



# The nature of the chemical bond in NO<sub>3</sub>, neutral and anion

Apostolos Kalemos<sup>1</sup>

Received: 19 November 2019 / Accepted: 3 February 2020  
© Springer-Verlag GmbH Germany, part of Springer Nature 2020

## Abstract

The nitrate radical, NO<sub>3</sub>, a molecular species of huge environmental importance has been an active research theme for at least a century at both the experimental and theoretical levels. Its ground-state symmetry, C<sub>2v</sub> or D<sub>3h</sub>, has puzzled the scientific community for nearly two decades, while its fascinating spectral profile is complicated due to intense vibronic couplings between its first five electronic states. In the present work, we report an elucidation of its chemical bonding based on a NO-to-NO<sub>2</sub>-to-NO<sub>3</sub> formation sequence. We conclude that there are three different chemical bonds between N and the three O atoms, one double  $\sigma$ ,  $\pi$  with an O (<sup>3</sup>P), one dative  $\sigma$  with an excited O (~<sup>1</sup>D) and finally a regular  $\sigma$  with a ground O (<sup>3</sup>P). Its anion, NO<sub>3</sub><sup>-</sup>, results naturally by grafting an additional electron to the ground neutral state.

**Keywords** Nature of chemical bond · Nitrate radical · Vibronic coupling

## 1 Introduction

The nitrate radical, NO<sub>3</sub>, is one of the first polyatomic radicals to be discovered about 140 years ago in Paris of the *Belle Époque* [1, 2]. It is a major factor in the earth's atmosphere either by regulating ozone's depletion or by being responsible for the creation of a variety of harmful pollutants; see, e.g., Refs. [3–12].

Additionally, it represents one of the most exciting, extraordinary and complicated species in chemical physics that has been posing great challenges to both experimentalists and theoreticians. The major source of these fascinating problems is the intense vibronic coupling of Jahn–Teller (JT) or pseudo-JT character between its low-lying three (D<sub>3h</sub>)/five (C<sub>2v</sub>) electronic states found within an energy range of 2 eV, namely  $\tilde{X}^2A'_2/1^2B_2$ ,  $\tilde{A}^2E''/1^2B_1$ ,  $1^2A_2$  and  $\tilde{B}^2E'/1^2A_1$ ,  $2^2B_2$ . Its intriguing characteristics have been the central theme of a great deal of high-quality work of both theoretical [13–38] and experimental [39–65] nature that continues up to the present [66, 67].

For nearly two decades, the question of whether its ground state is of C<sub>2v</sub> or D<sub>3h</sub> symmetry was a recurring

theme of research; see, e.g., Refs. [13, 15, 18, 19, 21, 26], but finally the equilibrium geometry of this species was concluded to be of D<sub>3h</sub> symmetry [21]. What is undoubtedly true is that the potential surface of its ground state is flat around its D<sub>3h</sub> minimum along the planar asymmetric distortion, and the most interesting question we can really ask is what we can really learn from that fact. Or in other words what does the C<sub>2v</sub>/D<sub>3h</sub> rivalry teach us concerning the way three O atoms bind to N?

Another field of active research gears toward the spectroscopic characterization of its vibrational levels coupled together by various nonadiabatic couplings. This investigation path was initiated by Mayer et al. [20] who as early as 1993 tried to theoretically calculate the photoelectron spectrum of NO<sub>3</sub><sup>-</sup>, obtained a few years earlier by Weaver et al. [44] through a multimode vibronic coupling model (KDC Hamiltonian) [68]. Weaver et al. observed directly and for the first time the first excited dark  $\tilde{A}^2E''$  state, concluded on the D<sub>3h</sub> symmetry of its ground state, and offered an extensive analysis of the vibronic coupling between  $\tilde{X}^2A'_2$  and  $\tilde{B}^2E'$  [44]. Its fascinating spectral profile has since been the subject of numerous theoretical *state-of-the-art* studies, see, e.g., Refs. [24–26, 28, 29, 32–38].

Despite the existence of so many theoretical studies on  $\tilde{X}^2A'_2$ ,  $\tilde{A}^2E''$  and  $\tilde{B}^2E'$ , there is still no answer on its bonding mechanism and this is exactly the sole purpose of the present paper. To this end, we have employed primarily the R(or U) CCSD(T) correlation method tailored for open-shell species

✉ Apostolos Kalemos  
kalemos@chem.uoa.gr

<sup>1</sup> Department of Chemistry, Laboratory of Physical Chemistry, National and Kapodistrian University of Athens, Panepistimiopolis, Athens 157 71, Greece

coupled with the (aug-)cc-pVQZ basis sets [69]. Vibrational frequencies were calculated at the R(or U)CCSD(T)/cc-pVQZ level for the ground states of the NO<sub>3</sub> and NO<sub>3</sub><sup>-</sup> species via numerical second derivatives. Additional information on computational aspects of this work will be given in due places throughout the text. Energy calculations were done with the MOLPRO code [70].

## 2 Results and discussion

With the goal of understanding the nature of the chemical bond in NO<sub>3</sub>, we plan to trace its formation path through the NO-to-NO<sub>2</sub>-to-NO<sub>3</sub> sequence. The ground NO state is of  $X^2\Pi$  symmetry with its first excited  $a^4\Pi$  state lying  $T_e = 38,440 \text{ cm}^{-1}$  (= 110 kcal/mol) higher [71] (see also Table 1 for RCCSD(T)/cc-pVQZ values). Both states dissociate adiabatically to the ground-state fragments N (<sup>4</sup>S) + O (<sup>3</sup>P). Their CASSCF (11 valence electrons/8 valence orbitals) equilibrium wavefunctions and atomic Mulliken (NBO) populations are

$$\begin{aligned} |X^2\Pi\rangle &\cong 0.96 \left| 1\sigma^2 2\sigma^2 3\sigma^2 1\pi_x^2 2\pi_x^1 1\pi_y^2 \right\rangle \quad \text{with } 1\sigma \sim 2s(\text{O}), \quad 2\sigma \sim 2s(\text{N}), \\ 3\sigma &\sim 0.71 \times 2p_z(\text{N}) - 0.74 \times 2p_z(\text{O}), \quad 1\pi_x \sim 0.52 \times 2p_x(\text{N}) + 0.75 \times 2p_x(\text{O}), \\ 2\pi_x &\sim 0.88 \times 2p_x(\text{N}) - 0.70 \times 2p_x(\text{O}), \\ 2s^{1.88} 2p_x^{1.31} 2p_y^{0.74} 2p_z^{0.98} /_{\text{N}} 2s^{1.80} 2p_x^{1.64} 2p_y^{1.22} 2p_z^{1.29} /_{\text{O}} \\ &\left( 2s^{1.68} 2p_x^{1.23} 2p_y^{0.66} 2p_z^{1.09} /_{\text{N}} 2s^{1.74} 2p_x^{1.75} 2p_y^{1.32} 2p_z^{1.43} /_{\text{O}} \right) \end{aligned}$$

and

$$\begin{aligned} |a^4\Pi\rangle &\cong 0.98 \left| 1\sigma^2 2\sigma^2 3\sigma^2 1\pi_x^2 2\pi_x^1 1\pi_y^2 2\pi_y^1 \right\rangle \quad \text{with } 1\sigma \sim 2s(\text{O}), \quad 2\sigma \sim 2s(\text{N}), \\ 3\sigma &\sim 0.60 \times 2p_z(\text{N}) - 0.73 \times 2p_z(\text{O}), \quad 1\pi_x \sim 0.30 \times 2p_x(\text{N}) + 0.91 \times 2p_x(\text{O}), \\ 2\pi_x &\sim 0.97 \times 2p_x(\text{N}) - 0.43 \times 2p_x(\text{O}), \quad 2s^{1.93} 2p_x^{1.13} 2p_y^{1.0} 2p_z^{0.86} /_{\text{N}} 2s^{1.92} 2p_x^{1.85} 2p_y^{1.0} 2p_z^{1.25} /_{\text{O}} \\ &\left( 2s^{1.85} 2p_x^{1.08} 2p_y^{1.0} 2p_z^{0.88} /_{\text{N}} 2s^{1.89} 2p_x^{1.91} 2p_y^{1.0} 2p_z^{1.35} /_{\text{O}} \right). \end{aligned}$$

Based on the above electronic characteristics, we can pictorially represent the  $X^2\Pi$  and  $a^4\Pi$  wavefunctions with the help of the valence bond Lewis (vbL) diagrams shown in Schemes 1 and 2.

The odd electron is hosted by an orbital with greater amplitude on N, and the  $X^2\Pi$ -to- $a^4\Pi$  transformation is accomplished through the rupture of the  $\pi_y$  bond. The addition of an H (<sup>2</sup>S) atom creates HNO ( $\tilde{X}^1A'$ ) but not NOH since the odd electron appears to be more localized on the N atom; see Table 1 for energies and molecular parameters. There is thus a double ( $\sigma$ ,  $\pi$ ) bond between N and O and a single bond between N and H (H–N=O). The latter (N–H)

bond features a binding energy of  $D_e = 52.7 \text{ kcal/mol}$  with respect to NO ( $X^2\Pi$ ) + H (<sup>2</sup>S) at the RCCSD(T)/cc-pVQZ computational level. Most interesting though is the addition of OH ( $X^2\Pi$ ) to form nitrous acid, HO–N=O. It has a planar ( $C_s$ ) structure of  $\tilde{X}^1A'$  symmetry with its RCCSD(T)/cc-pVQZ equilibrium parameters presented in Table 1. There is again a double ( $\sigma$ ,  $\pi$ ) bond between N and the terminal O atom and a single bond between N and the hydroxyl O atom (HO–N=O).

If we now consider H–N=O( $\tilde{X}^1A'$ ) and approach an O atom, we will get an isomer of nitrous acid, the H–NO<sub>2</sub> [ $\tilde{X}^1A_1(C_{2v})$ ] species where the H atom is now attached to N. Adiabatically, H–NO<sub>2</sub>( $\tilde{X}^1A_1$ ) follows the HNO ( $\tilde{a}^3A''$ ) + O (<sup>3</sup>P) fragmentation path rather than HNO ( $\tilde{X}^1A'$ ) + O (<sup>1</sup>D) since  $T_e(\tilde{a}^3A'' \leftarrow \tilde{X}^1A')$ <sub>HNO</sub> = 19.3 kcal/mol (Table 1) and  $\Delta E(^1D \leftarrow ^3P)_O = 45.1 \text{ kcal/mol}$  [72]; see Fig. 1 for the CASSCF (18 valence electrons/13 valence orbitals) interaction curves, but the HNO ( $\tilde{a}^3A''$ ;  $\pi_x^1 \pi_y^1$ ) + O (<sup>3</sup>P;  $2p_x^1 p_z^1$ ) electronic distribution does not lead to any chemical bonding. Hopefully enough, the interaction with the HNO ( $\tilde{X}^1A'$ ) + O

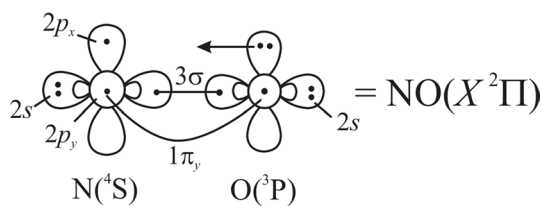
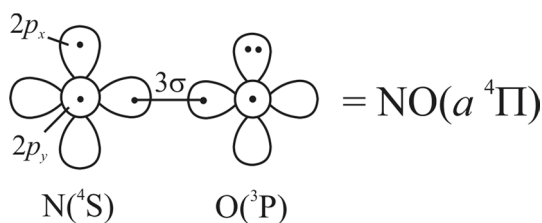
( $2p_x^2 p_y^2$ ;  $\sim ^1D$ ) distribution comes into rescue at around 5.0 bohr by creating a dative bond between the  $\sim 2s^2(\text{N})$  electronic density and the “empty”  $\sim 2p_z(\text{O})$  orbital. Proof of that is the equilibrium Mulliken (NBO) population  $2s^{1.30}$  ( $2s^{1.16}$ ) of nitrogen and the Mulliken charges on each O atom,  $q = -0.26$  ( $-0.32$ ). This population decline of the  $2s(\text{N})$  density reflects exactly the formation of a dative bond and that its minimum correlates adiabatically to HNO ( $\tilde{X}^1A'$ ) + O ( $\sim ^1D$ ). After a careful inspection of the evolution of the CASSCF wavefunction and molecular orbitals along the reaction coordinate, we come up with the following equilibrium  $C_{2v}$  structure represented pictorially by the vbL diagram of Scheme 3.

**Table 1** Energies  $E$  (hartree) and molecular parameters (bond distances in Å and bond angles in degrees) of the different species studied in the present work at the RCCSD(T)/cc-pVQZ computational level

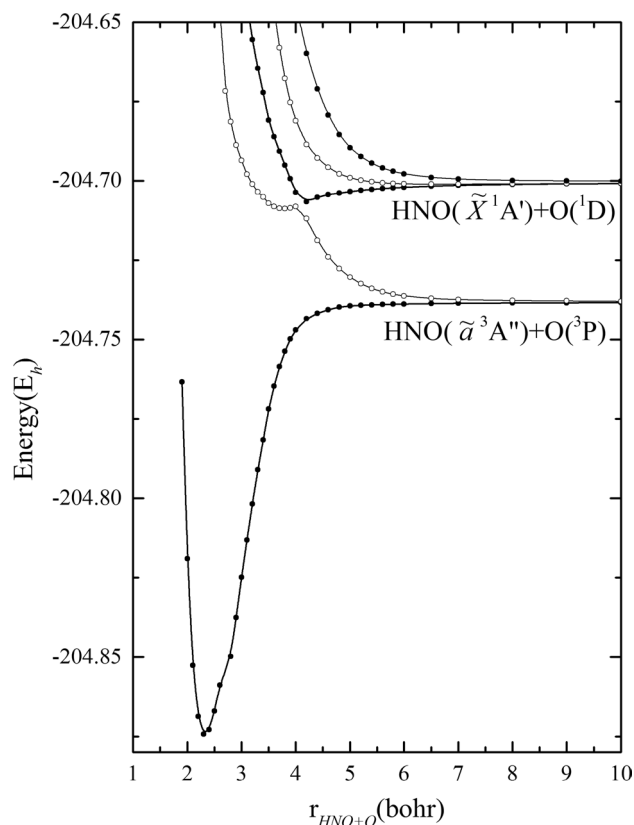
Species	$-E$	Molecular parameters					
NO( $X^2\Pi$ )	129.754 228	1.152 <sub>NO</sub>					
NO( $a^4\Pi$ )	129.579 560	1.421 <sub>NO</sub>					
HNO( $\tilde{X}^1A'$ )	130.338 133	1.211 <sub>NO</sub>	1.053 <sub>NH</sub>	108.0 <sub>∠ONH</sub>			
HNO( $\tilde{a}^3A''$ )	130.307 335	1.218 <sub>NO</sub>	1.026 <sub>NH</sub>	120.2 <sub>∠ONH</sub>			
HONO( $\tilde{X}^1A'$ )	205.497 705	1.422 <sub>HO-NO</sub>	1.171 <sub>HON-O</sub>	0.965 <sub>HO</sub>	110.7 <sub>∠ONO</sub>	102.0 <sub>∠HON</sub>	
HNO <sub>2</sub> ( $\tilde{X}^1A_1$ )	205.485 069	1.217 <sub>NO</sub>	1.034 <sub>NH</sub>	128.2 <sub>∠ONO</sub>	115.9 <sub>∠HNO</sub>		
NO <sub>2</sub> ( $\tilde{X}^2A_1$ )	204.862 081	1.195 <sub>NO</sub>	134.2 <sub>∠ONO</sub>				
NO <sub>2</sub> ( $\tilde{A}^2B_2$ )	204.814 133	1.258 <sub>NO</sub>	101.2 <sub>∠ONO</sub>				
NO <sub>2</sub> ( $\tilde{B}^2\Pi_u$ )	204.797 862	1.201 <sub>NO</sub>					
NO <sub>2</sub> ( $\tilde{C}^2A''$ )	204.786 491	1.167 <sub>NO_1</sub>	1.498 <sub>NO_2</sub>	109.6 <sub>∠O_1NO_2</sub>			
NO <sub>2</sub> ( $\tilde{C}^2A_2$ )	204.783 327	1.275 <sub>NO</sub>	109.9 <sub>∠ONO</sub>				
NO <sub>3</sub> ( $\tilde{X}^2A'_2$ )	279.930 737	1.233 <sub>NO_{1,2,3}}</sub>	120.0 <sub>∠ONO</sub>				
NO <sub>3</sub> ( $\tilde{A}^2E''$ )	279.888 325	1.261 <sub>NO_{1,2,3}}</sub>	120.0 <sub>∠ONO</sub>				
NO <sub>3</sub> ( $\tilde{A}^2B_1$ )	279.902 927	1.424 <sub>NO_1</sub>	1.204 <sub>NO_{2,3}}</sub>	114.7 <sub>∠O_1NO_{2,3}}</sub>	130.6 <sub>∠O_2NO_3</sub>		
NO <sub>3</sub> ( $\tilde{A}^2A_2$ )	279.895 105	1.202 <sub>NO_1</sub>	1.293 <sub>NO_{2,3}}</sub>	123.8 <sub>∠O_1NO_{2,3}}</sub>	112.5 <sub>∠O_2NO_3</sub>		
NO <sub>3</sub> ( $\tilde{B}^2E'$ )	279.857 994	1.266 <sub>NO_{1,2,3}}</sub>	120.0 <sub>∠ONO</sub>				
NO <sub>3</sub> ( $\tilde{B}^2A_1$ )	279.860 328	1.236 <sub>NO_1</sub>	1.283 <sub>NO_{2,3}}</sub>	118.3 <sub>∠O_1NO_{2,3}}</sub>	123.3 <sub>∠O_2NO_3</sub>		

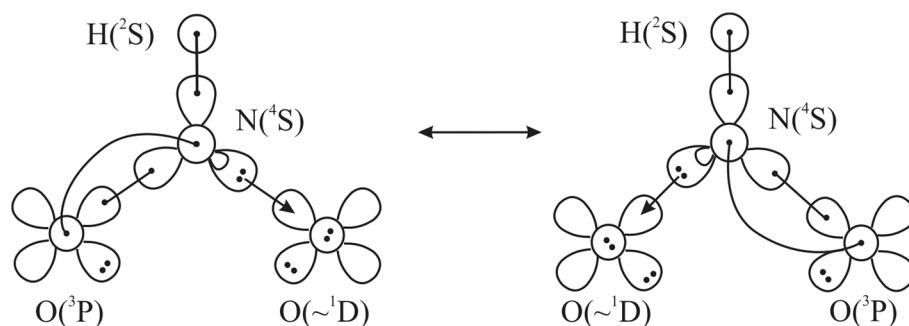
<sup>a</sup>NO<sub>1</sub> defines the C<sub>2v</sub> axis of the C<sub>2v</sub> point group

At the CASSCF equilibrium geometry, the wavefunction of the H–NO<sub>2</sub> ground state is dominated ( $C_0=0.95$ ) by the  $(1-10)a^{r^2}(1-2)a''^{r^2}$  electronic configuration characteristic of the HNO( $\tilde{X}^1A'$ ) + O( $^1D$ ) asymptote while the open singlet character of the HNO( $\tilde{a}^3A''$ ) + O( $^3P$ ) channel passes through to the second and third  $^1A'$  states. The upshot of the above discussion is that there is a double ( $\sigma, \pi$ ) N=O bond, a single dative N→O bond and a plain single N–H bond in H–NO<sub>2</sub>, where one of the O atoms is found in situ in its excited  $^1D$  (actually a mixture of  $^1D$  and  $^1S$ ) state and the other in its ground  $^3P$  one, while in nitrous acid, HO–N=O, both O atoms are found in their  $^3P$  ground states.

**Scheme 1** vbL diagram of NO ( $X^2\Pi$ )**Scheme 2** vbL diagram of NO ( $a^4\Pi$ )

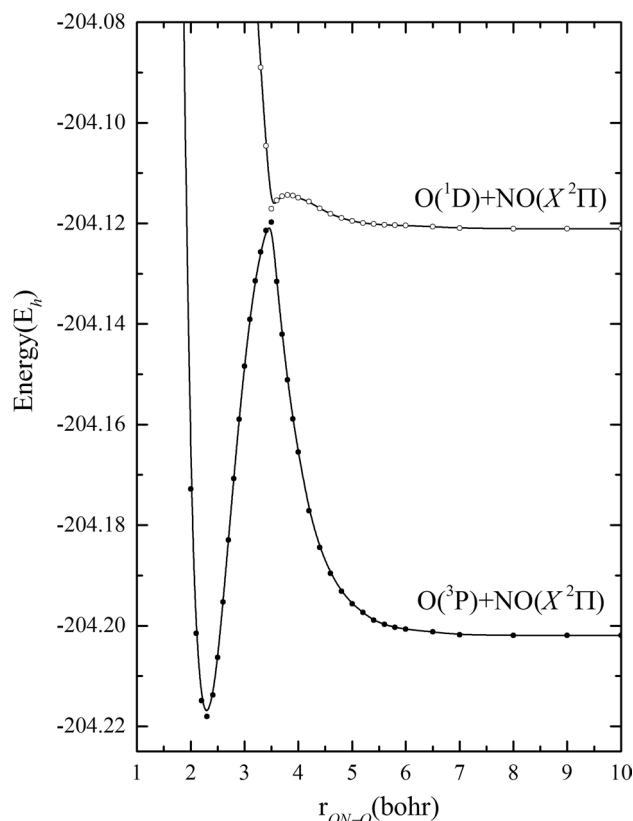
At this point, it is informative to compare H–NO<sub>2</sub> to the isoelectronic and isoivalent O<sub>3</sub> species since NH( $X^3\Sigma^-$ ) is

**Fig. 1** SACASSCF/cc-pVQZ potential energy curves ( $^1A'$ ) of the planar HNO+O interaction. The HNO unit features the equilibrium parameters of the ground HNO<sub>2</sub> species

**Scheme 3** vbL diagram of the ground HNO<sub>2</sub> state

isoelectronic and isoivalent to O (<sup>3</sup>P). As we have already shown [73, 74], the  $\tilde{X}^1A'_1O_3$  state is bound by a double ( $\sigma$ ,  $\pi$ ) bond and a single dative bond between the central and the terminal O atoms, as is the case between NH and the two terminal O atoms in H–NO<sub>2</sub>.

In order to decipher the chemical bond in NO<sub>3</sub> we should first understand NO<sub>2</sub> and the way it is formed. NO<sub>2</sub> is a notoriously difficult molecule with both an academic and environmental interest. It has been the subject of numerous theoretical studies during the last 50 years, see, e.g., Refs. [75–91]. It has a rich and complicated electronic spectrum primarily due to conical intersections. A recent synoptical presentation of the problems encountered in its study can be found in Ref. [91]. The focus of the NO<sub>2</sub> research is on its first four electronic states of  $\tilde{X}^2A_1$ ,  $\tilde{A}^2B_2$ ,  $\tilde{B}^2B_1(^2\Pi_u)$  and  $\tilde{C}^2A''$  symmetry with potential energy minima within an energy range of 2 eV; see Table 1 for RCCSD(T)/cc-pVQZ theoretical results. Its basic ingredient is clearly NO ( $X^2\Pi$ ) that features a regular  $\sigma$  and  $\pi$  bonds (see Scheme 1). A second O atom can approach either in its ground <sup>3</sup>P or its first excited <sup>1</sup>D state. The bent  $\tilde{X}^2A_1$  NO<sub>2</sub> state becomes a  $^2\Pi_u$  linear state. So, how can one form a linear ONO ( $^2\Pi_u$ ) state from NO ( $X^2\Pi$ ) + O? The answer is shown in Fig. 2 that displays the CASSCF (17 valence electrons/12 valence orbitals) potential curves of the NO ( $X^2\Pi$ ) + O (<sup>3</sup>P or <sup>1</sup>D) interaction. The NO ( $X^2\Pi$ ) + O (<sup>3</sup>P) attack is clearly repulsive, and this is expected on the basis of its asymptotic configuration, that is NO ( $X^2\Pi$ ) + O (<sup>3</sup>P;  $2p_x^1 2p_y^1 2p_z^2$ ). But the NO ( $X^2\Pi$ ) + O (<sup>1</sup>D) attack is attractive due to the dative  $\sigma$  bond between the  $2s^2(N)$  and O ( $2p_x^2 2p_y^2$ ;  $\sim^1D$ ) distributions. The Mulliken (NBO) population of the nitrogen  $2s^{1.20}$  ( $2s^{1.15}$ ) orbital and the  $-0.17$  ( $-0.36$ ) Mulliken (NBO) charge on the O atoms reflect once again the dative nature of the bonding mechanism. Graphically, it is described by Scheme 4.



**Fig. 2** SACASSCF/cc-pVQZ potential energy curves ( $^2\Pi$ ) of the linear NO + O interaction. The minimum of the lowest curve is of  $^2\Pi_u$  symmetry, while NO features the distance as found in ONO ( $X^2\Pi_u$ )

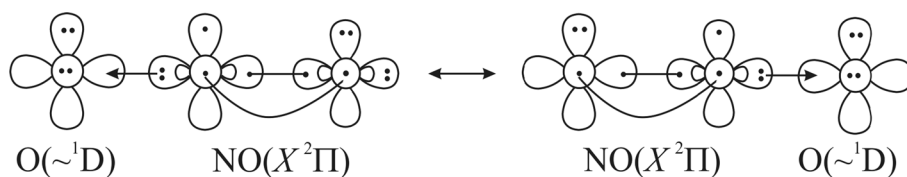
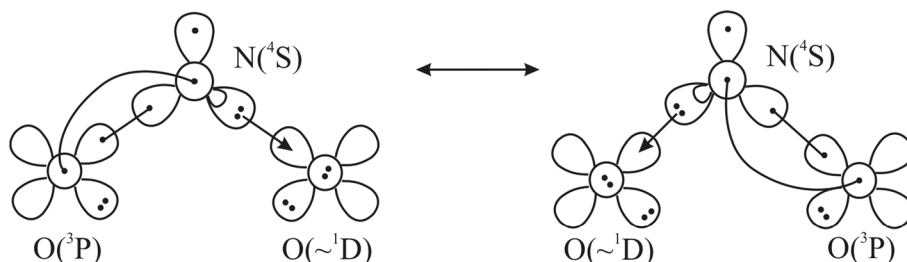
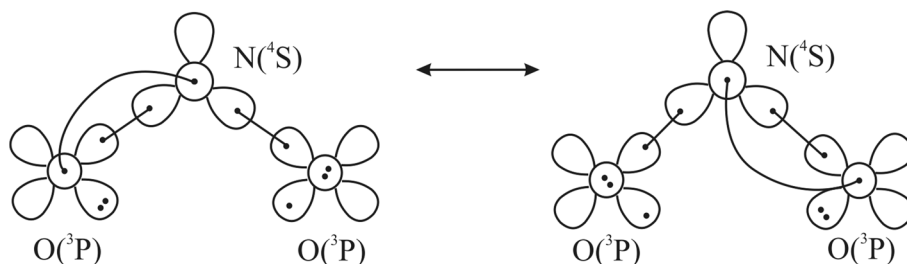
By bending it, we get NO<sub>2</sub> ( $\tilde{X}^2A_1$ ) with CASSCF (17 valence electrons/12 valence orbitals) equilibrium characteristics

$$|\tilde{X}^2A'(\tilde{X}^2A_1)\rangle \cong 0.94|(1-9)a'^2 10a'^1(1-2)a''^2\rangle \quad \text{with}$$

$$10a' \sim -0.36 \times 2s(N) - 0.32 \times s'(N) + 0.64 \times 2p_z(N) - 0.58 \times [2p_z(O_1) + 2p_z(O_2)],$$

$$\text{and atomic populations (Mulliken)} \quad 2s^{1.47} 2p_x^{1.0} 2p_y^{0.84} 2p_z^{1.18} /_N 2s^{1.83} 2p_x^{1.45} 2p_y^{1.29} 2p_z^{1.55} /_{O_{1,2}}$$

$$\text{and (NBO)} \quad 2s^{1.22} 2p_x^{0.87} 2p_y^{0.94} 2p_z^{1.20} /_N 2s^{1.76} 2p_x^{1.55} 2p_y^{1.39} 2p_z^{1.62} /_{O_{1,2}}.$$

**Scheme 4** vbL diagram of the linear ONO ( $\tilde{X}^2\Pi_u$ ) configuration**Scheme 5** vbL diagram of the ground NO<sub>2</sub> state**Scheme 6** vbL diagram of the first excited ( $\tilde{A}^2B_2$ ) NO<sub>2</sub> state

The NO<sub>2</sub> ( $\tilde{X}^2A_1$ ) state is mainly described graphically by Scheme 5.

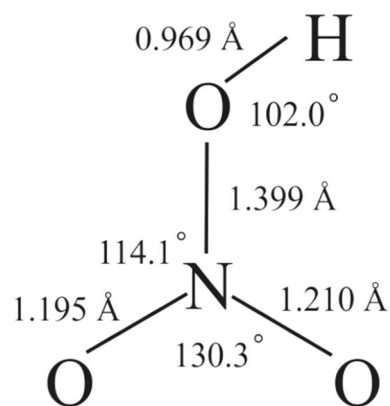
The above analysis is also in agreement with the bonding characteristics of the H–NO<sub>2</sub> ( $\leftarrow$ HNO<sub>2</sub> + O) species discussed above.

The first excited  $\tilde{A}^2B_2$  state with CASSCF (17 valence electrons/12 valence orbitals) equilibrium characteristics

$$|\tilde{A}^2A'(\tilde{A}^2B_2)\rangle \cong 0.92|(1-9)a^210a'^1(1-2)a''^2\rangle \quad \text{with} \\ 10a' \sim 0.62 \times [2p_y(O_1) + 2p_y(O_2)] - 0.43 \times [2p_z(O_1) - 2p_z(O_2)]$$

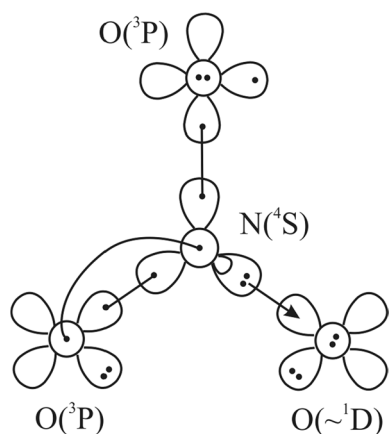
has its in-plane odd electron localized on the O atoms, and this can happen from the NO ( $X^2\Pi$ ) + O ( $^3P$ ) bent interaction as also analyzed in the planar ON–OH case (see above) and depicted graphically in Scheme 6.

It is clear that nitrous acid, HO–NO ( $110.7^\circ_{\angle\text{ONO}}$ ; Table 1), traces its diabatic lineage to the  $\tilde{A}^2B_2$  NO<sub>2</sub> ( $101.2^\circ_{\angle\text{ONO}}$ ; Table 1) state while H–NO<sub>2</sub> ( $128.2^\circ_{\angle\text{ONO}}$ ; Table 1) to  $\tilde{X}^2A_1$  NO<sub>2</sub> ( $134.2^\circ_{\angle\text{ONO}}$ ; Table 1). There is also a number of well-known chemical species that relate to NO<sub>2</sub> ( $\tilde{X}^2A_1$ ). These are O<sub>2</sub>N–NO<sub>2</sub> ( $135^\circ_{\angle\text{ONO}}$ ), HO–NO<sub>2</sub> ( $130^\circ_{\angle\text{ONO}}$ ), ON–NO<sub>2</sub> ( $130^\circ_{\angle\text{ONO}}$ ) and H<sub>2</sub>N–NO<sub>2</sub> ( $130^\circ_{\angle\text{ONO}}$ ) [92]. In all of the above species, the ONO angle is practically identical to the one in the ground NO<sub>2</sub> state and there is a single bond between NO<sub>2</sub> and the incoming ligand. The most interesting case is nitric

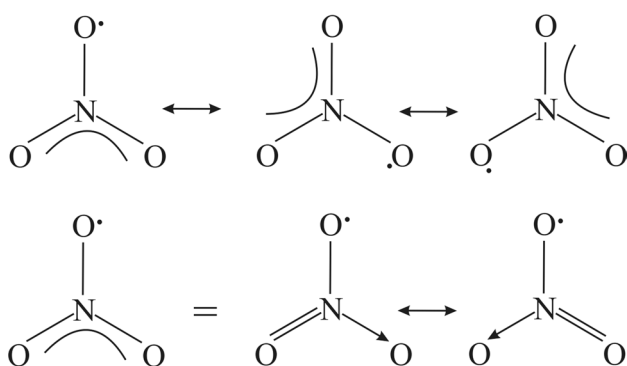
**Scheme 7** Molecular parameters of the ground HNO<sub>3</sub> state at the RCCSD(T)/cc-pVQZ computational level

acid, HO–NO<sub>2</sub>, featuring one  $\sigma$  bond between HO( $X^2\Pi$ ) and NO<sub>2</sub> ( $\tilde{X}^2A_1$ ), a double ( $\sigma$ ,  $\pi$ ) and a dative  $\sigma$  bond between N and the terminal O atoms. It has a planar  $C_s$  structure with its RCCSD(T)/cc-pVQZ molecular parameters appearing in Scheme 7.

By detaching the H atom, we get a  $^2A'$  NO<sub>3</sub> species that becomes its  $\tilde{X}^2A'_2$  state upon geometry optimization. So, the



**Scheme 8** vbL diagram of  $\text{NO}_3$  ( ${}^2A'$ )

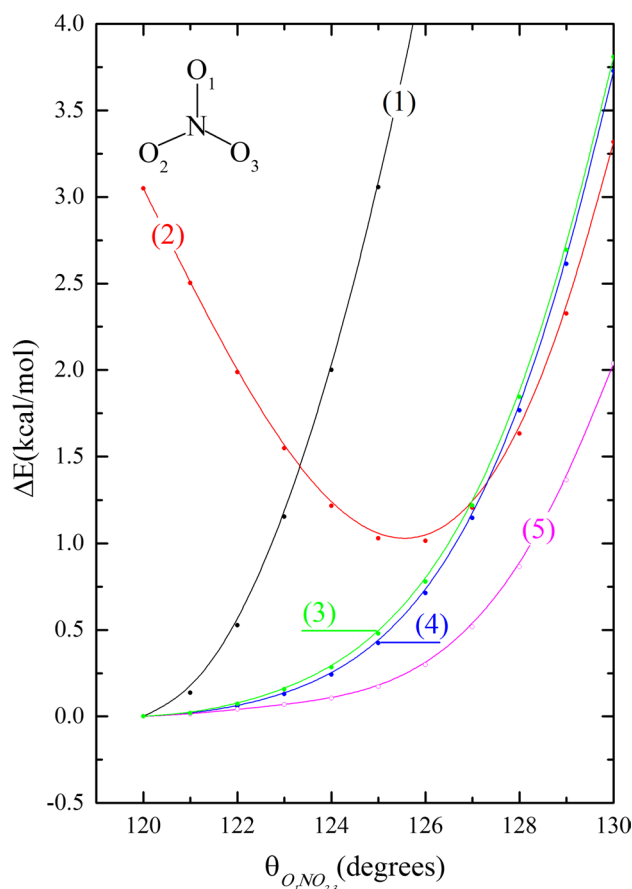


**Scheme 9** Resonant vbL structures of the ground  $\text{NO}_3$  state

generic type of bonding in the ground  $\text{NO}_3$  state is captured by the vbL diagram of Scheme 8.

There are three different chemical bonds in  $\text{NO}_3$ , a regular ( $2e^- - 2$  center)  $\sigma$ , a dative  $\sigma$  and a double  $\sigma, \pi$ , while the odd electron rests on a single O atom. Once again, the Mulliken (NBO) population and charges  $2s_N^{1.19}$  ( $2s_N^{1.05}$ ) and  $q(\text{O}) = -0.21$  ( $-0.29$ ),  $q(\text{N}) = +0.64$  ( $+0.88$ ) mirror the character of the chemical bond. The equilateral symmetry dictates similar vbL structures in which the odd electron can be found on all three O atoms that upon interaction confer it a  $D_{3h}$  equilibrium structure. This is graphically represented by the vbL diagram shown in Scheme 9.

The addition of an H atom destroys the above resonance, the wave function collapses into one of the three vbL structures, and the electron localizes on a particular O atom, and thus, we get a (quasi) $C_{2v}$ (H)O– $\text{NO}_2$  unit featuring one long and two short NO distances as found also in previous studies [13]. Thus, the  $D_{3h}$  structure of the ground  $\text{NO}_3$  species is due to the resonance of all the vbL structures shown in Scheme 9.



**Fig. 3** (R or U)CCSD(T)/cc-pVQZ potential energy curves (PEC) of the ground  $\text{NO}_3$  species along the  $\theta$  ( $\text{O}_1\text{NO}_2=\text{O}_1\text{NO}_3$ ) coordinate. At each energy point, the NO distances are optimized. PEC\_(1) (black) and \_(2) (red) are obtained at the ROHF( $\text{NO}_3$ )-RCCSD(T) level featuring a  $D_{3h}$  and  $C_{2v}$  energy minima, respectively, while PEC\_(3) (green), \_(4) (blue) and \_(5) (magenta) at the ROHF( $\text{NO}_3^-$ )-UCCSD(T), ROHF( $\text{NO}_3^-$ )-RCCSD(T) and ROHF( $\text{NO}_3^-$ )-UCCSD(T), respectively. The latter three PECs have been shifted so that their minima coincide to PEC\_(1)'s minimum (see Table 2 for absolute energies)

The symmetry breaking problem of the  $\tilde{X}^2A'_2$  state is illustrated in Fig. 3 that displays RCCSD(T) and UCCSD(T) potential energy curves along the  $\theta$  ( $\text{O}_1\text{NO}_2=\text{O}_1\text{NO}_3$ ) coordinate based on ROHF orbitals of either the neutral  $\text{NO}_3$  or anionic  $\text{NO}_3^-$  species. PEC\_(1) and PEC\_(2) are based on two different ROHF( $\text{NO}_3$ ) solutions that produce curves with either  $D_{3h}$  (see Table 2) or  $C_{2v}$  ( $E_e = -279.929\ 146 E_h$ ,  $r_e$  ( $\text{NO}_1$ ) = 1.197 Å,  $r_e$  ( $\text{NO}_{2,3}$ ) = 1.258 Å,  $\theta$  ( $\text{O}_2\text{NO}_3$ ) = 108.9°,  $\omega_e = 504, 636, 797, 1082, 1199, 1596\ \text{cm}^{-1}$ ) energy minima, respectively. Both  $D_{3h}$  and  $C_{2v}$  structures are chemical entities that should be considered evenly in order to accurately map the adiabatic surface of the ground  $\text{NO}_3$  state and it appears that ROHF( $\text{NO}_3$ )-UCCSD(T) or ROHF( $\text{NO}_3^-$ )-(R or U)CCSD(T) computational schemes are suitable for that.



**Table 2** Energies  $E$  (hartree), bond distances  $r_e$  (Å), harmonic frequencies  $\omega_e$  ( $\text{cm}^{-1}$ ) and electron affinity EA (eV) of the ground  $D_{3h}$   $\tilde{X}^2A'_2$  ( $\text{NO}_3$ ) and  $\tilde{X}^1A'$  ( $\text{NO}_3^-$ ) states at the ROHF-(R or U)CCSD(T)/(aug)-cc-pVQZ computational level

Species	$-E$	$r_e$	$\omega_e$ ( $q_4, q_2, q_1, q_3$ )	EA
$\text{NO}_3(\tilde{X}^2A'_2)$	279.930 737 <sup>a</sup>	1.233 <sup>a</sup>	614 ( $b_2, a_1$ ), 793 ( $b_1$ ), 1106 ( $a_1$ ), 1497 ( $b_2, a_1$ ) <sup>a</sup>	
	279.931 433 <sup>b</sup>	1.234 <sup>b</sup>	280 ( $b_2, a_1$ ), 793 ( $b_1$ ), 1107 ( $a_1$ ), 1131 ( $b_2, a_1$ ) <sup>b</sup>	
	279.929 216 <sup>c</sup>	1.233 <sup>c</sup>	263 ( $b_2, a_1$ ), 794 ( $b_1$ ), 1108 ( $a_1$ ), 1162 ( $b_2, a_1$ ) <sup>c</sup>	
	279.929 970 <sup>d</sup>	1.233 <sup>d</sup>	289 ( $b_2, a_1$ ), 794 ( $b_1$ ), 1108 ( $a_1$ ), 1171 ( $b_2, a_1$ ) <sup>d</sup>	
			369 ( $b_2, a_1$ ), 764 ( $b_1$ ), 1067 ( $a_1$ ), 1099 ( $b_2, a_1$ ) <sup>e</sup>	
			388 ( $b_2, a_1$ ), 808 ( $b_1$ ), 1095 ( $a_1$ ), 1067 ( $b_2, a_1$ ) <sup>f</sup>	
			349 ( $b_2, a_1$ ), 773 ( $b_1$ ), 1085 ( $a_1$ ), 1140 ( $b_2, a_1$ ) <sup>g</sup>	
			361 ( $b_2, a_1$ ), 1051 ( $a_1$ ), 994 ( $b_2, a_1$ ) <sup>h</sup>	
			237 ( $b_2, a_1$ ), 793 ( $b_1$ ), 1155 ( $a_1$ ), 1412 ( $b_2, a_1$ ) <sup>i</sup>	
		[1.24] <sup>j</sup> (279.940 813)	(1.234)	[365( $b_2, a_1$ ), <sup>k</sup> 762 ( $b_1$ ), <sup>k</sup> 1051( $a_1$ ), <sup>l</sup> ( $b_2, a_1$ ) <sup>m</sup> ]
$\text{NO}_3^-(\tilde{X}^1A')$	280.073 084	1.255	717 ( $b_2, a_1$ ), 859 ( $b_1$ ), 1066 ( $a_1$ ), 1423 ( $b_2, a_1$ )	3.87
			[723 ( $b_2, a_1$ ), 834 ( $b_1$ ), 1054 ( $a_1$ ), 1379 ( $b_2, a_1$ ) <sup>n</sup> ]	
	(280.090 367)	(1.257)		(4.07)
		[1.23] <sup>n</sup>		[3.937 ± 0.014] <sup>n</sup>

Experimental results in square brackets

<sup>a</sup>ROHF( $\text{NO}_3$ )-RCCSD(T) results, see also PEC\_(1) in Fig. 3

<sup>b</sup>ROHF( $\text{NO}_3$ )-UCCSD(T) results, see also PEC\_(5) in Fig. 3

<sup>c</sup>ROHF( $\text{NO}_3^-$ )-RCCSD(T) results, see also PEC\_(4) in Fig. 3

<sup>d</sup>ROHF( $\text{NO}_3^-$ )-UCCSD(T) results, see also PEC\_(3) in Fig. 3

<sup>e</sup>Scaled results based on a MSCAS(17e-/13o)PT2/aug-cc-pVTZ surface; unscaled ones are 392, 733, 1066 and 1162  $\text{cm}^{-1}$ , Ref. [33]

<sup>f</sup>EOMIP-CCSD/[3s2p1d] results based on the adiabatic approximation, Ref. [29]

<sup>g</sup>UCCSD(T)/ADZ results, Ref. [27]

<sup>h</sup>Results based on the KDC Hamiltonian and on EOMIP-CCSD/cc-pVTZ ab initio energy points, Ref. [26]

<sup>i</sup>MRCISD/AVTZ-f; MRCISD+Q results are 273, 773, 1083 and 1376  $\text{cm}^{-1}$ , Ref. [23]

<sup>j</sup>References [41, 42]

<sup>k</sup>Reference [61]

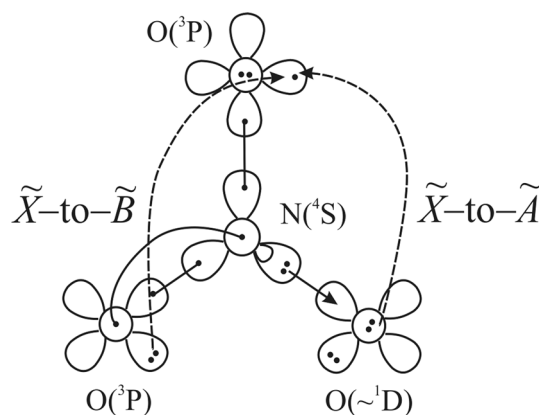
<sup>l</sup>References [39, 40]

<sup>m</sup>1087  $\text{cm}^{-1} \leq \omega_3 \leq 1127 \text{ cm}^{-1}$ , see Ref. [58],  $\omega_3 = 1492 \text{ cm}^{-1}$ , see, e.g., Ref. [64] and  $\omega_3 = 1044(16) \text{ cm}^{-1}$ , see Ref. [93]

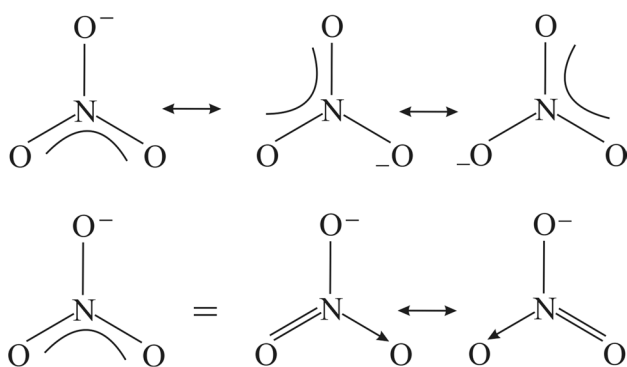
<sup>n</sup>Reference [42]

The above two “structures” lie in the heart of the  $C_{2v}/D_{3h}$  problem of the past.

It is interesting to comment on the behavior of the harmonic frequencies according to the computational schemes used (see Table 2). Although the  $\omega_2$  and  $\omega_1$  values are practically equal at all levels of theory employed, this is not the case for  $\omega_3$  and  $\omega_4$ . The computational schemes that take into account both  $D_{3h}$  and  $C_{2v}$  minima (PEC\_(3, 4, 5)) give values that are much closer to the experimental and some previous theoretical values. It turns out that the latter  $\omega_3$  values (see Table 2) are closer to the experimental expectation  $1087 \leq \omega_3 \leq 1127 \text{ cm}^{-1}$  (see Ref. [58]) and to the KDC value of 1069  $\text{cm}^{-1}$  (see Ref. [29]) than the 1492  $\text{cm}^{-1}$  value (see Ref. [64]). Based on our bonding analysis and the form of the potential curves, we believe that the  $\sim 1000 \text{ cm}^{-1}$  should be the correct one. And this is indeed the case as shown recently by the high-resolution photoelectron spectroscopy



**Scheme 10** vbL diagram of the (generic) electronic excitations from the ground to the first and second excited  $\text{NO}_3$  states



**Scheme 11** Resonant vbL structures of the ground  $\text{NO}_3^-$  state

of cryogenically cooled  $\text{NO}_3^-$  establishing a value of  $1044(16) \text{ cm}^{-1}$  [93].

Now that we understand the bonding nature of the ground  $\text{NO}_3$  state, it is not a difficult task to delve into the bonding character of its excited  $\tilde{A}^2E''(1^2B_1, 1^2A_2)$  and  $\tilde{B}^2E'$  ( $1^2A_1, 2^2B_2$ ) states. Under  $D_{3h}(C_{2v})$  symmetry labeling, the  $\tilde{A}^2E''(2A_2 \text{ or } 2B_1)$  state is realized through an  $e''(a_2 \text{ or } b_1) \rightarrow a_2'(b_2)$  transition, while the  $\tilde{B}^2E'(2A_1 \text{ or } 2B_2)$  state is realized through an  $e'(a_1 \text{ or } b_2) \rightarrow a_2'(b_2)$  excitation. Considering also the composition of the out-of-plane ( $e''$ )/in-plane ( $e'$ ) ( $\text{NO}_3$ ) molecular orbitals, we can easily visualize the  $\tilde{X}^2A_2' \rightarrow \tilde{A}^2E''/\tilde{B}^2E'$  transitions with the help of the  $C_s$  bonding motif shown in Scheme 10.

The resulting  $\tilde{A}^2E''$  and  $\tilde{B}^2E'$  states are Jahn–Teller active and give rise to  $C_{2v}$  structures of  $1^2B_1, 1^2A_2$  and  $1^2A_1, 2^2B_2$  symmetry, respectively; see Table 1 for their molecular parameters. In the  $1^2B_1$  state [ $T_e = 6104 \text{ cm}^{-1}; 7062.25(50) \text{ cm}^{-1}$  (exp.  $T_0$  value, see, e.g., Refs. [44] and [60])], the  $\pi$  electron is localized on the O atom that defines the  $C_2$  axis while in the  $1^2A_2$  state on the two equivalent O atoms. In the  $\tilde{B}$  states [ $T_e(1^2A_1) = 15,453 \text{ cm}^{-1}; 15,109 \text{ cm}^{-1}$  (exp.  $T_0$  value, see, e.g., Ref. [51])], the in-plane odd electron is on  $2p_y2p_z$  hybrids of the two equivalent O atoms.

Based on Scheme 8, we can easily understand the chemical structure of  $\text{NO}_3^-$ . The negative charge finds its way into the half-occupied O orbital. The Mulliken (NBO) population and charges  $2s_N^{1.24}$  ( $2s_N^{1.05}$ ) and  $q(\text{O}) = -0.54$  ( $-0.63$ ),  $q(\text{N}) = +0.61$  ( $+0.89$ ) are in agreement with the bonding situation. The additional electron is shared equally ( $1/3 = 0.33$ ) by all O atoms as witnessed by the Mulliken charges of the neutral ( $q(\text{O}) = -0.21$ ) and anion ( $q(\text{O}) = -0.54$ ), while that of N remains unaltered (see the vbL diagram of Scheme 11).

Its molecular parameters and its harmonic frequencies appear in Table 2. The computed electron affinity  $\text{EA} = 3.87$  (4.07) eV at the RCCSD(T)/(aug)-cc-pVQZ computational level is in fair agreement with the experimental value of  $3.937 \pm 0.014$  eV [44]. Interestingly enough, the EA value at the ROHF( $\text{NO}_3^-$ )-RCCSD(T)/(cc-pVQZ computational

level  $\text{EA} = 3.91$  eV is in much closer agreement with the experimental one.

### 3 Conclusions

The nitrate radical,  $\text{NO}_3$ , is a notoriously difficult species both in terms of bonding and of its spectral behavior complicated by various nonadiabatic couplings. All of its peculiarities should be traced back to the way the three O atoms bind to nitrogen. And this is exactly the subject matter of the present study. We have followed a  $\text{NO}$ -to- $\text{NO}_2$ -to- $\text{NO}_3$  formation path and have shown that the equilateral equilibrium structure of its ground  $\tilde{X}^2A_2'$  state is due to the resonance of vbL structures, each one of them featuring three different chemical bonds between N and O, one double  $\sigma, \pi$  with an O ( $^3P$ ), one dative  $\sigma$  with an excited O ( $\sim ^1D$ ) and finally a regular  $\sigma$  with a ground O ( $^3P$ ). The presence of an H atom (in  $\text{HO-NO}_2$ ) breaks the resonance of the  $\text{NO}_3$  unit conferring it a (quasi)  $C_{2v}$  character. An additional electron finds its place into the “hole” of the neutral radical, and consequently the anion features a similar  $D_{3h}$  structure.

### References

- Chappuis J (1882) Ann Sci ENS 11:137–186
- Hautefeuille P, Chappuis J (1881) C R Acad Sci Paris 92:80
- Atmospheric Ozone 1985: assessment of our understanding of the processes controlling its present distribution and change, World Meteorological Organization, Global Ozone Research and Monitoring Project-Report No. 16 (NASA, Washington DC, 1985), pp 32–35
- Johnston HS, Podolski J (1978) Rev Geophys Space Phys 16:491–519
- Seinfeld H (1989) Science 243:745–752
- Wayne RP, Barnes I, Biggs P, Burrows JP, Canosa-Mas CE, Hjorth JE, LeBras G, Moortgat GK, Perner D, Poulet G, Restelli G, Sidebottom H (1991) Atmos Environ 25A:1–203
- Wayne RP (1991) Chemistry of atmospheres. Clarendon, Oxford
- Platt U, Perner D, Winer AM, Harris GW, Pitts JV Jr (1980) Geophys Res Lett 7:89–92
- Noxon JF, Norton RB, Marovich E (1980) Geophys Res Lett 7:125–128
- Platt U, Heinz F (1994) Isr J Chem 34:289–300
- Atkinson R (2000) Atmos Environ 34:2063–2101
- Monks PS (2005) Chem Soc Rev 34:376–395
- Siegbahn PEM (1985) J Comput Chem 6:182–188
- Boehm RC, Lohr LL (1989) J Phys Chem 93:3430–3433
- Davy RD, Schaefer HF III (1989) J Chem Phys 91:4410–4411
- Kaldor U (1990) Chem Phys Lett 166:599–601
- Kim B, Hammond BL, Lester WA, Johnston HS (1990) Chem Phys Lett 168:131–134
- Stanton JF, Gauss J, Bartlett RJ (1991) J Chem Phys 94:4084–4087
- Stanton JF, Gauss J, Bartlett RJ (1992) J Chem Phys 97:5554–5559
- Mayer M, Cederbaum LS, Köppel H (1994) J Chem Phys 100:899–911
- Eisfeld W, Morokuma K (2000) J Chem Phys 113:5587–5597
- Cohen RD, Sherrill CD (2001) J Chem Phys 114:8257–8269



23. Einfeld W, Morokuma K (2001) *J Chem Phys* 114:9430–9440
24. Viel A, Einfeld W (2004) *J Chem Phys* 120:4603–4613
25. Mahapatra S, Einfeld W, Köppel H (2007) *Chem Phys Lett* 441:7–15
26. Stanton JF (2007) *J Chem Phys* 126:134309
27. Glendening ED, Halpern AM (2007) *J Chem Phys* 127:164307
28. Faraji S, Köppel H, Einfeld W, Mahapatra S (2008) *Chem Phys* 347:110–119
29. Stanton JF (2009) *Mol Phys* 107:1059–1075
30. Stanton JF, Okumura M (2009) *Phys Chem Chem Phys* 11:4742–4744
31. Grein F (2013) *J Chem Phys* 138:204305
32. Einfeld W, Vieuxmaire O, Viel A (2014) *J Chem Phys* 140:224109
33. Homayoon Z, Bowman JM (2014) *J Chem Phys* 141:161104
34. Mukherjee B, Mukherjee S, Sardar S, Shamasundar KR, Adhikari S (2017) *Mol Phys* 115:2833–2848
35. Mukherjee B, Mukherjee S, Adhikari S (2017) *J Phys Chem A* 121:6314–6326
36. Einfeld W, Viel A (2017) *J Chem Phys* 146:034303
37. Viel A, Einfeld W (2018) *Chem Phys* 509:81–90
38. Mukherjee B, Mukherjee S, Sardar S, Shamasundar KR, Adhikari S (2018) *Chem Phys* 515:350–359
39. Nelson HH, Pasternack L, McDonald JR (1983) *J Phys Chem* 87:1286–1288
40. Ishiwata T, Fujiwara L, Naruge Y, Obi K, Tanaka I (1983) *J Phys Chem* 87:1349–1352
41. Ishiwata T, Tanaka I, Kawaguchi K, Hirota E (1985) *J Chem Phys* 82:2196–2205
42. Friedl RR, Sander SP (1987) *J Phys Chem* 91:2721–2726
43. Kawaguchi K, Hirota E, Ishiwata T, Tanaka I (1990) *J Chem Phys* 93:951–956
44. Weaver A, Arnold DW, Bradforth SE, Neumark DM (1991) *J Chem Phys* 94:1740–1751
45. Monks PS, Stief LJ, Krauss M, Kuo SC, Zhang Z, Klemm RB (1994) *J Phys Chem* 98:10017–10022
46. Kawaguchi K, Ishiwata T, Tanaka I, Hirota E (1991) *Chem Phys Lett* 180:436–440
47. Kawaguchi K, Ishiwata T, Hirota E, Tanaka I (1998) *Chem Phys* 231:193–198
48. Ishiwata T, Tanaka I, Kawaguchi K, Hirota E (1992) *J Mol Spectrosc* 153:167–180
49. Wang D, Jiang P, Qian X, Hong G (1997) *J Chem Phys* 106:3003–3006
50. Kim BS, Hunter PL, Johnston HS (1992) *J Chem Phys* 96:4057–4067
51. Carter RT, Schmidt KF, Bitto H, Huber JR (1996) *Chem Phys Lett* 257:297–302
52. Hirota E, Ishiwata T, Kawaguchi K, Fujitake M, Obashi V, Tanaka I (1997) *J Chem Phys* 107:2829–2838
53. Okumura M, Stanton JF, Deev A, Sommar J (2006) *Phys Scr* 73:C64–C70
54. Hirota E, Kawaguchi K, Ishiwata T, Tanaka I (1991) *J Chem Phys* 95:771–775
55. Nelson HH, Pasternack L, McDonald JR (1983) *J Chem Phys* 79:4279–4284
56. Jacox ME, Thompson WE (2008) *J Chem Phys* 129:204306
57. Jacox ME, Thompson WE (2010) *J Phys Chem A* 114:4712–4718
58. Kawaguchi K, Shimizu N, Fujimori R, Tang J, Ishiwata T, Tanaka I (2011) *J Mol Spectrosc* 268:85–92
59. Simmons CS, Ichino T, Stanton JF (2012) *J Phys Chem Lett* 3:1946–1950
60. Takematsu K, Eddingsaas NC, Robichaud DJ, Okumura M (2013) *Chem Phys Lett* 555:57–63
61. Fujimori R, Shimizu N, Tang J, Ishiwata T, Kawaguchi K (2013) *J Mol Spectrosc* 283:10–17
62. Kawaguchi K, Fujimori R, Tang J, Ishiwata T (2013) *J Phys Chem A* 117:13732–13742
63. Tada K, Kashiwara W, Baba M, Ishiwata T, Hirota E, Kasahara S (2014) *J Chem Phys* 141:184307
64. Hirota E (2015) *J Mol Spectrosc* 310:99–104
65. Codd T, Chen M-W, Roudjane M, Stanton JF, Miller RA (2015) *J Chem Phys* 142: 184305
66. Tada K (2019) *Chem Phys* 524:21–25
67. Sharma K, Garner S, Miller TA, Stanton JF (2019) *J Phys Chem A* 123:4990–5004
68. Köppel H, Domcke W, Cederbaum LS (1984) *Adv Chem Phys* 57:59–246
69. Dunning TH Jr (1989) *J Chem Phys* 90:1007–1023
70. MOLPRO is a package of ab initio programs written by Werner H-J, Knowles PJ, Knizia G, Manby FR, Schütz M, Celani P, Györfy W, Kats D, Korona T, Lindh R, Mitrushenkov A, Rauhut G, Shamasundar KR, Adler TB, Amos RD, Bernhardtsson A, Berning A, Cooper DL, Deegan MJO, Dobbyn AJ, Eckert F, Goll E, Hampel C, Hesselmann A, Hetzer G, Hrenar T, Jansen G, Köppl C, Liu Y, Lloyd AW, Mata RA, May AJ, McNicholas SJ, Meyer W, Mura ME, Nicklaß A, O'Neill DP, Palmieri P, Peng D, Pflüger K, Pitzer R, Reiher M, Shiozaki T, Stoll H, Stone AJ, Tarroni R, Thorsteinsson T, Wang M (2008) MOLPRO, version 2012.1, a package of ab initio programs. University College Cardiff Consultants Limited, Cardiff
71. Huber KP, Herzberg G (1979) Constants of diatomic molecules (data prepared by J.W. Gallagher and R.D. Johnson, III). In: Linstrom PJ, Mallard WG (eds) NIST Chemistry WebBook, NIST Standard Reference Database Number 69. National Institute of Standards and Technology, Gaithersburg. <https://doi.org/10.18434/t4d303>
72. Kramida A, Ralchenko Y, Reader J, NIST ASD Team (2018) NIST atomic spectra database (ver. 5.6.1), <https://physics.nist.gov/asd>. National Institute of Standards and Technology, Gaithersburg. <https://doi.org/10.18434/T4W30F>
73. Kalemou A, Mavridis A (2008) *J Chem Phys* 129:054312
74. Kalemou A (2016) *J Phys Chem A* 120:169–170
75. Hay PJ (1973) *J Chem Phys* 58:4706–4707
76. Jackels CF, Davidson ER (1975) *J Chem Phys* 63:4672–4677
77. Jackels CF, Davidson ER (1976) *J Chem Phys* 64:2908–2917
78. Jackels CF, Davidson ER (1976) *J Chem Phys* 65:2941–2957
79. Shih S-K, Peyrimhoff SD, Buenker RJ (1977) *Chem Phys Lett* 46:201–207
80. Xie Y, Davy RD, Yates BF, Blabous CP III, Yamaguchi Y, Schaefer HF III (1989) *Chem Phys* 135:179–186
81. Blabous CP III, Yates BF, Xie Y, Schaefer HF III (1990) *J Chem Phys* 93:8105–8109
82. Burton NA, Yamaguchi Y, Alberts IL, Schaefer HF III (1991) *J Chem Phys* 95:7466–7478
83. Crawford TD, Stanton JF, Szalay PG, Schaefer HF III (1997) *J Chem Phys* 107:2525–2528
84. Mahapatra S, Köppel H, Cederbaum LS, Stampfuß P, Wenzel W (2000) *Chem Phys* 259:211–226
85. Kurkal V, Fleurat-Lessard P, Schinke R (2003) *J Chem Phys* 119:1489–1501
86. Varandas AJC (2003) *J Chem Phys* 119:2596–2613
87. Bera PP, Yamaguchi Y, Schaefer HF III (2007) *J Chem Phys* 127:174303
88. Grein F (2008) *Chem Phys Lett* 455:124–130
89. Mota VC, Caridale PJSB, Varandas AJC (2012) *J Phys Chem A* 116:3023–3034
90. Sardar S, Mukherjee S, Paul AK, Adhikari S (2013) *Chem Phys* 416:11–20
91. Mukherjee S, Mukherjee B, Sardar S, Adhikari S (2015) *J Chem Phys* 143:244307

92. Greenwood NN, Earnshaw A (1997) Chemistry of the elements, 2nd edn. Butterworth-Heinemann, Oxford
93. Babin MC, DeVine JA, DeWitt M, Stanton JF, Neumark DM (2020) J Phys Chem Lett 11:395–400

**Publisher's Note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.