is an example of a Hund's case (a) coupling (16) since the spin-orbit constant, $A^{\prime}$, is greater than the rotational constant, $B^{\prime}$, by a factor of 3 $\times 10^{4}$. With the $\Lambda$ doubling of the ${ }^{2} \Pi$ state and spin-rotation splitting of the ${ }^{2} \Sigma^{+}$
ground state, each vibrational band in the electronic spectrum consists of two wellseparated subbands that have six rotational branches (16). The assignment of the branches would be very difficult by traditional combination relation techniques (16). To overcome this problem Johnson and Zare (11) used the technique of populationlabeling optical-optical double resonance (PLOODR) to assign the $C^{2} \Pi-X^{2} \Sigma^{+}(0,0)$ band. The same approach was used for the $(8,8)$ band.

To measure the spectrum of one rotational branch without interference from others that overlap in the same wavelength region, the technique of selectively detected laserinduced fluorescence (SDLIF) was used. This method was first introduced in 1978 by Linton (17) to study the $A^{2} \Pi-X^{2} \Sigma^{+}$system of yttrium oxide, YO. It was subsequently used by Dulick et al. (18). Once an assignment has been obtained using PLOODR, SDLIF can be used to measure the frequencies of up to several hundred lines in a branch. This approach was also employed in measuring the $\mathrm{BaI} C^{2} I I-X^{2} \Sigma^{+}$ $(0,0)$ band (1).

## 2. EXPERIMENTAL DETAILS

Details of the techniques and apparatus used in this study have been described elsewhere (1,11). A summary of the two methods, population-labeling optical-optical double resonance and selectively detected laser-induced fluorescence, follows.

## (a) Population-Labeling Optical-Optical Double Resonance (PLOODR)

The energy level diagram in Fig. 1 demonstrates the principles involved in PLOODR. The technique uses two dye lasers, both tuned to the rotational structure of the vibronic transition being analyzed. The frequency of one laser, the probe laser, is fixed at the frequency of a single rotational transition. By constantly monitoring the laser-induced fluorescence (LIF) excited by this laser, the population of the ground state rotational level, the "labeled" level, is recorded. The second laser, the pump laser, is scanned across the entire rotational spectrum of the vibronic transition being studied. This laser must be powerful enough to reduce the population of the ground state levels as it excites the transitions. The large separation between the two subbands allows one laser to excite each subband and the resulting LIF from each laser to be collected independently using broad-band spectral filters. When the pump laser induces a transition originating from the labeled level, a decrease in the population of this state is observed. On the other hand, when this laser excites molecules to an upper state that fluoresces to the labeled ground state, the population increases. This is observed as an increase in the fluorescence signal intensity. In a band of the $C^{2} \Pi-X^{2} \Sigma^{+}$system there are a total of nine possible PLOODR signals for each labeled rotational level, of which six are positive and three are negative. This is illustrated in Fig. 1.

An assignment of the rotational numbering can be established and the parity of the ground state and the sign of the spin-rotation constant of the $X^{2} \Sigma^{+}$can be determined by comparing the PLOODR patterns with simulations based on estimated constants and measuring the spacings between the signals (11).

## (b) Selectively Detected Laser-Induced Fluorescence (SDLIF)

In SDLIF a single scanning laser is used to excite molecules and the resulting fluorescence is detected with a narrow-band filter whose transmission is fixed at a different


Fig. 1. Energy level diagram illustrating the principles of PLOODR as applied to the BaI $C^{2} \Pi-X^{2} \Sigma^{+}$ transition. As the pump laser is scanned, nine double resonance signals are expected, three as a decrease in fluorescence (broken lines labeled $P_{1}, Q_{1}, R_{1}$ ) and six as an increase ( solid lines labeled $Q_{12}, R_{1}, P_{12}, R_{12}$, $P_{1}, Q_{12}$ ).
wavelength from the excitation laser. The detector wavelength "window" is chosen so that it collects fluorescence from transitions that have a common upper level with those being excited. Ideally the detector window should be set close to a bandhead so that many rotational lines can be scanned without changing the wavelength of the detector. However this is not essential and measurement of the $Q$-branch members was carried out by gradually altering the detector wavelength (between scans) along the appropriate $P$ or $R$ branch. An illustration of the SDLIF technique as applied to the measurement of the $P_{2}$ branch is given in the upper panel of Fig. 2. The detector window is set to collect the $Q_{21}$ and $R_{2}$-branch members that have a $J^{\prime \prime}$ between about 50.5 and 300.5 ; the laser is scanned along the $P_{2}$-branch transitions.

## (c) Procedure

In all the experiments a molecular beam of BaI was produced by heating Ba and $\mathrm{BaI}_{2}$ in a stainless steel crucible to approximately 1300 K . The beam was subsequently collimated to reduce the Doppler width to about 120 MHz when excited by a laser beam perpendicular to the molecular beam.


FlG. 2. Fortrat diagram (upper panel) of the $\mathrm{BaI} C^{2} \Pi_{3 / 2}-X^{2} \Sigma^{+}(8,8)$ subband illustrating selective detection of the $P_{2}$ branch. The lower panel shows the same Fortrat diagram as the upper panel except that all vibrational bands from $(6,6)$ to $(10,10)$ are included to demonstrate how complicated the picture becomes when other vibrational bands are considered. The dotted lines show where two areas of contamination from other bands are expected as the $P_{2}$-branch spectrum is scanned.

For the PLOODR experiment two single-mode continuous-wave lasers were used, a Coherent 599-21 linear dye laser and a Spectra-Physics 380D ring dye laser. Both were pumped by a Spectra-Physics 171-17 argon ion laser, which gave about 6 W at 514.5 nm . For the region of the spectrum where the BaI $C^{2} \Pi-X^{2} \Sigma^{+}$band system is located, the dye rhodamine 560 was used. A power of about 50 mW was used in each subband for double resonance spectra. The fluorescence from the BaI beam was collected at $f / 3$ and divided into two paths by a $50 \%$ beam splitter. Each fluorescence beam was then detected by a photomultiplier with the appropriate filter to isolate the fluorescence from one spin-orbit subband. The pump laser was chopped so that lockin detection could be used. The double resonance spectrum was obtained using a lockin amplifier to monitor the probe beam fluorescence at the modulation frequency of the pump beam. An iodine spectrum and the fringes of a 250 MHz etalon were recorded simultaneously with each PLOODR spectrum. Absolute frequency calibration was performed by interpolating between the frequencies of iodine reference lines (19) using the etalon fringes.

For the SDLIF experiments only one dye laser was required. Data for the $C^{2} \Pi_{1 / 2^{-}}$ $X^{2} \Sigma^{+}$subband were collected using the Coherent 599-21 laser while data for the $C^{2} \Pi_{3 / 2}-X^{2} \Sigma^{+}$were collected using a Coherent 699-29 ring dye laser because it gave more power in this region of the spectrum. Rhodamine 560 dye was used for both subbands but a few drops of a buffered base were added to the dye solution to shift the dye fluorescence profile to the shorter wavelengths required for $C^{2} \Pi_{3 / 2}-X^{2} \Sigma^{+}$. A $1-\mathrm{m}$ monochromator (Interactive Technology CT103) was used to disperse the fluorescence. The entrance and exit slits could be varied between 0 and 3 mm . Usually $150-\mu \mathrm{m}$ slits were used, which gave a band-pass width of between 3 and $4 \mathrm{~cm}^{-1}$. The dispersed fluorescence was measured by single-photon counting; the signal from the photomultiplier (Centronic Q4283 RA) was amplified (Ortec 9301/474) and converted to an analog signal by a discriminator/ratemeter combination (Ortec 436 and 449). With this arrangement count rates on resonance were on the order of 300 counts $\mathbf{s}^{-1}$. For absolute frequency calibration an $I_{2}$ spectrum and the fringes of a 250 MHz etalon were recorded simultaneously for each SDLIF scan.

## 3. RESULTS AND ANALYSIS

The PLOODR procedure was repeated for a number of different rotational transitions in the $C^{2} \Pi_{1 / 2^{-}} X^{2} \Sigma^{+}$subband and for one transition in $C^{2} \Pi_{3 / 2}-X^{2} \Sigma^{+}$. A total of 25 PLOODR transitions were assigned. Figure 3 shows a PLOODR spectrum from the BaI $C^{2} \Pi_{3 / 2} X^{2} \Sigma^{+}(8,8)$ subband and the $I_{2}$ spectrum with superimposed etalon fringes which was recorded simultaneously. By comparing the observed pattern with

Double Resonance Signal


Fig. 3. An example of a PLOODR spectrum for the BaI $C^{2} \Pi_{3 / 2}-X^{2} \Sigma^{+}(8,8)$ in which the probe laser was tuned to label the ground state $J^{\prime \prime}=50.5$ level while the pump laser was scanned across the rotational structure of the transition. The $I_{2}$ spectrum with superimposed etalon fringes is shown in the lower panel, which was recorded simultaneously for wavenumber calibration.
hypothetical calculated patterns (11) the parity of the ground state rotational level was determined to be $f$ and the sign of the ground state spin-rotational constant, $\gamma^{\prime \prime}$, to be positive. The $J^{\prime \prime}$ assignment was carried out using simplified energy level expressions for the two states (only $B^{\prime}, B^{\prime \prime}$, and $\gamma^{\prime \prime}$ were used). Estimates of the $B$ constants were used to calculate the value of $J^{\prime \prime}$ from various combination relations of the measured lines. For the spectrum illustrated in Fig. 3 the $J^{\prime \prime}$ was found to be 50.5 .

Figure 4 shows an example of a SDLIF spectrum for the $P_{2}$ branch. The monochromator was tuned to the ( $Q_{21}, R_{2}$ ) branches to collect this data [see Fig. 2 (upper panel)]. The parentheses around ( $Q_{21}, R_{2}$ ) are used to denote a pair of very closely spaced branches. The $\mathrm{I}_{2}$ spectrum, which was used for absolute calibration, is also shown. The lower panel of Fig. 2 illustrates how the application of SDLIF to this level is not completely straightforward. When the monochromator is tuned to the (8.8) ( $Q_{21}, R_{2}$ ) branches a portion of the ( 7,7 ) $R_{21}$-branch members can also be detected. This causes the excitation of the (7,7) ( $Q_{2}, P_{21}$ ) transitions ( $J^{\prime \prime} \approx 120.5$ ) to be observed in one part of the $(8,8) P_{2}$ SDLIF spectrum ( $J^{\prime \prime} \approx 120.5$ ). The lower panel of Fig. 2 also shows where contamination of the $P_{2}$ branch will occur from the ( 6,6 ) vibrational band. The beginning of this overlap is visible in the spectrum in Fig. 4; at the low wavenumber end where the baseline rises, there are underlying ( $Q_{2}, P_{21}$ )-branch members of the $(6,6)$ band which are not resolved. Similar problems arise for the other branches; for example, $R_{21}$ is contaminated by the ( $Q_{21}, R_{2}$ ) branches of the $(9,9)$ band in the region of $J^{\prime \prime} \approx 120.5$.


Fig. 4. The upper panel shows a portion of the $P_{2}$ branch from the BaI $C^{2} \Pi_{3 / 2}-X^{2} \Sigma^{+}(8,8)$ subband between $J^{\prime \prime}=202.5$ and 170.5 (left to right) recorded using SDLIF (see Fig. 2). The lower panel shows the $\mathrm{I}_{2}$ spectrum recorded simultaneously for calibration.

From the Fortrat diagram in Fig. 2 (upper panel) it can be seen that the ( $P_{21}, Q_{2}$ ) branches lie almost on top of each other. This is the same for the pairs of branches ( $Q_{21}, R_{2}$ ), ( $P_{1}, Q_{12}$ ), and ( $Q_{1}, R_{12}$ ). Each of these pairs of branches involves the same upper level for a particular $J^{\prime \prime}$; thus they cannot be separated by selective detection.

In the lower $C^{2} \Pi_{1 / 2}-X^{2} \Sigma^{+}$subband, the $P$ - and $R$-branch members are broadened by hyperfine interactions to about 600 MHz compared to 150 MHz for the $Q$-branch transitions (10). This, combined with the dipole moment transition strength of the $Q$-branch members, which is approximately double that of the $P$ - and $R$-branch members, means the peak intensity of the $Q$-branch lines is about five times that of the $P$ and $R$-branch lines for the same value of $J^{\prime \prime}$. This allowed the measurement of the $Q_{12}$ and $Q_{1}$ branches but the weak underlying $P_{1}$ and $R_{12}$ branches could not be observed.

In the $C^{2} \Pi_{3 / 2}-X^{2} \Sigma^{+}$subband the hyperfine splitting for all branches is very similar (about 300 MHz width). The peak intensities of the ( $P_{21}, Q_{2}$ ) and ( $Q_{21}, R_{2}$ ) transitions are within a factor of 2 of each other. Thus, these branches cannot be easily distinguished. None of these four branches was measured.

A total of 881 different rotational lines were recorded by SDLIF in the $P_{12}, Q_{1}$, $Q_{12}, R_{1}, P_{21}$, and $R_{2}$ branches. (The other 10 lines in the data set were only recorded by PLOODR.) Where assignment of the rotational lines could not be carried out by counting directly up the branch from the PLOODR transitions, extrapolation was used. In most cases, even where a branch was contaminated by transitions in neighboring vibrational bands the overall structure of the branch of interest was dominant and the $J^{\prime \prime}$ assignment could still be carried out directly.

The best value of the wavenumber of each recorded rotational line was made by measuring the position of its center of mass. This intensity-weighted mean is chosen to account for hyperfine effects, which result in an asymmetric broadening of the rotational lines (1). In the spectra used for this analysis the effects of hyperfine interactions were only just observable in the $P_{12}$ and $R_{1}$ branches of the lower subband. An analysis of the hyperfine interactions in $\mathrm{BaI} X^{2} \Sigma^{+}$and $C^{2} \Pi$ states has been carried out and measurement of the center of mass was shown to take account of the asymmetric broadening in the rotational transitions measured (1).

Absolute wavenumber calibration for both PLOODR and SDLIF was provided by fitting a polynomial to the peaks of the etalon fringes and then interpolating and extrapolating between the known positions of the iodine lines in each spectrum. In this way the wavenumbers of the transitions measured in the SDLIF spectra are accurate to $\pm 0.002 \mathrm{~cm}^{-1}$ while those measured by PLOODR are accurate to $\pm 0.005 \mathrm{~cm}^{-1}$. The accuracy of the PLOODR wavenumbers is lower than the SDLIF because the pump and probe laser linewidths were narrower than the BaI rotational linewidths, which are broadened by hyperfine interactions. This could result in a small wavenumber offset in the PLOODR spectra, which is taken into account by the greater uncertainty assigned to these measurements.

The experimental transition wavenumbers were given different weights for fitting because not all the lines measured were known to the same accuracy. As discussed above, the PLOODR data were only good to $\pm 0.005 \mathrm{~cm}^{-1}$ while the best parts of the SDLIF spectra were accurate to $\pm 0.002 \mathrm{~cm}^{-1}$. In addition a lower weight was used for the SDLIF where there was blending in the spectrum from another branch, when
the signal to noise was poor and where hyperfine effects made estimation of the line center more difficult. In addition, when the same transition had been measured more than once, the average wavenumber was used taking appropriate account of the weights, and the weight was adjusted accordingly.

A weighted nonlinear least-squares fit of the measured line positions to the usual $C^{2} \Pi-X^{2} \Sigma^{+}$Hamiltonian was carried out (20). First a preliminary fit using nine parameters to the PLOODR wavenumbers and the lower $J^{\prime \prime}$ SDLIF data was done. The nine parameters chosen for the fit were the band origin, $\nu_{0}$, the spin-orbit splitting of the ${ }^{2} \Pi$ state, $A^{\prime}$, the lower and upper rotational constants, $B^{\prime \prime}$ and $B^{\prime}$, and their centrifugal distortion corrections, $D^{\prime \prime}$ and $D^{\prime}$, the spin-rotation constant of the ground state, $\gamma^{\prime \prime}$, and the $\Lambda$-doubling constants of the upper state, $p^{\prime}$ and $q^{\prime}$. Gradually more rotational lines were included as the assignment was extrapolated up the rotational branches. At each stage the "current best fit" parameters were used to check the new assignments. Particular care had to be taken when there was a gap in the experimental data. For example, only transitions with $J^{\prime \prime}$ values greater than 100 were measured for the $C^{2} \mathrm{I}_{3 / 2}-X^{2} \Sigma^{+}$subband so these $R_{2^{-}}$and $P_{21}$-branch members were included in the fit last. The $J^{\prime \prime}$ assignments were checked carefully by examining what happened to the overall fit if one branch was reassigned by one unit in $J^{\prime \prime}$. In all cases tested, the residuals from the fit showed significant trends so incorrect assignments were easily spotted and discarded.

When all 891 lines had been included with a maximum $J^{\prime \prime}$ of 271.5 , an investigation was carried out to determine whether all the nine parameters included were needed and whether further centrifugal distortion constants had to be added to reproduce the data within the experimental accuracy. First, the $\Lambda$-doubling constant, $q^{\prime}$, was found to be very poorly determined and a fit without it showed no significant difference

TABLE I
Spectroscopic Constants in $\mathrm{cm}^{-1}$ for the BaI $C^{2} I I-X^{2} \Sigma^{+}(8,8)$ Band Determined from a Weighted Least-Squares Fit of the Data

| $\mathbf{v}_{0}$ | $1.82362071(5) \times 10^{4} \mathrm{a}$ |
| :--- | :--- |
| $\mathrm{A}^{\prime}$ | $7.571060(8) \times 10^{2}$ |
| $\mathrm{~A}_{\mathrm{D}}{ }^{\prime}$ | $-4.0(3) \times 10^{-7}$ |
| $\mathrm{~B}^{\prime}$ | $2.616285(269) \times 10^{-2}$ |
| $\mathrm{D}^{\prime}$ | $3.0565(178) \times 10^{-9}$ |
| $\mathbf{P}^{\prime}$ | $6.602(7) \times 10^{-3}$ |
| $\mathbf{P}_{D^{\prime}}$ | $-2.7(2) \times 10^{-9}$ |
| $\mathrm{~B}^{\prime \prime}$ | $2.621843(270) \times 10^{-2}$ |
| $\mathrm{D}^{\prime \prime}$ | $3.3130(181) \times 10^{-9}$ |
| $\boldsymbol{\gamma}^{\prime \prime}$ | $2.338(10) \times 10^{-3}$ |

[^1]within the experimental error. This constant was therefore omitted from the final fit. Addition of the centrifugal distortion constants, $A_{\mathrm{D}}^{\prime}$ and $p_{\mathrm{D}}^{\prime}$ was found to improve the fit significantly whereas addition of the parameters $\gamma_{\mathrm{D}}^{\prime \prime}, H^{\prime}$, and $H^{\prime \prime}$ did not.

In total, therefore, 10 adjustable molecular "constants" were included in the leastsquares fit. The final values are given in Table I with two-standard-deviation uncertainties derived from the fit. The normalized residuals from the fit are shown in Fig. 5. The upper panel shows those from the $C^{2} \Pi_{1 / 2}-X^{2} \Sigma^{+}$subband while the lower panel shows those from $C^{2} \Pi_{3 / 2}-X^{2} \Sigma^{+}$. For each transition the normalized residual is the difference between the experimental and calculated wavenumbers (in $\mathrm{cm}^{-1}$ ) divided by the experimental standard deviation (in $\mathrm{cm}^{-1}$ ).

The Appendix lists the experimental wavenumbers of the transitions included in the least-squares fit along with wavenumbers calculated using the parameters in Table I, the experimental standard deviations which are equal to the reciprocal of the weights used and the normalized residuals from the fit.


Fig. 5. Residuals from the least-squares fit of the BaI $C^{2} \Pi_{1 / 2} X^{2} \Sigma^{+}(8,8)$ subband (upper panel; (O) $=Q_{1},(+)=Q_{12},(\times)=R_{1},(\Delta)=P_{12}$, and (\#) $=R_{12}$ and $P_{1}$ ) and the $C^{2} \Pi_{3 / 2} X^{2} \Sigma^{+}$subband (lower panel; $(O)=P_{2},(\triangle)=R_{21},(\times)=P_{21}, R_{2}, Q_{2}$, and $Q_{21}$ ). The normalized residuals are calculated from the difference between the experimental and calculated wavenumbers divided by the experimental standard deviations as given in the Appendix.

## 4. DISCUSSION

The ( 8,8 ) band of the BaI $C^{2} \Pi-X^{2} \Sigma^{+}$transition has been rotationally analyzed by a weighted nonlinear least-squares fitting procedure. The final fit is good; the parameters are all well determined and no trends are observed in the residuals. The variance of the weighted least-squares fit is 0.582 so that the experimental wavenumbers are reproduced within their expected experimental errors. (If the weights used in the fit were, on average, the reciprocal of one experimental standard deviation, the variance would be 1.0 ). The molecular constants determined from the least-squares fit (see Table I) are a minimum set of parameters that reproduce the experimental transition wavenumbers. The number of figures quoted for the rotational constants, $B^{\prime}$ and $B^{\prime \prime}$, and the centrifugal distortion constants, $D^{\prime}$ and $D^{\prime \prime}$, is more than would be expected from their standard deviations because the differences between $B^{\prime}$ and $B^{\prime \prime}$, and $D^{\prime}$ and $D^{\prime \prime}$ is determined more precisely than their absolute values (21). The number of figures quoted is needed to reproduce the calculated wavenumbers given in the Appendix. Since the residuals from the least-squares fit show no systematic trends (see Fig. 5), we conclude that there are no major frequency perturbations affecting these transitions.

The choice of which molecular constants from the standard ${ }^{2} \Pi-{ }^{2} \Sigma^{+}$Hamiltonian are included in the final least-squares fit was made with the intention of obtaining a good fit to the data within the accuracy of the experiment. In particular, we comment on the $\Lambda$-doubling constant, $q^{\prime}$, which has been omitted from the fit.

The $\Lambda$-doubling constant, $q_{v}^{\prime}$, is defined for a general vibrational level, $v$, as

$$
\begin{equation*}
q_{v}^{\prime}=2 \sum_{n^{\prime} v^{\prime}} \frac{\langle n v J| B(r) L_{+}\left|n^{\prime} v^{\prime} J\right\rangle^{2}}{E_{n v J}-E_{n^{\prime} v^{\prime} J}}, \tag{1}
\end{equation*}
$$

where the sum is over all perturbing electronic states, $n^{\prime}$, and their vibrational levels, $v^{\prime}(20)$. Separating the vibrational and electronic matrix elements according to the Born-Oppenheimer approximation gives

$$
\begin{equation*}
\langle n v J| B(r) L_{+}\left|n^{\prime} v^{\prime} J\right\rangle=\langle v J| B(r)\left|v^{\prime} J\right\rangle\langle n| L_{+}\left|n^{\prime}\right\rangle . \tag{2}
\end{equation*}
$$

By neglecting the centrifugal distortion, $q_{v}^{\prime}$ is taken to be independent of $J$. Hence,

$$
\begin{equation*}
\langle v J| B(r)\left|v^{\prime} J\right\rangle=\langle v| B(r)\left|v^{\prime}\right\rangle \tag{3}
\end{equation*}
$$

and

$$
\begin{equation*}
E_{n v J}-E_{n^{\prime} v^{\prime} J}=E_{n v}-E_{n^{\prime} v^{\prime}} . \tag{4}
\end{equation*}
$$

This gives

$$
\begin{equation*}
q_{v}^{\prime}=2 \sum_{n^{\prime}}\langle n| L_{+}\left|n^{\prime}\right\rangle^{2} \sum_{v^{\prime}} \frac{\langle v| B(r)\left|v^{\prime}\right\rangle\left\langle v^{\prime}\right| B(r)|v\rangle}{E_{n v}-E_{n^{\prime} v^{\prime}}} . \tag{5}
\end{equation*}
$$

Further assumptions are necessary to enable us to estimate $q_{v}^{\prime}$. First, we use the unique perturber approximation in which only one electronic $\Sigma$ state is assumed to be perturbing the state. Second, we replace the energy denominator by an effective energy denominator that is independent of $v^{\prime}$. The equation for $q_{v}^{\prime}$ then reduces to

$$
\begin{equation*}
q_{v}^{\prime}=\frac{2\langle v| B^{2}(r)|v\rangle\langle n| L_{+}\left|n^{\prime}\right\rangle^{2}}{E_{n}-E_{n^{\prime}}} \tag{6}
\end{equation*}
$$

The nearest known $\Sigma$ state to the $C^{2} \Pi$ state is the $D^{2} \Sigma^{+}$state which has a band origin at $25774 \mathrm{~cm}^{-1} ; E_{n}-E_{n^{\prime}}$ is therefore close to $7600 \mathrm{~cm}^{-1}(8) .\langle n| L_{+}\left|n^{\prime}\right\rangle$ is taken to be $l(l+1)$ where $l$ is approximated by unity. We also make the approximation

$$
\begin{equation*}
\langle v| r^{-4}|v\rangle=\langle v| r^{-2}|v\rangle^{2} . \tag{7}
\end{equation*}
$$

Then, for $B_{8}^{\prime}$ equal to $0.026 \mathrm{~cm}^{-1}$, we have the estimate $q_{8}^{\prime}$ equals $-3 \times 10^{-7} \mathrm{~cm}^{-1}$. However, the unique perturber approximation is not valid, since there are at least four ${ }^{2} \Sigma^{+}$states ( $X, B, D$, and $E$ ) interacting with the $C^{2} \Pi$ state to cause the $\Lambda$ doubling. This is therefore an order of magnitude estimate. The sign of $q_{8}^{\prime}$ cannot be predicted since the perturbing states lie both above ( $D^{2} \Sigma^{+}$and $E^{2} \Sigma^{+}$) and below ( $B^{2} \Sigma^{+}$and $X^{2} \Sigma^{+}$) the $C^{2} \Pi$ state. A value of $q_{8}^{\prime}$ of approximately $\pm 3 \times 10^{-7} \mathrm{~cm}^{-1}$ has very little effect on the transition wavenumbers. Thus, we conclude that $q_{8}^{\prime}$ is too small to be determined from the present line positions measured. Similarly, rough estimates of the $H^{\prime \prime}, H^{\prime}$, and $\gamma_{D}^{\prime \prime}$ constants suggest that their effects on the transitions measured would be too small to be observed.

The molecular constants given in Table I reproduce the experimental transition wavenumbers very well. However, most of the data is limited to 6 of the 12 possible rotational branches and there is a strong bias in favor of the $C^{2} \Pi_{1 / 2}-X^{2} \Sigma^{+}$subband. Despite these problems we have a definite $J^{\prime \prime}$ assignment for all transitions measured. This has permitted a spectroscopic study of the dynamics of the beam-gas reaction, $\mathrm{Ba}+\mathrm{HI} \rightarrow \mathrm{BaI}\left(v^{\prime \prime}=8\right)+\mathrm{H}(13)$, and will allow additional studies under crossedbeam conditions.

BaI $C-X(8,8)$ ROTATIONAL ANALYSIS

## APPENDIX

TABLE AI
Rotational and Branch Assignment, Experimental Wavenumbers, Calculated Wavenumbers, Standard Deviations, and Normalized Residuals for all Rotational Transitions used in the Least-Squares Fit.

| Branch | J' | Experimental wavenumber ( $\mathrm{cm}-1$ ) | Calculated wavenumber ( $\mathrm{cm}-1$ ) | Experimental standard deviation(cm-1) | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
| P11 | 50.5 | 17855.9790 | 17855.9846 | 0.0050 | -1. 12 |
|  | 54.5 | 17855.8250 | 17855.8392 | 0.0050 | -2.84 |
| R12 | 49.5 | 17859.0750 | 17859.0765 | 0.0050 | -0.30 |
|  | 53.5 | 17859.1860 | 17859.1757 | 0.0050 | 2.07 |
| P12 | 190.5 | 17841.9378 | 17841.9394 | 0.0022 | -0.71 |
|  | 189.5 | 17842.0240 | 17842.0259 | 0.0022 | -0.88 |
|  | 188.5 | 17842.1094 | 17842.1125 | 0.0022 | -1.41 |
|  | 187.5 | 17842.1945 | 17842.1991 | 0.0022 | -2.09 |
|  | 186.5 | 17842.2804 | 17842.2857 | 0.0022 | -2.41 |
|  | 185.5 | 17842.3739 | 17842.3723 | 0.0019 | 0.82 |
|  | 184.5 | 17842.4613 | 17842.4590 | 0.0019 | 1.22 |
|  | 183.5 | 17842.5515 | 17842.5456 | 0.0019 | 3.06 |
|  | 182.5 | 17842.6379 | 17842.6323 | 0.0019 | 2.92 |
|  | 181.5 | 17842.7216 | 17842.7189 | 0.0019 | 1.38 |
|  | 180.5 | 17842.8150 | 17842.8056 | 0.0030 | 3.13 |
|  | 179.5 | 17842.8971 | 17842.8923 | 0.0019 | 2.49 |
|  | 178.5 | 17842.9801 | 17842.9790 | 0.0019 | 0.58 |
|  | 177.5 | 17843.0675 | 17843.0657 | 0.0019 | 0.95 |
|  | 176.5 | 17843.1532 | 17843.1524 | 0.0019 | 0.43 |
|  | 175.5 | 17843.2362 | 17843.2391 | 0.0022 | -1.31 |
|  | 173.5 | 17843.4180 | 17843.4125 | 0.0018 | 3.07 |
|  | 172.5 | 17843.5049 | 17843.4992 | 0.0018 | 3.18 |
|  | 171.5 | 17843.5894 | 17843.5859 | 0.0018 | 1.96 |
|  | 170.5 | 17843.6749 | 17843.6726 | 0.0018 | 1.30 |
|  | 169.5 | 17843.7616 | 17843.7593 | 0.0018 | 1.30 |
|  | 168.5 | 17843.8482 | 17843.8459 | 0.0018 | 1.25 |
|  | 167.5 | 17843.9339 | 17843.9326 | 0.0018 | 0.71 |
|  | 166.5 | 17844.0187 | 17844.0193 | 0.0018 | -0.33 |
|  | 165.5 | 17844.1053 | 17844.1059 | 0.0018 | -0.36 |
|  | 164.5 | 17844.1911 | 17844.1926 | 0.0018 | -0.83 |
|  | 163.5 | 17844.2804 | 17844.2792 | 0.0018 | 0.65 |
|  | 162.5 | 17844.3656 | 17844.3659 | 0.0018 | -0.14 |
|  | 161.5 | 17844.4520 | 17844.4525 | 0.0018 | -0.26 |
|  | 160.5 | 17844.5388 | 17844.5391 | 0.0018 | -0.15 |
|  | 159.5 | 17844.6236 | 17844.6256 | 0.0018 | -1.14 |
|  | 158.5 | 17844.7108 | 17844.7122 | 0.0018 | -0.78 |
|  | 157.5 | 17844.7960 | 17844.7988 | 0.0018 | -1.53 |
|  | 156.5 | 17844.8842 | 17844.8853 | 0.0018 | -0.60 |
|  | 155.5 | 17844.9693 | 17844.9718 | 0.0018 | -1. 38 |
|  | 154.5 | 17845.0571 | 17845.0583 | 0.0018 | -0.65 |
|  | 153.5 | 17845.1420 | 17845.1447 | 0.0018 | -1. 52 |
|  | 152.5 | 17845.2343 | 17845.2312 | 0.0018 | 1.74 |
|  | 151.5 | 17845.3212 | 17845.3176 | 0.0018 | 2.01 |
|  | 150.5 | 17845.4076 | 17845.4040 | 0.0018 | 2.02 |
|  | 149.5 | 17845.4922 | 17845.4903 | 0.0018 | 1.04 |
|  | 148.5 | 17845.5795 | 17845.5767 | 0.0018 | 1.58 |
|  | 147.5 | 17845.6660 | 17845.6630 | 0.0018 | 1.69 |
|  | 146.5 | 17845.7540 | 17845.7492 | 0.0018 | 2.64 |
|  | 145.5 | 17845.8402 | 17845.8355 | 0.0025 | 1.89 |
|  | 144.5 | 17845.9263 | 17845.9217 | 0.0025 | 1.84 |
|  | 143.5 | 17846.0115 | 17846.0079 | 0.0025 | 1.45 |
|  | 142.5 | 17846.0988 | 17846.0940 | 0.0025 | 1.91 |
|  | 141.5 | 17846.1824 | 17846.1801 | 0.0035 | 0.65 |
|  | 140.5 | 17846.2682 | 17846.2662 | 0.0035 | 0.57 |
|  | 139.5 | 17846.3545 | 17846.3522 | 0.0035 | 0.64 |

TABLE AI-Continued

| Branch | J' | Experimental wavenumber ( $\mathrm{cm}-1$ ) | Calculated wavenumber (cm-1) | Experimental <br> standard deviation(cm-1) | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 138.5 | 17846.4393 | 17846.4382 | 20.0035 | 0.30 |
|  | 137.5 | 17846.5259 | 17846.5242 | 20.0035 | 0.48 |
|  | 136.5 | 17846.6112 | 17846.6101 | 10.0035 | 0.31 |
|  | 135.5 | 17846.6969 | 17846.6960 | 0.0035 | 0.25 |
|  | 134.5 | 17846.7832 | 17846.7819 | $9 \quad 0.0035$ | 0.38 |
|  | 133.5 | 17846.8686 | 17846.8677 | $7 \quad 0.0035$ | 0.27 |
|  | 132.5 | 17846.9530 | 17846.9534 | $4 \quad 0.0035$ | -0.12 |
|  | 131.5 | 17847.0399 | 17847.0391 | 0.0035 | 0.22 |
|  | 127.5 | 17847.3787 | 17847.3815 | $5 \quad 0.0040$ | -0.70 |
|  | 126.5 | 17847.4654 | 17847.4670 | 0.0040 | -0.39 |
|  | 125.5 | 17847.5538 | 17847.5524 | - 0.0040 | 0.35 |
|  | 124.5 | 17847.6424 | 17847.6378 | - 0.0040 | 1.16 |
|  | 123.5 | 17847.7286 | 17847.7231 | -0.0040 | 1.38 |
|  | 122.5 | 17847.8115 | 17847.8084 | 40.0040 | 0.78 |
|  | 121.5 | 17847.8961 | 17847.8936 | - 0.0040 | 0.63 |
|  | 120.5 | 17847.9813 | 17847.9787 | 70.0040 | 0.64 |
|  | 119.5 | 17848.0648 | 17848.0639 | - 0.0040 | 0.24 |
|  | 118.5 | 17848.1467 | 17848.1489 | - 0.0040 | -0. 55 |
|  | 117.5 | 17848.2316 | 17848.2339 | - 0.0040 | -0.57 |
|  | 115.5 | 17848.4076 | 17848.4037 | - 0.0040 | 0.97 |
|  | 114.5 | 17848.4950 | 17848.4885 | 50.0040 | 1.62 |
|  | 113.5 | 17848.5740 | 17848.5733 | -0.0040 | 0.18 |
|  | 112.5 | 17848.6566 | 17848.6580 | 0.0040 | -0.35 |
|  | 111.5 | 17848.7394 | 17848.7426 | $6 \quad 0.0040$ | -0.81 |
|  | 110.5 | 17848.8176 | 17848.8272 | 20.0040 | -2.40 |
|  | 109.5 | 17848.9102 | 17848.9117 | $7 \quad 0.0040$ | -0.38 |
|  | 108.5 | 17848.9978 | 17848.9962 | -0.0040 | 0.41 |
|  | 107.5 | 17849.0826 | 17849.0806 | - 0.0040 | 0.51 |
|  | 106.5 | 17849.1629 | 17849.1649 | $9 \quad 0.0040$ | -0.49 |
|  | 105.5 | 17849.2514 | 17849.2491 | 10.0040 | 0.57 |
|  | 103.5 | 17849.4181 | 17849.4174 | $4 \quad 0.0021$ | 0.31 |
|  | 102.5 | 17849.4999 | 17849.5015 | $5 \quad 0.0021$ | -0.75 |
|  | 101.5 | 17849.5810 | 17849.5855 | 50.0028 | -1.58 |
|  | 100.5 | 17849.6685 | 17849.6694 | 40.0021 | -0.41 |
|  | 99.5 | 17849.7536 | 17849.7532 | 20.0021 | 0.18 |
|  | 98.5 | 17849.8360 | 17849.8370 | -0.0021 | -0.46 |
|  | 97.5 | 17849.9218 | 17849.9207 | $7 \quad 0.0021$ | 0.53 |
|  | 96.5 | 17850.0044 | 17850.0043 | 30.0021 | 0.05 |
|  | 95.5 | 17850.0852 | 17850.0878 | 80.0021 | -1.25 |
|  | 94.5 | 17850.1701 | 17850.1713 | $3 \quad 0.0021$ | -0.57 |
|  | 93.5 | 17850.2551 | 17850.2547 | $7 \quad 0.0021$ | 0.18 |
|  | 92.5 | 17850.3372 | 17850.3380 | 0.0015 | -0.54 |
|  | 91.5 | 17850.4233 | 17850.4213 | $3 \quad 0.0018$ | 1.12 |
|  | 90.5 | 17850.5044 | 17850.5045 | $5 \quad 0.0018$ | -0.03 |
|  | 89.5 | 17850.5887 | 17850.5875 | - 0.0018 | 0.64 |
|  | 88.5 | 17850.6716 | 17850.6706 | 6 0.0018 | 0.58 |
|  | 87.5 | 17850.7553 | 17850.7535 | $5 \quad 0.0018$ | 1.00 |
|  | 86.5 | 17850.8376 | 17850.8363 | $3 \quad 0.0018$ | 0.69 |
|  | 85.5 | 17850.9203 | 17850.9191 | 10.0018 | 0.65 |
|  | 84.5 | 17851.0036 | 17851.0018 | $8 \quad 0.0018$ | 0.99 |
|  | 83.5 | 17851.0832 | 17851.0844 | $4 \quad 0.0015$ | -0.84 |
|  | 82.5 | 17851.1660 | 17851.1670 | 0.0015 | -0.66 |
|  | 81.5 | 17851.2488 | 17851.2494 | 40.0015 | -0.42 |
|  | 80.5 | 17851.3270 | 17851.3318 | $8 \quad 0.0025$ | -1.91 |
|  | 79.5 | 17851.4105 | 17851.4140 | 0.0025 | -1.42 |
|  | 78.5 | 17851.4917 | 17851.4962 | 20.0025 | -1.82 |
|  | 77.5 | 17851.5743 | 17851.5784 | 40.0025 | -1.62 |
|  | 76.5 | 17851.6558 | 17851.6604 | 40.0025 | -1.83 |
|  | 75.5 | 17851.7367 | 17851.7423 | $3 \quad 0.0025$ | -2.25 |
|  | 74.5 | 17851.8183 | 17851.8242 | 20.0025 | -2.35 |
|  | 73.5 | 17851.9007 | 17851.9059 | $9 \quad 0.0025$ | -2.09 |
|  | 72.5 | 17851.9867 | 17851.9876 | $6 \quad 0.0013$ | -0.71 |

TABLE AI—Continued

| Branch | J" | Experimental wavenumber (cm-1) | Calculated wavenumber (cm-1) | Experimental standard deviation(cm-1) | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 71.5 | 17852.0693 | 17852.0692 | 0.0013 | 0.09 |
|  | 70.5 | 17852.1505 | 17852.1507 | 0.0013 | -0.13 |
|  | 69.5 | 17852.2320 | 17852.2321 | 0.0013 | -0.06 |
|  | 68.5 | 17852.3138 | 17852.3134 | 0.0013 | 0.30 |
|  | 67.5 | 17852.3950 | 17852.3946 | 0.0013 | 0.28 |
|  | 66.5 | 17852.4756 | 17852.4758 | 0.0013 | -0.12 |
|  | 65.5 | 17852.5567 | 17852.5568 | 0.0013 | -0.08 |
|  | 64.5 | 17852.6378 | 17852.6378 | 0.0013 | 0.04 |
|  | 63.5 | 17852.7190 | 17852.7186 | 0.0013 | 0.29 |
|  | 62.5 | 17852.7984 | 17852.7994 | 0.0013 | -0.72 |
|  | 61.5 | 17852.8793 | 17852.8800 | 0.0013 | -0.55 |
|  | 60.5 | 17852.9599 | 17852.9606 | 0.0018 | -0.40 |
|  | 59.5 | 17853.0423 | 17853.0411 | 0.0018 | 0.67 |
|  | 58.5 | 17853.1223 | 17853.1215 | 0.0018 | 0.46 |
|  | 57.5 | 17853.2036 | 17853.2018 | 0.0018 | 1.02 |
|  | 56.5 | 17853.2826 | 17853.2820 | 0.0018 | 0.36 |
|  | 55.5 | 17853.3624 | 17853.3620 | 0.0017 | 0.21 |
|  | 54.5 | 17853.4421 | 17853.4420 | 0.0018 | 0.03 |
|  | 53.5 | 17853.5216 | 17853.5219 | 0.0017 | -0.20 |
|  | 52.5 | 17853.6005 | 17853.6017 | 0.0018 | -0.69 |
|  | 51.5 | 17853.6790 | 17853.6815 | 0.0017 | -1.45 |
|  | 50.5 | 17853.7604 | 17853.7611 | 0.0018 | -0.36 |
|  | 49.5 | 17853.8376 | 17853.8406 | 0.0017 | -1.75 |
|  | 47.5 | 17854.0007 | 17853.9993 | 0.0018 | 0.80 |
|  | 46.5 | 17854.0798 | 17854.0785 | 0.0018 | 0.74 |
|  | 45.5 | 17854.1579 | 17854.1576 | 0.0018 | 0.18 |
|  | 44.5 | 17854.2368 | 17854.2366 | 0.0018 | 0.13 |
|  | 43.5 | 17854.3175 | 17854.3155 | 0.0018 | 1.13 |
|  | 42.5 | 17854.3953 | 17854.3943 | 0.0018 | 0.57 |
|  | 41.5 | 17854.4748 | 17854.4730 | 0.0018 | 1.02 |
|  | 40.5 | 17854.5528 | 17854.5516 | 0.0018 | 0.69 |
|  | 39.5 | 17854.6313 | 17854.6300 | 0.0018 | 0.70 |
|  | 38.5 | 17854.7114 | 17854.7084 | 0.0040 | 0.74 |
|  | 37.5 | 17854.7885 | 17854.7867 | 0.0030 | 0.60 |
|  | 36.5 | 17854.8674 | 17854.8649 | 0.0030 | 0.84 |
| Q12 | 186.5 | 17850.7503 | 17850.7511 | 0.0020 | -0.42 |
|  | 185.5 | 17850.7925 | 17850.7930 | 0.0020 | -0.26 |
|  | 184.5 | 17850.8346 | 17850.8349 | 0.0025 | -0.13 |
|  | 183.5 | 17850.8761 | 17850.8768 | 0.0020 | -0.35 |
|  | 182.5 | 17850.9182 | 17850.9187 | 0.0020 | -0.25 |
|  | 181.5 | 17850.9599 | 17850.9606 | 0.0020 | -0.34 |
|  | 180.5 | 17851.0019 | 17851.0025 | 0.0020 | -0.29 |
|  | 179.5 | 17851.0439 | 17851.0444 | 0.0020 | -0.23 |
|  | 178.5 | 17851.0867 | 17851.0862 | 0.0020 | 0.23 |
|  | 177.5 | 17851.1278 | 17851.1281 | 0.0020 | -0.16 |
|  | 176.5 | 17851.1696 | 17851.1700 | 0.0020 | -0.20 |
|  | 175.5 | 17851.2116 | 17851.2119 | 0.0020 | -0.13 |
|  | 174.5 | 17851.2541 | 17851.2537 | 0.0025 | 0.16 |
|  | 173.5 | 17851.2948 | 17851.2956 | 0.0020 | -0.38 |
|  | 172.5 | 17851.3380 | 17851.3374 | 0.0020 | 0.31 |
|  | 171.5 | 17851.3788 | 17851.3792 | 0.0020 | -0.20 |
|  | 170.5 | 17851.4231 | 17851.4210 | 0.0025 | 0.83 |
|  | 169.5 | 17851.4620 | 17851.4628 | 0.0020 | -0.40 |
|  | 168.5 | 17851.5048 | 17851.5046 | 0.0025 | 0.09 |
|  | 167.5 | 17851.5452 | 17851.5463 | 0.0020 | -0.57 |
|  | 166.5 | 17851.5877 | 17851.5881 | 0.0025 | -0.16 |
|  | 165.5 | 17851.6290 | 17851.6298 | 0.0020 | -0.41 |
|  | 164.5 | 17851.6711 | 17851.6715 | 0.0025 | -0.17 |
|  | 162.5 | 17851.7524 | 17851.7549 | 0.0020 | -1.23 |
|  | 161.5 | 17851.7935 | 17851.7965 | 0.0020 | -1.50 |

TABLE AI-Continued

| Branch | J" | ```Experimental wavenumber (cm-1)``` | $\begin{gathered} \text { Calculated } \\ \text { wavenumber } \\ (\mathrm{cm}-1) \end{gathered}$ | ```Experimental standard deviation(cm-1)``` | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 160.5 | 17851.8354 | 17851.8381 | 0.0020 | -1.36 |
|  | 159.5 | 17851.8775 | 17851.8797 | 0.0020 | -1.10 |
|  | 158.5 | 17851.9187 | 17851.9213 | 0.0020 | -1.28 |
|  | 157.5 | 17851.9605 | 17851.9628 | 0.0020 | -1.15 |
|  | 156.5 | 17852.0033 | 17852.0043 | 0.0020 | -0.50 |
|  | 155.5 | 17852.0432 | 17852.0458 | 0.0020 | -1.29 |
|  | 154.5 | 17852.0846 | 17852.0872 | 0.0020 | -1.32 |
|  | 153.5 | 17852.1255 | 17852.1286 | 0.0020 | -1.57 |
|  | 152.5 | 17852.1682 | 17852.1700 | 0.0020 | -0.92 |
|  | 151.5 | 17852.2085 | 17852.2114 | 0.0020 | -1.44 |
|  | 150.5 | 17852.2511 | 17852.2527 | 0.0020 | -0.80 |
|  | 149.5 | 17852.2915 | 17852.2940 | 0.0020 | -1.24 |
|  | 148.5 | 17852.3335 | 17852.3352 | 0.0020 | -0.86 |
|  | 147.5 | 17852.3737 | 17852.3764 | 0.0020 | -1.37 |
|  | 146.5 | 17852.4149 | 17852.4176 | 0.0020 | -1.35 |
|  | 145.5 | 17852.4563 | 17852.4587 | 0.0025 | -0.97 |
|  | 144.5 | 17852.4981 | 17852.4998 | 0.0025 | -0.69 |
|  | 143.5 | 17852.5396 | 17852.5409 | 0.0025 | -0.51 |
|  | 142. 5 | 17852.5804 | 17852.5819 | 0.0025 | -0.59 |
|  | 141.5 | 17852.6209 | 17852.6228 | 0.0025 | -0.78 |
|  | 140.5 | 17852.6607 | 17852.6638 | 0.0025 | -1.23 |
|  | 137.5 | 17852.7857 | 17852.7863 | 0.0025 | -0.22 |
|  | 136.5 | 17852.8266 | 17852.8270 | 0.0025 | -0.16 |
|  | 135.5 | 17852.8674 | 17852.8677 | 0.0025 | -0.11 |
|  | 134.5 | 17852.9074 | 17852.9083 | 0.0025 | -0.37 |
|  | 132.5 | 17852.9887 | 17852.9894 | 0.0025 | -0.30 |
|  | 131.5 | 17853.0291 | 17853.0299 | 0.0025 | -0.33 |
|  | 130.5 | 17853.0692 | 17853.0704 | 0.0025 | -0.46 |
|  | 129.5 | 17853.1105 | 17853.1107 | 0.0025 | -0.10 |
|  | 128.5 | 17853.1495 | 17853.1511 | 0.0025 | -0.63 |
|  | 127.5 | 17853.1898 | 17853.1913 | 0.0025 | -0.61 |
|  | 126.5 | 17853.2296 | 17853.2315 | 0.0025 | -0.78 |
|  | 125.5 | 17853.2701 | 17853.2717 | 0.0025 | -0.64 |
|  | 124.5 | 17853.3103 | 17853.3118 | 0.0025 | -0.60 |
|  | 123.5 | 17853.3512 | 17853.3518 | 0.0025 | -0.26 |
|  | 122.5 | 17853.3906 | 17853.3918 | 0.0025 | -0.49 |
|  | 121.5 | 17853.4311 | 17853.4317 | 0.0025 | -0.26 |
|  | 120.5 | 17853.4708 | 17853.4716 | 0.0025 | -0.32 |
|  | 119.5 | 17853.5105 | 17853.5114 | 0.0025 | -0.36 |
|  | 118.5 | 17853.5506 | 17853.5511 | 0.0025 | -0.21 |
|  | 117.5 | 17853.5900 | 17853.5908 | 0.0025 | -0.32 |
|  | 116.5 | 17853.6306 | 17853.6304 | 0.0025 | 0.08 |
|  | 112.5 | 17853.7876 | 17853.7882 | 0.0020 | -0.29 |
|  | 111.5 | 17853.8264 | 17853.8275 | 0.0020 | -0.53 |
|  | 110.5 | 17853.8659 | 17853.8667 | 0.0020 | -0.38 |
|  | 109.5 | 17853.9050 | 17853.9058 | 0.0020 | -0.40 |
|  | 108.5 | 17853.9437 | 17853.9449 | 0.0020 | -0.58 |
|  | 107.5 | 17853.9829 | 17853.9839 | 0.0020 | -0.48 |
|  | 106.5 | 17854.0221 | 17854.0228 | 0.0020 | -0.34 |
|  | 105.5 | 17854.0604 | 17854.0616 | 0.0020 | -0.62 |
|  | 104.5 | 17854.0998 | 17854.1004 | 0.0020 | -0.31 |
|  | 103.5 | 17854.1387 | 17854.1391 | 0.0016 | -0.27 |
|  | 102.5 | 17854.1769 | 17854.1777 | 0.0016 | -0. 54 |
|  | 101.5 | 17854.2165 | 17854.2163 | 0.0016 | 0.13 |
|  | 100.5 | 17854.2539 | 17854.2548 | 0.0016 | -0.56 |
|  | 99.5 | 17854.2927 | 17854.2932 | 0.0014 | -0.34 |
|  | 98.5 | 17854.3303 | 17854.3315 | 0.0014 | -0.85 |
|  | 97.5 | 17854.3691 | 17854.3698 | 0.0014 | -0.46 |
|  | 96.5 | 17854.4066 | 17854.4079 | 0.0014 | -0.93 |
|  | 95.5 | 17854.4458 | 17854.4460 | 0.0014 | -0.15 |

TABLE AI-Continued

| Branch | $J^{\prime \prime}$ | ```Experimental wavenumber (cm-1)``` | ```Calculated wavenumber (cm-1)``` | ```Experimental standard deviation(cm-1)``` | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 94.5 | 17854.4837 | 17854.4840 | 0.0014 | -0.23 |
|  | 93.5 | 17854.5223 | 17854.5219 | 0.0014 | 0.25 |
|  | 92.5 | 17854.5598 | 17854.5598 | 0.0014 | 0.00 |
|  | 91.5 | 17854.5975 | 17854.5976 | 0.0014 | -0.04 |
|  | 90.5 | 17854.6361 | 17854.6352 | 0.0014 | 0.60 |
|  | 89.5 | 17854.6721 | 17854.6728 | 0.0014 | -0.53 |
|  | 88.5 | 17854.7098 | 17854.7104 | 0.0014 | -0.40 |
|  | 87.5 | 17854.7479 | 17854.7478 | 0.0020 | 0.05 |
|  | 86.5 | 17854.7846 | 17854.7851 | 0.0020 | -0.27 |
|  | 85.5 | 17854.8217 | 17854.8224 | 0.0020 | $-0.36$ |
|  | 84.5 | 17854.8589 | 17854.8596 | 0.0020 | -0.34 |
|  | 83.5 | 17854.8956 | 17854.8967 | 0.0020 | -0.54 |
|  | 82.5 | 17854.9335 | 17854.9337 | 0.0020 | -0.09 |
|  | 81.5 | 17854.9705 | 17854.9706 | 0.0020 | -0.05 |
|  | 80.5 | 17855.0073 | 17855.0074 | 0.0016 | -0.08 |
|  | 79.5 | 17855.0441 | 17855.0442 | 0.0016 | -0.05 |
|  | 78.5 | 17855.0800 | 17855.0808 | 0.0025 | -0.33 |
|  | 77.5 | 17855.1174 | 17855.1174 | 0.0025 | 0.01 |
|  | 76.5 | 17855.1534 | 17855.1539 | 0.0025 | -0.18 |
|  | 75.5 | 17855.1895 | 17855.1902 | 0.0025 | -0.29 |
|  | 74.5 | 17855.2269 | 17855.2265 | 0.0025 | 0.15 |
|  | 73.5 | 17855.2634 | 17855.2627 | 0.0025 | 0.27 |
|  | 72.5 | 17855.2991 | 17855.2988 | 0.0025 | 0.11 |
|  | 71.5 | 17855.3347 | 17855.3348 | 0.0025 | -0.05 |
|  | 70.5 | 17855.3709 | 17855.3708 | 0.0025 | 0.06 |
|  | 69.5 | 17855.4061 | 17855.4066 | 0.0017 | -0.29 |
|  | 68.5 | 17855.4413 | 17855.4423 | 0.0017 | -0.61 |
|  | 67.5 | 17855.4775 | 17855.4779 | 0.0017 | -0.27 |
|  | 66.5 | 17855.5132 | 17855.5135 | 0.0017 | -0.17 |
|  | 65.5 | 17855.5489 | 17855.5489 | 0.0017 | -0.01 |
|  | 64.5 | 17855.5834 | 17855.5843 | 0.0017 | -0.53 |
|  | 63.5 | 17855.6186 | 17855.6195 | 0.0017 | -0.56 |
|  | 62.5 | 17855.6534 | 17855.6547 | 0.0017 | -0.77 |
|  | 61.5 | 17855.6896 | 17855.6897 | 0.0017 | -0.08 |
|  | 60.5 | 17855.7244 | 17855.7247 | 0.0017 | $-0.18$ |
|  | 59.5 | 17855.7595 | 17855.7595 | 0.0017 | -0.03 |
|  | 58.5 | 17855.7950 | 17855.7943 | 0.0017 | 0.42 |
|  | 57.5 | 17855.8285 | 17855.8290 | 0.0013 | $-0.35$ |
|  | 56.5 | 17855.8637 | 17855.8635 | 0.0013 | 0.12 |
|  | 55.5 | $17855.89 \% 0$ | 17855.8980 | 0.0013 | $-0.77$ |
|  | 54.5 | 17855.9325 | 17855.9324 | 0.0013 | 0.11 |
|  | 53.5 | 17855.9664 | 17855.9666 | 0.0015 | -0.14 |
|  | 52.5 | 17856.0018 | 17856.0008 | 0.0016 | 0.64 |
|  | 51.5 | 17856.0343 | 17856.0348 | 0.0015 | -0.35 |
|  | 50.5 | 17856.0690 | 17856.0688 | 0.0016 | 0.13 |
|  | 49.5 | 17856.1026 | 17856.1026 | 0.0015 | -0.03 |
|  | 48.5 | 17856.1370 | 17856.1364 | 0.0016 | 0.38 |
|  | 47.5 | 17856.1703 | 17856.1700 | 0.0016 | 0.16 |
|  | 46.5 | 17856.2044 | 17856.2036 | 0.0016 | 0.51 |
|  | 45.5 | 17856.2373 | 17856.2370 | 0.0016 | 0.17 |
|  | 44.5 | 17856.2700 | 17856.2704 | 0.0016 | -0.23 |
|  | 43.5 | 17856.3045 | 17856.3036 | 0.0016 | 0.57 |
|  | 42.5 | 17856.3360 | 17856.3367 | 0.0016 | -0.46 |
|  | 41.5 | 17856.3704 | 17856.3697 | 0.0023 | 0.28 |
|  | 40.5 | 17856.4029 | 17856.4027 | 0.0023 | 0.10 |
|  | 39.5 | 17856.4364 | 17856.4355 | 0.0023 | 0.40 |
|  | 38.5 | 17856.4686 | 17856.4682 | 0.0023 | 0.18 |
|  | 37.5 | 17856.5013 | 17856.5008 | 0.0023 | 0.22 |
|  | 36.5 | 17856.5343 | 17856.5333 | 0.0023 | 0.45 |
|  | 35.5 | 17856.5656 | 17856.5657 | 0.0023 | -0.03 |

TABLE AI-Continued

| Branch | J" | Experimental wavenumber (cm-1) | Calculated wavenumber ( cm -1) | Experimental standard deviation(cm-1) | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Q11 | 34.5 | 17856.5978 | 17856.5979 | 0.0023 | -0.06 |
|  | 33.5 | 17856.6300 | 17856.6301 | 0.0023 | -0.05 |
|  | 32.5 | 17856.6621 | 17856.6622 | 0.0023 | -0.03 |
|  | 31.5 | 17856.6956 | 17856.6941 | 0.0023 | 0.64 |
|  | 30.5 | 17856.7266 | 17856.7260 | 0.0023 | 0.27 |
|  | 29.5 | 17856.7582 | 17856.7577 | 0.0023 | 0.21 |
|  | 13.5 | 17858.0427 | 17858.0444 | 0.0035 | -0.49 |
|  | 14.5 | 17858.0757 | 17858.0711 | 0.0035 | 1.31 |
|  | 15.5 | 17858.0990 | 17858.0977 | 0.0035 | 0.36 |
|  | 16.5 | 17858.1241 | 17858.1242 | 0.0035 | -0.03 |
|  | 17.5 | 17858.1596 | 17858.1506 | 0.0035 | 2.58 |
|  | 18.5 | 17858.1771 | 17858.1768 | 0.0035 | 0.07 |
|  | 19.5 | 17858.2030 | 17858.2030 | 0.0018 | 0.00 |
|  | 20.5 | 17858.2313 | 17858.2290 | 0.0018 | 1.28 |
|  | 21.5 | 17858.2553 | 17858.2550 | 0.0018 | 0.19 |
|  | 22.5 | 17858.2820 | 17858.2808 | 0.0013 | 0.97 |
|  | 23.5 | 17858.3076 | 17858.3065 | 0.0013 | 0.89 |
|  | 24.5 | 17858.3328 | 17858.3321 | 0.0013 | 0.58 |
|  | 25.5 | 17858.3592 | 17858.3575 | 0.0013 | 1.31 |
|  | 26.5 | 17858.3839 | 17858.3829 | 0.0013 | 0.79 |
|  | 27.5 | 17858.4090 | 17858.4081 | 0.0013 | 0.67 |
|  | 28.5 | 17858.4336 | 17858.4333 | 0.0013 | 0.25 |
|  | 29.5 | 17858.4593 | 17858.4583 | 0.0018 | 0.55 |
|  | 30.5 | 17858.4840 | 17858.4832 | 0.0018 | 0.43 |
|  | 31.5 | 17858.5091 | 17858.5080 | 0.0018 | 0.59 |
|  | 32.5 | 17858.5323 | 17858.5327 | 0.0013 | -0.34 |
|  | 33.5 | 17858.5581 | 17858.5573 | 0.0013 | 0.62 |
|  | 34.5 | 17858.5815 | 17858.5818 | 0.0013 | -0.22 |
|  | 35.5 | 17858.6064 | 17858.6061 | 0.0013 | 0.20 |
|  | 36.5 | 17858.6306 | 17858.6304 | 0.0013 | 0.16 |
|  | 37.5 | 17858.6553 | 17858.6545 | 0.0013 | 0.60 |
|  | 38.5 | 17858.6784 | 17858.6786 | 0.0013 | -0.13 |
|  | 39.5 | 17858.7026 | 17858.7025 | 0.0013 | 0.09 |
|  | 40.5 | 17858.7261 | 17858.7263 | 0.0013 | -0.16 |
|  | 41.5 | 17858.7504 | 17858.7500 | 0.0013 | 0.31 |
|  | 42.5 | 17858.7723 | 17858.7736 | 0.0018 | -0.72 |
|  | 43.5 | 17858.7963 | 17858.7971 | 0.0018 | -0.43 |
|  | 44.5 | 17858.8193 | 17858.8205 | 0.0013 | -0.90 |
|  | 45.5 | 17858.8428 | 17858.8437 | 0.0013 | -0.72 |
|  | 46.5 | 17858.8659 | 17858.8669 | 0.0013 | -0.76 |
|  | 47.5 | 17858.8892 | 17858.8899 | 0.0013 | -0.57 |
|  | 48.5 | 17858.9117 | 17858.9129 | 0.0013 | -0.91 |
|  | 49.5 | 17858.9341 | 17858.9357 | 0.0013 | -1.25 |
|  | 50.5 | 17858.9560 | 17858.9584 | 0.0012 | -1.96 |
|  | 51.5 | 17858.9806 | 17858.9810 | 0.0013 | -0.34 |
|  | 52.5 | 17859.0023 | 17859.0035 | 0.0013 | -0.98 |
|  | 53.5 | 17859.0258 | 17859.0260 | 0.0013 | -0.12 |
|  | 54.5 | 17859.0477 | 17859.0482 | 0.0012 | -0.45 |
|  | 55.5 | 17859.0698 | 17859.0704 | 0.0013 | -0.50 |
|  | 56.5 | 17859.0914 | 17859.0925 | 0.0013 | -0.89 |
|  | 57.5 | 17859.1140 | 17859.1145 | 0.0013 | -0.40 |
|  | 58.5 | 17859.1356 | 17859.1364 | 0.0013 | -0.62 |
|  | 59.5 | 17859.1573 | 17859.1582 | 0.0013 | -0.67 |
|  | 60.5 | 17859.1794 | 17859.1798 | 0.0013 | -0.33 |
|  | 61.5 | 17859.2015 | 17859.2014 | 0.0013 | 0.09 |
|  | 62.5 | 17859.2229 | 17859.2228 | 0.0013 | 0.05 |
|  | 63.5 | 17859.2444 | 17859.2442 | 0.0013 | 0.16 |
|  | 64.5 | 17859.2661 | 17859.2654 | 0.0013 | 0.52 |
|  | 65.5 | 17859.2860 | 17859.2866 | 0.0013 | -0.46 |
|  | 66.5 | 17859.3077 | 17859.3076 | 0.0013 | 0.05 |

TABLE AI-Continued

| Branch | J' | Experimental wavenumber ( $\mathrm{cm}-1$ ) | Calculated wavenumber ( $\mathrm{cm}-1$ ) | Experimental standard deviation (cm-1) | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 67.5 | 17859.3289 | 17859.3286 | 0.0013 | 0.25 |
|  | 68.5 | 17859.3495 | 17859.3494 | 0.0013 | 0.06 |
|  | 69.5 | 17859.3698 | 17859.3702 | 0.0013 | -0.28 |
|  | 70.5 | 17859.3914 | 17859.3908 | 0.0013 | 0.47 |
|  | 71.5 | 17859.4111 | 17859.4113 | 0.0013 | -0.19 |
|  | 72.5 | 17859.4312 | 17859.4318 | 0.0013 | -0.45 |
|  | 73.5 | 17859.4519 | 17859.4521 | 0.0013 | -0.17 |
|  | 74.5 | 17859.4721 | 17859.4724 | 0.0018 | -0.14 |
|  | 75.5 | 17859.4913 | 17859.4925 | 0.0013 | -0.94 |
|  | 76.5 | 17859.5123 | 17859.5125 | 0.0013 | -0.18 |
|  | 77.5 | 17859.5322 | 17859.5325 | 0.0013 | -0.22 |
|  | 78.5 | 17859.5527 | 17859.5523 | 0.0013 | 0.30 |
|  | 79.5 | 17859.5721 | 17859.5721 | 0.0013 | 0.03 |
|  | 80.5 | 17859.5921 | 17859.5917 | 0.0013 | 0.30 |
|  | 81.5 | 17859.6119 | 17859.6113 | 0.0013 | 0.49 |
|  | 82.5 | 17859.6316 | 17859.6307 | 0.0013 | 0.68 |
|  | 83.5 | 17859.6503 | 17859.6501 | 0.0013 | 0.16 |
|  | 84.5 | 17859.6703 | 17859.6694 | 0.0013 | 0.74 |
|  | 85.5 | 17859.6890 | 17859.6885 | 0.0016 | 0.28 |
|  | 86.5 | 17859.7079 | 17859.7076 | 0.0014 | 0.20 |
|  | 87.5 | 17859.7270 | 17859.7266 | 0.0014 | 0.28 |
|  | 88.5 | 17859.7446 | 17859.7455 | 0.0015 | -0.58 |
|  | 89.5 | 17859.7627 | 17859.7643 | 0.0015 | -1.03 |
|  | 90.5 | 17859.7817 | 17859.7830 | 0.0015 | -0.84 |
|  | 91.5 | 17859.8020 | 17859.8016 | 0.0015 | 0.25 |
|  | 92.5 | 17859.8180 | 17859.8201 | 0.0015 | -1.39 |
|  | 93.5 | 17859.8377 | 17859.8386 | 0.0015 | -0.56 |
|  | 94.5 | 17859.8565 | 17859.8569 | 0.0018 | -0.23 |
|  | 95.5 | 17859.8735 | 17859.8752 | 0.0018 | -0.93 |
|  | 96.5 | 17859.8922 | 17859.8933 | 0.0018 | -0.63 |
|  | 97.5 | 17859.9110 | 17859.9114 | 0.0018 | -0.23 |
|  | 98.5 | 17859.9289 | 17859.9294 | 0.0015 | -0.33 |
|  | 99.5 | 17859.9460 | 17859.9473 | 0.0015 | -0.84 |
|  | 100.5 | 17859.9647 | 17859.9651 | 0.0015 | -0.27 |
|  | 101.5 | 17859.9841 | 17859.9828 | 0.0015 | 0.81 |
|  | 102.5 | 17860.0002 | 17860.0005 | 0.0015 | -0.19 |
|  | 103.5 | 17860.0183 | 17860.0181 | 0.0015 | 0.16 |
|  | 104.5 | 17860.0360 | 17860.0355 | 0.0019 | 0.25 |
|  | 105.5 | 17860.0537 | 17860.0529 | 0.0019 | 0.41 |
|  | 106.5 | 17860.0696 | 17860.0702 | 0.0019 | -0.32 |
|  | 107.5 | 17860.0875 | 17860.0874 | 0.0019 | 0.03 |
|  | 108.5 | 17860.1066 | 17860.1046 | 0.0019 | 1.05 |
|  | 109.5 | 17860.1206 | 17860.1216 | 0.0019 | -0.55 |
|  | 110.5 | 17860.1380 | 17860.1386 | 0.0019 | -0.33 |
|  | 111.5 | 17860.1544 | 17860.1555 | 0.0014 | -0.83 |
|  | 112.5 | 17860.1715 | 17860.1723 | 0.0014 | -0.62 |
|  | 113.5 | 17860.1871 | 17860.1891 | 0.0015 | -1.33 |
|  | 114.5 | 17860.2043 | 17860.2058 | 0.0014 | -1.07 |
|  | 115.5 | 17860.2213 | 17860.2223 | 0.0014 | -0.77 |
|  | 116.5 | 17860.2382 | 17860.2388 | 0.0015 | -0.44 |
|  | 117.5 | 17860.2547 | 17860.2553 | 0.0016 | -0.36 |
|  | 118.5 | 17860.2706 | 17860.2716 | 0.0015 | -0.71 |
|  | 119.5 | 17860.2900 | 17860.2879 | 0.0017 | 1.26 |
|  | 120.5 | 17860.3035 | 17860.3041 | 0.0015 | -0.43 |
|  | 121.5 | 17860.3200 | 17860.3203 | 0.0015 | -0.18 |
|  | 122.5 | 17860.3362 | 17860.3363 | 0.0018 | -0.07 |
|  | 123.5 | 17860.3531 | 17860.3523 | 0.0016 | 0.49 |
|  | 124.5 | 17860.3670 | 17860.3682 | 0.0016 | -0.77 |
|  | 125.5 | 17860.3831 | 17860.3841 | 0.0016 | -0.62 |
|  | 126.5 | 17860.3996 | 17860.3999 | 0.0018 | -0.15 |

TABLE AI-Continued

| Branch | J' | Experimental wavenumber ( $\mathrm{cm}-1$ ) | Calculated wavenumber ( $\mathrm{cm}-1$ ) | Experimental standard deviation (cm-1) | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 127.5 | 17860.4167 | 17860.4156 | 0.0020 | 0.58 |
|  | 128.5 | 17860.4297 | 17860.4312 | 0.0015 | -0.98 |
|  | 129.5 | 17860.4458 | 17860.4468 | 0.0015 | -0.64 |
|  | 130.5 | 17860.4617 | 17860.4623 | 0.0015 | -0.38 |
|  | 131.5 | 17860.4775 | 17860.4777 | 0.0015 | -0.15 |
|  | 132.5 | 17860.4925 | 17860.4931 | 0.0015 | -0.39 |
|  | 133.5 | 17860.5091 | 17860.5084 | 0.0018 | 0.39 |
|  | 134.5 | 17860.5230 | 17860.5237 | 0.0018 | -0.37 |
|  | 135.5 | 17860.5389 | 17860.5388 | 0.0015 | 0.03 |
|  | 136.5 | 17860.5521 | 17860.5540 | 0.0015 | -1.21 |
|  | 137.5 | 17860.5686 | 17860.5690 | 0.0016 | -0.26 |
|  | 138.5 | 17860.5852 | 17860.5840 | 0.0016 | 0.73 |
|  | 139.5 | 17860.5983 | 17860.5990 | 0.0016 | -0.41 |
|  | 140.5 | 17860.6122 | 17860.6138 | 0.0016 | -1.02 |
|  | 141.5 | 17860.6276 | 17860.6287 | 0.0019 | -0.57 |
|  | 142.5 | 17860.6428 | 17860.6434 | 0.0019 | -0.33 |
|  | 143.5 | 17860.6577 | 17860.6581 | 0.0019 | -0.23 |
|  | 144.5 | 17860.6717 | 17860.6728 | 0.0019 | -0.57 |
|  | 145.5 | 17860.6864 | 17860.6874 | 0.0019 | -0.51 |
|  | 146.5 | 17860.7009 | 17860.7019 | 0.0019 | -0.54 |
|  | 147.5 | 17860.7175 | 17860.7164 | 0.0019 | 0.56 |
|  | 148.5 | 17860.7305 | 17860.7309 | 0.0019 | -0.19 |
|  | 149.5 | 17860.7448 | 17860.7452 | 0.0019 | -0.23 |
|  | 150.5 | 17860.7590 | 17860.7596 | 0.0019 | -0.30 |
|  | 151.5 | 17860.7741 | 17860.7739 | 0.0019 | 0.12 |
|  | 152.5 | 17860.7881 | 17860.7881 | 0.0019 | 0.00 |
|  | 153.5 | 17860.8024 | 17860.8023 | 0.0019 | 0.06 |
|  | 154.5 | 17860.8165 | 17860.8164 | 0.0015 | 0.05 |
|  | 155.5 | 17860.8325 | 17860.8305 | 0.0030 | 0.66 |
|  | 156.5 | 17860.8458 | 17860.8446 | 0.0030 | 0.41 |
|  | 157.5 | 17860.8585 | 17860.8586 | 0.0015 | -0.05 |
|  | 158.5 | 17860.8731 | 17860.8725 | 0.0015 | 0.37 |
|  | 159.5 | 17860.8860 | 17860.8865 | 0.0015 | -0.30 |
|  | 160.5 | 17860.9002 | 17860.9003 | 0.0015 | -0.09 |
|  | 161.5 | 17860.9134 | 17860.9142 | 0.0015 | -0. 0.51 |
|  | 162.5 | 17860.9287 | 17860.9280 | 0.0015 | 0.47 |
|  | 163.5 | 17860.9430 | 17860.9417 | 0.0015 | 0.83 |
|  | 164.5 | 17860.9553 | 17860.9555 | 0.0015 | -0.11 |
|  | 165.5 | 17860.9683 | 17860.9691 | 0.0015 | -0. 56 |
|  | 166.5 | 17860.9819 | 17860.9828 | 0.0015 | -0.59 |
|  | 167.5 | 17860.9968 | 17860.9964 | 0.0015 | 0.26 |
|  | 168.5 | 17861.0138 | 17861.0100 | 0.0040 | 0.95 |
|  | 169.5 | 17861.0266 | 17861.0235 | 0.0040 | 0.77 |
|  | 170.5 | 17861.0356 | 17861.0371 | 0.0019 | -0.78 |
|  | 171.5 | 17861.0499 | 17861.0505 | 0.0016 | -0.40 |
|  | 172.5 | 17861.0653 | 17861.0640 | 0.0023 | 0.56 |
|  | 173.5 | 17861.0812 | 17861.0774 | 0.0040 | 0.94 |
|  | 174.5 | 17861.0923 | 17861.0908 | 0.0040 | 0.37 |
|  | 175.5 | 17861.1037 | 17861.1042 | 0.0021 | -0.23 |
|  | 176.5 | 17861.1190 | 17861.1175 | 0.0028 | 0.52 |
|  | 177.5 | 17861.1296 | 17861.1309 | 0.0040 | -0.32 |
|  | 179.5 | 17861.1554 | 17861.1574 | 0.0025 | -0.82 |
|  | 180.5 | 17861.1710 | 17861.1707 | 0.0031 | 0.10 |
|  | 181.5 | 17861.1886 | 17861.1839 | 0.0050 | 0.93 |
|  | 183.5 | 17861.2085 | 17861.2103 | 0.0025 | -0.73 |
|  | 184.5 | 17861.2233 | 17861.2235 | 0.0025 | -0.09 |
|  | 185.5 | 17861.2355 | 17861.2367 | 0.0022 | -0. 53 |
|  | 186.5 | 17861.2492 | 17861.2498 | 0.0022 | -0.28 |
|  | 187.5 | 17861.2599 | 17861.2630 | 0.0025 | -1.22 |
|  | 188.5 | 17861.2786 | 17861.2761 | 0.0025 | 1.01 |

TABLE AI-Continued

| Branch | J" | Experimental wavenumber (cm-1) | Calculated wavenumber ( $\mathrm{cm}-1$ ) | Experimental standard deviation (cm-1) | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 189.5 | 17861.2880 | 17861.2892 | 0.0022 | -0.53 |
|  | 190.5 | 17861.3018 | 17861.3023 | 0.0022 | -0.22 |
|  | 191.5 | 17861.3142 | 17861.3154 | 0.0025 | -0.47 |
|  | 192.5 | 17861.3272 | 17861.3285 | 0.0025 | -0.50 |
|  | 193.5 | 17861.3393 | 17861.3415 | 0.0025 | -0.89 |
|  | 194.5 | 17861.3548 | 17861.3546 | 0.0031 | 0.06 |
|  | 195.5 | 17861.3655 | 17861.3677 | 0.0022 | -0.97 |
|  | 196.5 | 17861.3795 | 17861.3807 | 0.0040 | -0.31 |
|  | 197.5 | 17861.3944 | 17861.3938 | 0.0040 | 0.15 |
|  | 200.5 | 17861.4302 | 17861.4329 | 0.0040 | -0.69 |
|  | 201.5 | 17861.4431 | 17861.4460 | 0.0040 | -0.73 |
|  | 204.5 | 17861.4832 | 17861.4852 | 0.0040 | -0.50 |
|  | 205.5 | 17861.4978 | 17861.4983 | 0.0025 | -0.19 |
|  | 207.5 | 17861.5225 | 17861.5245 | 0.0040 | -0.49 |
|  | 210.5 | 17861.5651 | 17861.5638 | 0.0040 | 0.32 |
|  | 211.5 | 17861.5749 | 17861.5770 | 0.0040 | -0.52 |
|  | 213.5 | 17861.6003 | 17861.6033 | 0.0040 | -0.75 |
|  | 235.5 | 17861.8990 | 17861.9002 | 0.0040 | -0.29 |
|  | 236.5 | 17861.9130 | 17861.9141 | 0.0040 | -0.28 |
|  | 237.5 | 17861.9281 | 17861.9281 | 0.0040 | 0.00 |
|  | 238.5 | 17861.9414 | 17861.9421 | 0.0040 | -0.18 |
|  | 239.5 | 17861.9547 | 17861.9562 | 0.0050 | -0.30 |
|  | 240.5 | 17861.9698 | 17861.9703 | 0.0050 | -0.11 |
|  | 241.5 | 17861.9827 | 17861.9845 | 0.0040 | -0.46 |
|  | 242.5 | 17861.9961 | 17861.9988 | 0.0040 | -0.67 |
|  | 243.5 | 17862.0112 | 17862.0131 | 0.0040 | -0.47 |
|  | 251.5 | 17862.1258 | 17862.1298 | 0.0040 | -0.99 |
|  | 252.5 | 17862.1435 | 17862.1447 | 0.0040 | -0.29 |
|  | 253.5 | 17862.1578 | 17862.1596 | 0.0040 | -0.45 |
|  | 254.5 | 17862.1750 | 17862.1746 | 0.0050 | 0.07 |
|  | 255.5 | 17862.1885 | 17862.1898 | 0.0040 | -0.32 |
|  | 256.5 | 17862.2056 | 17862.2049 | 0.0040 | 0.16 |
|  | 257.5 | 17862.2210 | 17862.2202 | 0.0040 | 0.20 |
|  | 258.5 | 17862.2349 | 17862.2356 | 0.0050 | -0.13 |
|  | 259.5 | 17862.2521 | 17862.2510 | 0.0040 | 0.28 |
|  | 260.5 | 17862.2642 | 17862.2665 | 0.0040 | -0.58 |
|  | 261.5 | 17862.2827 | 17862.2821 | 0.0040 | 0.15 |
|  | 262.5 | 17862.3022 | 17862.2978 | 0.0040 | 1.10 |
|  | 263.5 | 17862.3151 | 17862.3136 | 0.0050 | 0.31 |
|  | 265.5 | 17862.3434 | 17862.3454 | 0.0040 | -0.49 |
|  | 268.5 | 17862.3825 | 17862.3938 | 0.0050 | -2.26 |
|  | 269.5 | 17862.4087 | 17862.4101 | 0.0040 | -0.35 |
|  | 270.5 | 17862.4240 | 17862.4265 | 0.0040 | -0.64 |
|  | 271.5 | 17862.4404 | 17862.4431 | 0.0040 | -0.67 |
| R11 | 47.5 | 17861.1067 | 17861.1064 | 0.0018 | 0.19 |
|  | 48.5 | 17861.1764 | 17861.1749 | 0.0018 | 0.81 |
|  | 49.5 | 17861.2440 | 17861.2434 | 0.0018 | 0.32 |
|  | 50.5 | 17861.3143 | 17861.3118 | 0.0017 | 1.47 |
|  | 51.5 | 17861.3810 | 17861.3801 | 0.0018 | 0.52 |
|  | 52.5 | 17861.4487 | 17861.4482 | 0.0018 | 0.27 |
|  | 53.5 | 17861.5159 | 17861.5163 | 0.0018 | -0.20 |
|  | 54.5 | 17861.5842 | 17861.5842 | 0.0017 | 0.00 |
|  | 55.5 | 17861.6527 | 17861.6520 | 0.0018 | 0.38 |
|  | 56.5 | 17861.7194 | 17861.7197 | 0.0018 | -0.19 |
|  | 57.5 | 17861.7875 | 17861.7873 | 0.0018 | 0.09 |
|  | 58.5 | 17861.8542 | 17861.8548 | 0.0018 | -0.36 |
|  | 59.5 | 17861.9223 | 17861.9222 | 0.0018 | 0.04 |
|  | 60.5 | 17861.9891 | 17861.9895 | 0.0018 | -0.23 |
|  | 61.5 | 17862.0567 | 17862.0567 | 0.0018 | 0.01 |
|  | 62.5 | 17862.1235 | 17862.1238 | 0.0035 | -0.07 |

TABLE AI-Continued

| Branch | $J^{\prime \prime}$ | Experimental wavenumber (cm-1) | Calculated wavenumber ( $\mathrm{cm}-1$ ) | Experimental standard deviation (cm-1) | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 63.5 | 17862.1903 | 17862.1907 | 0.0035 | -0.12 |
|  | 64.5 | 17862.2575 | 17862.2576 | 0.0035 | -0.02 |
|  | 65.5 | 17862.3243 | 17862.3243 | 0.0035 | 0.00 |
|  | 66.5 | 17862.3909 | 17862.3909 | 0.0035 | -0.01 |
|  | 67.5 | 17862.4574 | 17862.4575 | 0.0035 | -0.02 |
|  | 68.5 | 17862.5236 | 17862.5239 | 0.0035 | -0.09 |
|  | 69.5 | 17862.5899 | 17862.5902 | 0.0035 | -0.09 |
|  | 70.5 | 17862.6550 | 17862.6564 | 0.0035 | -0.41 |
|  | 71.5 | 17862.7215 | 17862.7226 | 0.0035 | -0.30 |
|  | 72.5 | 17862.7896 | 17862.7886 | 0.0016 | 0.65 |
|  | 73.5 | 17862.8553 | 17862.8545 | 0.0016 | 0.52 |
|  | 74.5 | 17862.9203 | 17862.9203 | 0.0016 | 0.02 |
|  | 75.5 | 17862.9870 | 17862.9860 | 0.0016 | 0.64 |
|  | 76.5 | 17863.0526 | 17863.0516 | 0.0018 | 0.58 |
|  | 77.5 | 17863.1188 | 17863.1171 | 0.0018 | 0.97 |
|  | 78.5 | 17863.1840 | 17863.1824 | 0.0018 | 0.87 |
|  | 79.5 | 17863.2492 | 17863.2477 | 0.0018 | 0.82 |
|  | 80.5 | 17863.3147 | 17863.3129 | 0.0018 | 0.99 |
|  | 81.5 | 17863.3795 | 17863.3780 | 0.0018 | 0.83 |
|  | 82.5 | 17863.4440 | 17863.4430 | 0.0018 | 0.57 |
|  | 83.5 | 17863.5084 | 17863.5079 | 0.0018 | 0.30 |
|  | 84.5 | 17863.5732 | 17863.5726 | 0.0018 | 0.31 |
|  | 85.5 | 17863.6380 | 17863.6373 | 0.0018 | 0.37 |
|  | 86.5 | 17863.7031 | 17863.7019 | 0.0018 | 0.66 |
|  | 87.5 | 17863.7675 | 17863.7664 | 0.0018 | 0.61 |
|  | 88.5 | 17863.8319 | 17863.8308 | 0.0018 | 0.62 |
|  | 89.5 | 17863.8955 | 17863.8951 | 0.0018 | 0.23 |
|  | 90.5 | 17863.9602 | 17863.9593 | 0.0018 | 0.51 |
|  | 91.5 | 17864.0249 | 17864.0234 | 0.0018 | 0.85 |
|  | 92.5 | 17864.0886 | 17864.0874 | 0.0018 | 0.68 |
|  | 93.5 | 17864.1519 | 17864.1513 | 0.0018 | 0.35 |
|  | 94.5 | 17864.2155 | 17864.2151 | 0.0018 | 0.23 |
|  | 95.5 | 17864.2789 | 17864.2788 | 0.0018 | 0.06 |
|  | 96.5 | 17864.3427 | 17864.3424 | 0.0018 | 0.16 |
|  | 97.5 | 17864.4055 | 17864.4059 | 0.0018 | -0.25 |
|  | 98.5 | 17864.4695 | 17864.4694 | 0.0018 | 0.07 |
|  | 99.5 | 17864.5320 | 17864.5327 | 0.0013 | -0.56 |
|  | 100.5 | 17864.5954 | 17864.5960 | 0.0018 | -0.31 |
|  | 101.5 | 17864.6584 | 17864.6591 | 0.0018 | -0.40 |
|  | 102.5 | 17864.7215 | 17864.7222 | 0.0018 | -0.37 |
|  | 103.5 | 17864.7846 | 17864.7851 | 0.0025 | -0.22 |
|  | 104.5 | 17864.8485 | 17864.8480 | 0.0025 | 0.19 |
|  | 105.5 | 17864.9098 | 17864.9108 | 0.0025 | -0.41 |
|  | 106.5 | 17864.9714 | 17864.9735 | 0.0025 | -0.85 |
|  | 110.5 | 17865.2274 | 17865.2234 | 0.0050 | 0.79 |
|  | 111.5 | 17865.2869 | 17865.2857 | 0.0050 | 0.24 |
|  | 112.5 | 17865.3460 | 17865.3479 | 0.0050 | -0.38 |
|  | 113.5 | 17865.4106 | 17865.4100 | 0.0050 | 0.12 |
|  | 114.5 | 17865.4744 | 17865.4720 | 0.0050 | 0.48 |
|  | 115.5 | 17865.5325 | 17865.5339 | 0.0050 | -0.28 |
|  | 116.5 | 17865.6003 | 17865.5958 | 0.0050 | 0.91 |
|  | 117.5 | 17865.6564 | 17865.6575 | 0.0050 | -0.22 |
|  | 118.5 | 17865.7226 | 17865.7192 | 0.0050 | 0.68 |
|  | 119.5 | 17865.7786 | 17865.7808 | 0.0050 | -0.44 |
|  | 120.5 | 17865.8438 | 17865.8423 | 0.0050 | 0.30 |
|  | 121.5 | 17865.9063 | 17865.9037 | 0.0026 | 1.00 |
|  | 122.5 | 17865.9652 | 17865.9651 | 0.0022 | 0.06 |
|  | 123.5 | 17866.0264 | 17866.0263 | 0.0022 | 0.02 |
|  | 124.5 | 17866.0876 | 17866.0875 | 0.0022 | 0.02 |
|  | 125.5 | 17866.1505 | 17866.1487 | 0.0022 | 0.82 |

TABLE AI-Continued

| Branch | J" | Experimental wavenumber ( $\mathrm{cm}-1$ ) | Calculated wavenumber ( $\mathrm{cm}-1$ ) | Experimental standard deviation (cm-1) | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 126.5 | 17866.2108 | 17866.2097 | 0.0025 | 0.44 |
|  | 127.5 | 17866.2709 | 17866.2707 | 0.0013 | 0.18 |
|  | 128.5 | 17866.3311 | 17866.3316 | 0.0013 | -0.36 |
|  | 129.5 | 17866.3920 | 17866.3924 | 0.0013 | -0.29 |
|  | 130.5 | 17866.4535 | 17866.4531 | 0.0013 | 0.31 |
|  | 131.5 | 17866.5138 | 17866.5138 | 0.0013 | 0.02 |
|  | 132.5 | 17866.5750 | 17866.5744 | 0.0013 | 0.50 |
|  | 133.5 | 17866.6354 | 17866.6349 | 0.0013 | 0.41 |
|  | 134.5 | 17866.6956 | 17866.6953 | 0.0013 | 0.21 |
|  | 135.5 | 17866.7564 | 17866.7557 | 0.0013 | 0.55 |
|  | 136.5 | 17866.8168 | 17866.8160 | 0.0010 | 0.76 |
|  | 137.5 | 17866.8761 | 17866.8763 | 0.0013 | -0.12 |
|  | 138.5 | 17866.9370 | 17866.9364 | 0.0010 | 0.56 |
|  | 139.5 | 17866.9967 | 17866.9965 | 0.0010 | 0.17 |
|  | 140.5 | 17867.0570 | 17867.0566 | 0.0010 | 0.43 |
|  | 141.5 | 17867.1169 | 17867.1165 | 0.0010 | 0.36 |
|  | 142.5 | 17867.1775 | 17867.1764 | 0.0013 | 0.84 |
|  | 143.5 | 17867.2371 | 17867.2363 | 0.0013 | 0.66 |
|  | 144.5 | 17867.2966 | 17867.2960 | 0.0013 | 0.44 |
|  | 145.5 | 17867.3565 | 17867.3557 | 0.0013 | 0.59 |
|  | 146.5 | 17857.4161 | 17867.4154 | 0.0013 | 0.55 |
|  | 147.5 | 17867.4758 | 17867.4750 | 0.0013 | 0.64 |
|  | 148.5 | 17867.5357 | 17867.5345 | 0.0013 | 0.94 |
|  | 149.5 | 17867.5951 | 17867.5940 | 0.0013 | 0.89 |
|  | 150.5 | 17867.6540 | 17867.6534 | 0.0013 | 0.49 |
|  | 151.5 | 17867.7137 | 17867.7127 | 0.0013 | 0.76 |
|  | 152.5 | 17867.7712 | 17867.7720 | 0.0018 | -0.45 |
|  | 153.5 | 17867.8304 | 17867.8313 | 0.0018 | -0.47 |
|  | 157.5 | 17868.0676 | 17868.0676 | 0.0025 | -0.01 |
|  | 158.5 | 17868.1269 | 17868.1266 | 0.0018 | 0.17 |
|  | 159.5 | 17868.1860 | 17868.1855 | 0.0018 | 0.27 |
|  | 160.5 | 17868.2449 | 17868.2444 | 0.0018 | 0.29 |
|  | 161.5 | 17868.3041 | 17868.3032 | 0.0018 | 0.51 |
|  | 162.5 | 17868.3621 | 17868.3619 | 0.0018 | 0.09 |
|  | 163.5 | 17868.1214 | 17868.4207 | 0.0018 | 0.41 |
|  | 164.5 | 17868.4802 | 17868.4793 | 0.0018 | 0.49 |
|  | 165.5 | 17868.5378 | 17868.5379 | 0.0018 | -0.08 |
|  | 166.5 | 17868.5973 | 17868.5965 | 0.0018 | 0.43 |
|  | 167.5 | 17868.6562 | 17868.6551 | 0.0018 | 0.64 |
|  | 168.5 | 17868.7148 | 17868.7135 | 0.0018 | 0.70 |
|  | 169.5 | 17868.7722 | 17868.7720 | 0.0018 | 0.12 |
|  | 170.5 | 17868.8308 | 17868.8304 | 0.0018 | 0.23 |
|  | 171.5 | 17868.8896 | 17868.8888 | 0.0018 | 0.47 |
|  | 172.5 | 17868.9480 | 17868.9471 | 0.0018 | 0.51 |
|  | 173.5 | 17869.0069 | 17869.0054 | 0.0018 | 0.86 |
|  | 174.5 | 17869.0615 | 17869.0636 | 0.0018 | -1.17 |
|  | 175.5 | 17869.1209 | 17869.1218 | 0.0018 | -0.51 |
|  | 176.5 | 17869.1785 | 17869.1800 | 0.0018 | -0.83 |
|  | 177.5 | 17869.2369 | 17869.2381 | 0.0018 | -0.68 |
|  | 178.5 | 17869.2951 | 17869.2962 | 0.0018 | -0.63 |
|  | 179.5 | 17869.3531 | 17869.3543 | 0.0018 | -0.67 |
|  | 180.5 | 17869.4128 | 17869.4124 | 0.0018 | 0.25 |
|  | 181.5 | 17869.4698 | 17869.4704 | 0.0018 | -0.31 |
|  | 182.5 | 17869.5291 | 17869.5283 | 0.0018 | 0.42 |
|  | 183.5 | 17869.5845 | 17869.5863 | 0.0018 | -1.00 |
|  | 184.5 | 17869.6419 | 17869.6442 | 0.0018 | -1.29 |
|  | 185.5 | 17869.7011 | 17869.7021 | 0.0018 | -0.56 |
|  | 186.5 | 17869.7589 | 17869.7600 | 0.0018 | -0.60 |
|  | 187.5 | 17869.8161 | 17869.8178 | 0.0018 | -0.96 |
|  | 188.5 | 17869.8738 | 17869.8757 | 0.0018 | -1.03 |

TABLE AI-Continued

| Branch | J" | Experimental wavenumber (cm-1) | Calculated wavenumber (cm-1) | ```Experimental standard deviation(cm-1)``` | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 189.5 | 17869.9304 | 17869.9335 | 0.0018 | -1.70 |
|  | 190.5 | 17869.9889 | 17869.9912 | 0.0018 | -1.30 |
|  | 191.5 | 17870.0493 | 17870.0490 | 0.0018 | 0.17 |
|  | 192.5 | 17870.1068 | 17870.1067 | 0.0018 | 0.03 |
|  | 193.5 | 17870.1662 | 17870.1645 | 0.0018 | 0.97 |
|  | 194.5 | 17870.2215 | 17870.2222 | 0.0018 | -0.37 |
|  | 195.5 | 17870.2800 | 17870.2799 | 0.0018 | 0.08 |
|  | 196.5 | 17870.3378 | 17870.3375 | 0.0018 | 0.15 |
|  | 197.5 | 17870.3942 | 17870.3952 | 0.0018 | -0.55 |
|  | 198.5 | 17870.4517 | 17870.4528 | 0.0018 | -0.63 |
|  | 199.5 | 17870.5100 | 17870.5105 | 0.0018 | -0.26 |
|  | 200.5 | 17870.5682 | 17870.5681 | 0.0018 | 0.06 |
|  | 201.5 | 17870.6260 | 17870.6257 | 0.0018 | 0.16 |
|  | 202.5 | 17870.6840 | 17870.6833 | 0.0018 | 0.38 |
|  | 203.5 | 17870.7433 | 17870.7409 | 0.0018 | 1.32 |
|  | 204.5 | 17870.8015 | 17870.7985 | 0.0018 | 1.66 |
|  | 205.5 | 17870.8567 | 17870.8561 | 0.0018 | 0.33 |
|  | 206.5 | 17870.9149 | 17870.9137 | 0.0018 | 0.67 |
|  | 207.5 | 17870.9693 | 17870.9713 | 0.0018 | -1.09 |
| R21 | 49.5 | 18618.4750 | 18618.4663 | 0.0050 | 1.74 |
|  | 117.5 | 18623.1220 | 18623.1217 | 0.0026 | 0.12 |
|  | 118.5 | 18623.1870 | 18623.1870 | 0.0026 | 0.00 |
|  | 119.5 | 18623.2525 | 18623.2522 | 0.0026 | 0.11 |
|  | 120.5 | 18623.3183 | 18623.3174 | 0.0026 | 0.36 |
|  | 121.5 | 18623.3824 | 18623.3824 | 0.0026 | -0.01 |
|  | 122.5 | 18623.4464 | 18623.4474 | 0.0026 | -0.40 |
|  | 123.5 | 18623.5111 | 18623.5123 | 0.0026 | -0.48 |
|  | 124.5 | 18623.5771 | 18623.5772 | 0.0026 | -0.03 |
|  | 125.5 | 18623.6408 | 18623.6419 | 0.0026 | -0.44 |
|  | 126.5 | 18623.7056 | 18623.7066 | 0.0026 | -0.40 |
|  | 127.5 | 18623.7688 | 18623.7713 | 0.0026 | -0.94 |
|  | 128.5 | 18623.8343 | 18623.8358 | 0.0026 | -0.57 |
|  | 129.5 | 18623.9011 | 18623.9003 | 0.0021 | 0.40 |
|  | 130.5 | 18623.9656 | 18623.9647 | 0.0017 | 0.55 |
|  | 131.5 | 18624.0301 | 18624.0290 | 0.0017 | 0.65 |
|  | 132.5 | 18624.0943 | 18624.0932 | 0.0017 | 0.62 |
|  | 133.5 | 18624.1603 | 18624.1574 | 0.0023 | 1.24 |
|  | 134.5 | 18624.2231 | 18624.2215 | 0.0023 | 0.68 |
|  | 135.5 | 18624.2867 | 18624.2856 | 0.0023 | 0.49 |
|  | 136.5 | 18624.3507 | 18624.3496 | 0.0023 | 0.50 |
|  | 137.5 | 18624.4149 | 18624.4135 | 0.0023 | 0.62 |
|  | 138.5 | 18624.4792 | 18624.4773 | 0.0023 | 0.82 |
|  | 139.5 | 18624.5428 | 18624.5411 | 0.0023 | 0.74 |
|  | 140.5 | 18624.6050 | 18624.6048 | 0.0023 | 0.09 |
|  | 141.5 | 18624.6686 | 18624.6684 | 0.0023 | 0.07 |
|  | 142.5 | 18624.7313 | 18624.7320 | 0.0014 | -0.51 |
|  | 143.5 | 18624.7951 | 18624.7955 | 0.0014 | -0.31 |
|  | 144.5 | 18624.8590 | 18624.8590 | 0.0014 | 0.00 |
|  | 145.5 | 18624.9224 | 18624.9224 | 0.0018 | 0.00 |
|  | 146.5 | 18624.9853 | 18624.9857 | 0.0018 | -0.24 |
|  | 147.5 | 18625.0463 | 18625.0490 | 0.0018 | -1. 51 |
|  | 148.5 | 18625.1104 | 18625.1122 | 0.0018 | -1.02 |
|  | 149.5 | 18625.1737 | 18625.1754 | 0.0018 | -0.94 |
|  | 150.5 | 18625.2364 | 18625.2385 | 0.0018 | -1.16 |
|  | 151.5 | 18625.3009 | 18625.3015 | 0.0018 | -0.35 |
|  | 152.5 | 18625.3653 | 18625.3645 | 0.0018 | 0.43 |
|  | 153.5 | 18625.4256 | 18625.4275 | 0.0018 | -1.03 |
|  | 154.5 | 18625.4873 | 18625.4903 | 0.0018 | -1.69 |
|  | 155.5 | 18625.5525 | 18625.5532 | 0.0012 | -0.56 |
|  | 156.5 | 18625.6153 | 18625.6159 | 0.0012 | -0.54 |

TABLE AI-Continued


TABLE AI-Continued


TABLE AI-Continued

| Branch | J" | Experimental wavenumber (cm-1) | Calculated wavenumber ( $\mathrm{cm}-1$ ) | ```Experimental standard deviation(cm-1)``` | Normalized residual |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 174.5 | 18599.8586 | 18599.8582 | 0.0032 | 0.13 |
|  | 175.5 | 18599.7684 | 18599.7689 | 0.0032 | -0.15 |
|  | 176.5 | 18599.6789 | 18599.6796 | 0.0032 | -0.21 |
|  | 177.5 | 18599.5904 | 18599.5902 | 0.0035 | 0.04 |
|  | 178.5 | 18599.4991 | 18599.5009 | 0.0035 | -0.53 |
|  | 179.5 | 18599.4097 | 18599.4117 | 0.0035 | -0.56 |
|  | 180.5 | 18599.3199 | 18599.3224 | 0.0035 | -0.71 |
|  | 181.5 | 18599.2328 | 18599.2331 | 0.0035 | -0.09 |
|  | 182.5 | 18599.1429 | 18599.1438 | 0.0035 | -0.27 |
|  | 183.5 | 18599.0535 | 18599.0546 | 0.0035 | -0.32 |
|  | 184.5 | 18598.9627 | 18598.9654 | 0.0035 | -0.76 |
|  | 185.5 | 18598.8750 | 18598.8762 | 0.0035 | -0.33 |
|  | 186.5 | 18598.7853 | 18598.7870 | 0.0035 | -0.48 |
|  | 187.5 | 18598.6961 | 18598.6978 | 0.0035 | -0.48 |
|  | 188.5 | 18598.6078 | 18598.6086 | 0.0035 | -0.24 |
|  | 189.5 | 18598.5188 | 18598.5195 | 0.0035 | -0.20 |
|  | 190.5 | 18598.4292 | 18598.4304 | 0.0035 | -0.34 |
|  | 191.5 | 18598.3399 | 18598.3413 | 0.0035 | -0.40 |
|  | 192.5 | 18598.2517 | 18598.2523 | 0.0035 | -0.16 |
|  | 193.5 | 18598.1635 | 18598.1632 | 0.0035 | 0.08 |
|  | 194.5 | 18598.0740 | 18598.0742 | 0.0035 | -0.06 |
|  | 195.5 | 18597.9833 | 18597.9852 | 0.0035 | -0.56 |
|  | 196.5 | 18597.8957 | 18597.8963 | 0.0035 | -0.17 |
|  | 197.5 | 18597.8069 | 18597.8074 | 0.0035 | -0.14 |
|  | 198.5 | 18597.7177 | 18597.7185 | 0.0024 | -0.34 |
|  | 199.5 | 18597.6282 | 18597.6297 | 0.0024 | -0.61 |
|  | 200.5 | 18597.5393 | 18597.5409 | 0.0024 | -0.65 |
|  | 201.5 | 18597.4514 | 18597.4521 | 0.0024 | -0.28 |
|  | 202.5 | 18597.3637 | 18597.3633 | 0.0024 | 0.15 |
|  | 203.5 | 18597.2737 | 18597.2747 | 0.0027 | -0.36 |
|  | 204.5 | 18597.1838 | 18597.1860 | 0.0027 | -0.83 |
|  | 205.5 | 18597.0939 | 18597.0974 | 0.0045 | -0.78 |
|  | 206.5 | 18597.0088 | 18597.0088 | 0.0045 | -0.01 |
|  | 207.5 | 18596.9208 | 18596.9203 | 0.0045 | 0.11 |
|  | 210.5 | 18596.6502 | 18596.6550 | 0.0045 | -1.08 |
|  | 211.5 | 18596.5635 | 18596.5667 | 0.0045 | -0.71 |
|  | 212.5 | 18596.4773 | 18596.4784 | 0.0045 | -0.25 |
|  | 213.5 | 18596.3889 | 18596.3902 | 0.0045 | -0.30 |
|  | 214.5 | 18596.2993 | 18596.3021 | 0.0045 | -0.61 |
|  | 215.5 | 18596.2103 | 18596.2140 | 0.0045 | -0.81 |
|  | 216.5 | 18596.1231 | 18596.1259 | 0.0045 | -0.63 |
|  | 217.5 | 18596.0375 | 18596.0379 | 0.0045 | -0.10 |
|  | 218.5 | 18595.9539 | 18595.9500 | 0.0045 | 0.87 |
|  | 219.5 | 18595.8673 | 18595.8621 | 0.0045 | 1.15 |
|  | 220.5 | 18595.7749 | 18595.7743 | 0.0045 | 0.12 |
|  | 221.5 | 18595.6853 | 18595.6866 | 0.0045 | -0.29 |
|  | 222.5 | 18595.6007 | 18595.5989 | 0.0045 | 0.39 |
|  | 223.5 | 18595.5168 | 18595.5113 | 0.0045 | 1.21 |
| P21 | 51.5 | 18613.1700 | 18613.1712 | 0.0050 | -0.25 |
| Q21 | 49.5 | 18615.8330 | 18615.8253 | 0.0050 | 1.54 |
|  | 51.5 | 18615.8720 | 18615.8644 | 0.0050 | 1.52 |
| Q22 | 50.5 | 18613.2890 | 18613.2916 | 0.0050 | -0.53 |
| R22 | 48.5 | 18615.9430 | 18615.9411 | 0.0050 | 0.39 |
|  | 50.5 | 18615.9890 | 18615.9848 | 0.0050 | 0.83 |

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    ${ }^{4}$ Work in this laboratory shows that the bandheads in Bal are not formed for $J^{\prime \prime}<420.5$ (14); these earlier studies actually observed closely spaced lines corresponding to points of inflection on a Fortrat diagram. However, we follow the earlier nomenclature and refer to them as bandheads.

[^1]:    a Two standard deviation uncertainties derived
    from the fit are given in parentheses in units
    of the last significant figure.

