## Molecular Physics <br> An International Journal at the Interface Between Chemistry and Physics

# An ab initio study of the bonding in $\mathrm{BeH}\left(X^{2} \Sigma^{+}\right)$, $\mathrm{BeH}^{-}\left(X^{1} \Sigma^{+}\right), \mathrm{Be}_{2}\left(X^{1} \Sigma^{+}{ }_{g}\right), \mathrm{O}_{3}\left(X^{\sim} \mathrm{A}_{1}\right)$, and $\mathrm{CO}_{3}\left({ }^{\sim} X^{1} \mathrm{~A}_{1}\right)$ through an adiabatic to diabatic transformation 

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To cite this article: Apostolos Kalemos (2023): An ab initio study of the bonding in BeH $\left(X^{2} \Sigma^{+}\right), \mathrm{BeH}^{-}\left(X^{1} \Sigma^{+}\right), \mathrm{Be}_{2}\left(X^{1} \Sigma^{+}{ }_{g}\right), \mathrm{O}_{3}\left(X^{\sim 1} \mathrm{~A}_{1}\right)$, and $\mathrm{CO}_{3}\left({ }^{\sim} X^{1} \mathrm{~A}_{1}\right)$ through an adiabatic to diabatic transformation, Molecular Physics, DOI: 10.1080/00268976.2023.2230315

To link to this article: https://doi.org/10.1080/00268976.2023.2230315

Published online: 06 Jul 2023.

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# An ab initio study of the bonding in $\mathrm{BeH}\left(X^{2} \Sigma^{+}\right), \mathrm{BeH}^{-}\left(X^{1} \Sigma^{+}\right), \mathrm{Be}_{2}\left(X^{1} \Sigma^{+}{ }_{g}\right), \mathrm{O}_{3}$ ( $\tilde{X}^{1} \mathrm{~A}_{1}$ ), and $\mathrm{CO}_{3}\left(\tilde{X}^{1} \mathrm{~A}_{1}\right)$ through an adiabatic to diabatic transformation 

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ABSTRACT
We have studied the bonding situation in $\mathrm{BeH}\left(X^{2} \Sigma^{+}\right)$, $\mathrm{BeH}^{-}\left(X^{1} \Sigma^{+}\right), \mathrm{Be}_{2}\left(X^{1} \Sigma_{g}^{+}\right), \mathrm{O}_{3}\left(\tilde{X}^{1} \mathrm{~A}_{1}\right)$, and $\mathrm{CO}_{3}$ ( $\tilde{X}^{1} \mathrm{~A}_{1}$ ) both diabatically and adiabatically through MRCl calculations. In particular the Be containing species, $\mathrm{BeH}, \mathrm{BeH}^{-}$and $\mathrm{Be}_{2}$, are formed through an excited ${ }^{3} \mathrm{P}\left(2 s^{1} 2 p^{1}\right) \mathrm{Be}$ state, the ground state $\mathrm{O}_{3}$ molecule results from the interaction of the excited $\mathrm{O}_{2}\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)$ fragments and finally the $\mathrm{CO}_{3}$ species results from the combination of $\mathrm{CO}\left(a^{3} \Pi\right)+2 \mathrm{O}\left({ }^{3} \mathrm{P}\right) / \mathrm{O}_{2}\left(X^{3} \Sigma_{g}^{-}\right)$.


## ARTICLE HISTORY

Received 28 April 2023
Accepted 22 June 2023

## 1. Introduction

Chemistry studies matter and its transformation at the atomic level. Its quantum mechanical theoretical description is greatly simplified by the introduction of the

Born - Oppenheimer (BO) approximation which fixes in space the various nuclei of the molecular species. This way the various classical concepts of chemistry survive in the quantum realm [1,2]. Under the BO mathematical

[^0]and computational scheme the atoms emerge as building blocks of the molecular species while the concept of the chemical bond acquires a legitimate quantum mechanical status. In order to understand its formation we usually need to spot it as a localized entity so we have to extract this 'localized' information from a rather complicated and delocalized molecular wavefunction.

A convenient starting point for such a task is a properly designed complete active space SCF (CASSCF) wavefunction. Several localization techniques have been proposed (see e.g. Refs. [3-5]) based on its invariance with respect to unitary transformations among the active orbitals. Ruedenberg and collaborators (see e.g. Ref. [6]) advanced the idea that free atoms partially survive in molecules and came up with the quasi atomic orbitals (QUAO) in order to rationalize the bonding formation and chemical transformations in reactions.

Another path towards the visual consideration of the chemical bond is through the spin coupled generalized valence bond (SCGVB) wavefunction [7,8]. It can be considered as the best single configuration representation of a CASSCF [9] but it has less variational degrees of freedom [10] so it is energetically inferior to a CASSCF. It nevertheless has some attractive features. The SCGVB orbitals sort out quasi localized and this is in line with the established chemical concepts while their evolution along a reaction path may be helpful in detailing the molecular formation process through an atoms - in - molecule (AIM) perspective [11].

Within the same AIM spirit Nicolaides and Komninos [12,13] presented an interesting theory that connects the molecular structure with the shape of the (usually excited) atomic state that is responsible for the molecular formation. This geometrically active atomic state is nevertheless not provided. Its knowledge results out of experience and trials. When correctly identified both the molecular shape and the corresponding hybridization result naturally by inspection of the maxima of the probability density.

But how can one identify this 'correct' atomic state? We have previously addressed this issue by constructing the non adiabatic coupling matrix elements (NACME) and corresponding diabatic curves [14-16] in a number of cases. And we intend to act similarly for BeH $\left(X^{2} \Sigma^{+}\right), \mathrm{BeH}^{-}\left(X^{1} \Sigma^{+}\right), \mathrm{Be}_{2}\left(X^{1} \Sigma_{g}^{+}\right), \mathrm{O}_{3}\left(\tilde{X}^{1} \mathrm{~A}_{1}\right)$, and $\mathrm{CO}_{3}\left(\tilde{X}^{1} \mathrm{~A}_{1}\right)$ with the goal to unveil the role of the excited atomic and/or fragmentary states in the formation of their respective ground molecular states.

## 2. Computational details

We have studied the formation of the titled species both diabatically and adiabatically through state averaged

CASSCF (SACASSCF) and multi reference CI (MRCI) calculations coupled with the (aug) - cc - pVQZ basis set. The technical details of the SACASSCF wavefunctions are as follow: SACASSCF ( $3 \mathrm{e}^{-} / 23$ orb, 16 states) for $\operatorname{BeH}\left(X^{2} \Sigma^{+}\right)$; SACASSCF ( $4 \mathrm{e}^{-} / 23$ orb, 16 states) for $\mathrm{BeH}^{-}\left(X^{1} \Sigma^{+}\right)$; SACASSCF ( $4 \mathrm{e}^{-} / 26$ orb, 6 states) for $\mathrm{Be}_{2}\left(X^{1} \Sigma_{g}^{+}\right)$; SACASSCF ( $18 \mathrm{e}^{-} / 12$ orb, 6 states) for $\mathrm{O}_{3}\left(\tilde{X}^{1} \mathrm{~A}_{1}\right)$; and SACASSCF ( $16 \mathrm{e}^{-} / 13$ orb, 16 states) for $\mathrm{CO}_{3}\left(\tilde{X}^{1} \mathrm{~A}_{1}\right)$. The size of the active spaces and the number of states included in the SACASSCF calculations resulted after a number of trials. Diabatic curves have been constructed by rotating the adiabatic ones while the associated NACMEs have been computed by finite differences with a step of $0.01 \AA$ along the chosen reaction path.

Diabatic curves have the property to retain the electronic characteristics of the asymptotic channel along the reaction path $\left(\left\langle\psi_{i}^{\text {diabatic }}\right| d / d Q_{\kappa}\left|\psi_{j}^{\text {diabatic }}\right\rangle=0\right)$ and consequently they are useful when an analysis of the chemical bond is in order. When two or more potential energy curves interact strongly, become degenerate or quasi degenerate the NACMEs acquire substantial values. The Born - Huang expansion [17] introduces the above couplings that arise from the nuclear kinetic energy operator acting on the electronic wavefunctions and contain 1 st and $2^{\text {nd }}$ order differential operators. This way the non adiabatic behavior is recovered but the singularities of the non adiabatic couplings create computational problems that are handled by transforming to a diabatic basis (see e.g. Refs. [18,19]) where the kinetic coupling is either minimized or completely eliminated. The transformation from an adiabatic to a diabatic basis is unitary and depends parametrically on $\left\langle\left.\psi_{i}^{\text {adiabatic }}\right|^{d} / d Q_{\kappa} \mid \psi_{j}^{\text {adiabatic }}\right\rangle$; see e.g. [20].

The MOLPRO computational package [21] has been employed throughout our work.

## 3. Results (past and present) and discussion

In what follows we shall present a critical survey of the existing literature related to the bonding description of the studied species. The most recent studies on BeH and $\mathrm{BeH}^{-}$are documented in Refs. [22-24] and [25-27], respectively, while both the neutral and anion species are discussed in Ref. [28]. Their bonding is only discussed in Refs. [22], [25], [27], and [28] and in the following we shall focus on their most important points.

In Ref. [22] we read.
' $\ldots$. At short distances, let us say up to $3 \AA$, both MOs can be described as resulting from the bonding and non bonding $\left(2 s_{\mathrm{Be}}-2 p_{\mathrm{Be}}\right)$ hybrid $+\left(1 s_{\mathrm{H}}\right) . '$
and
' ... The bond formation of BeH , both in the ground state (GS) and excited states, deserve special interest, as many other compounds of Be do, due to the relevance of the promotion from the $2 s$ to the $2 p$ orbital in the formation of the molecule.'.

The $\mathrm{BeH}^{-}$anion is studied in Ref. [25] but a discussion on its parental neutral species is also given. The authors state that
' ... it is well known that the Be atom is able to form two $s p$ hybrid orbitals ... placed in a linear arrangement at the opposite sides with respect to the Be atom ... due to the quasi degenerate nature of the $2 s$ and $2 p$ atomic orbitals... Indeed, the first excited triplet state $\left({ }^{3} \mathrm{P}\right)$ is only 2.725192 eV above the ground state, ...'.
One of the above described $s p$ hybrids combines with the $1 s$ hydrogen orbital to form the $\sigma \mathrm{BeH}$ bond while the other (opposite) $s p$ hybid hosts the second Be valence electron and the minus charge. This bonding mode is condensed in the Lewis structure $(: \mathrm{Be}-\mathrm{H})^{-}$and certainly this is in perfect agreement with the structure of the isoelectronic and linear $\mathrm{H}: \mathrm{Be}-\mathrm{H}\left(\leftarrow \mathrm{H}^{+}+(: \mathrm{Be}-\mathrm{H})^{-}\right)$ system. All of the above ideas have been confirmed by carefully constructing FCI calculations. They have finally concluded that the bond formation is the result of two combined effects, the quasi degeneracy of the $2 s$ and $2 p$ orbitals and the very weak electron affinity of H .

In Ref. [27] the authors offer a comparative study of $\mathrm{RG}-\mathrm{H}^{-}(\mathrm{RG}=\mathrm{He}-\mathrm{Rn})$ and $\mathrm{MH}^{-}(\mathrm{M}=\mathrm{Be}-\mathrm{Ra})$. Based on QCISD contour plots and on an AIM population analysis the authors concluded that the bonding situation results from the displacement of the $2 s^{2}$ Be density away from the incoming $\mathrm{H}^{-}$ion into an $s p$ hybrid and the partial donation of $\mathrm{H}^{-}$into a dative covalent manner while both atoms retain the majority of their electron density (i.e.: $\mathrm{Be} \leftarrow\left(\mathrm{H}^{-}\right)$).

In Ref. [28] both BeH and $\mathrm{BeH}^{-}$systems are discussed and the conclusions reached are in agreement with those in Ref. [25], i.e. the in situ Be atom is found in its excited ${ }^{3} \mathrm{P}$ state (stated explicitly), a covalent BeH bond is formed while the negative charge of $\mathrm{BeH}^{-}$is coupled with the spin defining $\mathrm{e}^{-}$of the neutral species in the $s p$ hybrid opposing the BeH bond.

Concerning BeH (both neutral and anion) we have constructed adiabatic and diabatic potential curves at the MRCI level that show the excited nature of the in situ Be atom. The MRCI potential energy curves of six BeH states of ${ }^{2} \Sigma^{+}$symmetry are displayed in Figure 1. The NACMEs of the $X^{2} \Sigma^{+}-2{ }^{2} \Sigma^{+}$interaction are shown in Figure 2 along with the corresponding adiabatic and diabatic potential curves (see inset). The latter show the diabatic chemical origin of the ground $X^{2} \Sigma^{+} \mathrm{BeH}$ minimum or in other words the excited in situ character ( $2 s^{1} 2 p^{1} ;{ }^{3} \mathrm{P}$ ) of the Be atom. We should mention at


Figure 1. $\mathrm{MRCl} / \mathrm{aug}-\mathrm{cc}-\mathrm{pVQZ}$ adiabatic potential energy curves of $\mathrm{BeH}\left({ }^{2} \Sigma^{+}\right)$.
this point that the $X^{2} \Sigma^{+}-2^{2} \Sigma^{+}$interaction/avoided crossing is mentioned in a SCGVB computationally study some forty years ago [29].

The formation of the anion appears to be straightforward. The additional electron is singlet coupled with the spin defining electron of the neutral species that resides in the $s p$ hybrid opposing the BeH bond. The equilibrium CASSCF configuration is

$$
\left|X^{1} \Sigma^{+}\left({ }^{1} A_{1}\right)_{\mathrm{C}_{2 v}}\right\rangle \cong 0.81\left|1 a_{1}^{2} 2 a_{1}^{2}\right\rangle-0.46\left|1 a_{1}^{2} 2 a_{1}^{1} 4 \bar{a}_{1}^{1}\right\rangle
$$

where $1 a_{1}\left(\sim 0.65[2 s]_{\mathrm{Be}}+0.64[1 s]_{\mathrm{H}}\right)$ describes the covalent sigma BeH bond while $2 a_{1}\left(\sim 0.7[2 s]_{\mathrm{Be}}-0.5\right.$ $\left.\left[2 p_{z}\right]_{\mathrm{Be}}-0.3[1 s]_{\mathrm{H}}\right)$ is a $s p$ hybrid pointing away from the sigma bond. The 0.46 configuration describes the same situation as the 0.81 one but in a SCGVB way (a different orbital for different electrons).

Figure 3 shows the diabatic origin of its $\left(\mathrm{BeH}^{-}\right)$equilibrium character. Its minimum relates adiabatically to the $\mathrm{Be}\left({ }^{1} \mathrm{~S}\right)+\mathrm{H}^{-}\left({ }^{1} \mathrm{~S}\right)$ asymptote. Diabatically their interaction is repulsive as expected due to their closed shell character. The diabatic attractive interactions result not


Figure 2. NACMEs of the $\mathrm{BeH} X^{2} \Sigma^{+}-2{ }^{2} \Sigma^{+}$interaction along with their adiabatic (black curves) and diabatic (red curves) potential energy curves (inset). Numerical results at the MRCI/aug - cc - pVQZ computational level. Diabatization is treated as a $2 \times 2$ problem.
only from the $\mathrm{Be}^{-}\left({ }^{2} \mathrm{P}_{\text {Ryd }}\right)+\mathrm{H}$ asymptote but also from higher Rydberg diabats (i.e. $\mathrm{Be}^{-}\left({ }^{2} \mathrm{~S}_{\mathrm{Ryd}}\right), \mathrm{Be}^{-}\left({ }^{2} \mathrm{P}_{\mathrm{Ryd}}\right)$; see Figure 3). The adiabatic curve, a 'mixture' of all these diabatic curves has an overall attractive character.

Although the ground Be state has a negative electron affinity this is not true for its first excited ${ }^{3} \mathrm{P}$ ( $2 s^{1} 2 p^{1}$ ) state. The following numerical MRCI results are quite indicative: $\Delta \mathrm{E}\left(2 s^{1} 2 p^{1}\right.$; ${ }^{3} \mathrm{P}$ ( Be$) \leftarrow 2 s^{2}$; ${ }^{1} \mathrm{~S}$ $(\mathrm{Be}))=63.08 \mathrm{kcal} / \mathrm{mol}$ but $\Delta \mathrm{E}\left(2 s^{2} p^{1} ;{ }^{2} \mathrm{P}_{\mathrm{Ryd}}\left(\mathrm{Be}^{-}\right)\right.$ $\leftarrow 2 s^{2}$; $\left.{ }^{1} \mathrm{~S}(\mathrm{Be})\right)=6.91 \mathrm{kcal} / \mathrm{mol}$. For higher Rydberg states we have $\Delta \mathrm{E}\left(2 s^{2} s^{1} ;{ }^{2} S_{\mathrm{Ryd}}\left(\mathrm{Be}^{-}\right) \leftarrow 2 s^{2} ;{ }^{1} \mathrm{~S}\right.$ $(\mathrm{Be}))=16.90 \mathrm{kcal} / \mathrm{mol}$ and $\Delta \mathrm{E}\left(2 \mathrm{~s}^{2} p^{\prime} ;{ }^{2} \mathrm{P}_{\mathrm{Ryd}}\left(\mathrm{Be}^{-}\right) \leftarrow\right.$ $\left.2 s^{2} ;{ }^{1} \mathrm{~S}(\mathrm{Be})\right)=25.27 \mathrm{kcal} / \mathrm{mol}$. Thus $\mathrm{Be}^{-}\left(2 s^{2} p^{1} ;{ }^{2} \mathrm{P}_{\mathrm{Ryd}}\right)$ is stabilized upon interaction with H and 'lives' inside $\mathrm{BeH}^{-}\left(X^{1} \Sigma^{+}\right)$notwithstanding its unbound (with respect to $\mathrm{Be}\left({ }^{1} \mathrm{~S}\right)$ ) atomic nature.

The last Be containing species to be presently examined is the homonuclear diatomic $\mathrm{Be}_{2}\left(X^{1} \Sigma_{g}^{+}\right)$. An extensive bibliographic survey up to 2016 is critically exposed in Ref. [28] and it will not be repeated here.


Figure 3. Adiabatic (black curves) and diabatic (red curves) potential energy curves for the $\mathrm{BeH}^{-}$states of ${ }^{1} \Sigma^{+}$symmetry at the SACASSCF/aug - cc - pVQZ level of theory. Diabatization is treated as a $4 \times 4$ problem.

The conclusion reached is that its ground $X^{1} \Sigma_{g}^{+}$state results from the interaction of two excited ${ }^{3} \mathrm{P}$ states bound together with two nominally sigma bonds.

A recent SCGVB study [30] on $\mathrm{Be}_{2}$ concludes that there is a pair of singlet coupled electrons hosted by a set of highly overlapping ( $\mathrm{S}=0.83$ ) 'inner' orbitals that constitute a traditional sigma bond and an 'outer' pair of singlet coupled electrons in a set of weakly overlapping orbitals ( $\mathrm{S}=0.27$ ) thus having a significant diradical character. It is assumed that the two Be atoms are in situ in their ground ${ }^{1}$ S state and the binding results as a reorganization of the spin couplings of the four valence electrons. Due to an overlap between the 'inner' and 'outer' orbitals ( $\mathrm{S}=0.17$ and 0.34 ) there is a considerable Pauli repulsion that destabilizes the system by $\sim$ $60 \mathrm{kcal} / \mathrm{mol}$. The same Pauli repulsion is also found as the predominant destabilizing factor in an EDA - NOCV analysis at the BP86/TZ2P computational level [31].

We have constructed both diabatic and adiabatic curves; see Figure 4. Two ground state Be atoms interact


Figure 4. $\mathrm{MRCl} / \mathrm{aug}-\mathrm{cc}-\mathrm{pVQZ}$ adiabatic (black curves) and diabatic (red curves) potential energy curves of $\mathrm{Be}_{2}\left({ }^{1} \Sigma_{g}^{+}\right)$dissociating to $\mathrm{Be}\left({ }^{1} \mathrm{~S}\right)+\mathrm{Be}\left({ }^{1} \mathrm{~S}\right)$ and $\mathrm{Be}\left({ }^{3} \mathrm{P}\right)+\mathrm{Be}\left({ }^{3} \mathrm{P}\right)$. Several $\mathrm{Be}_{2}$ states of ${ }^{1} \Sigma_{g}^{+}$symmetry at the SACASSCF level appear in the inset. Diabatization is treated as a $5 \times 5$ problem.
purely repulsively due to their closed shell character but two excited ${ }^{3} \mathrm{P}\left(2 s^{1} 2 p^{1}\right)$ states interfere constructively. Our present findings are in complete harmony with the conclusions reached in Ref. [28], i.e. the shallow minimum of the ground beryllium dimer is due to two excited ${ }^{3} \mathrm{PBe}$ atoms.

The $\mathrm{O}_{3}$ species, a diamagnetic molecule, is believed to feature a partial diradical character (30\% [32], 24\% [33], $20 \%$ [34], and $23 \%$ [35]) while it is believed to be formed by the association of three $\mathrm{O}\left({ }^{3} \mathrm{P}\right)$ atoms. Two singlet coupled electrons are thought to reside primarily on the terminal oxygen atoms [36]. This chemical interpretation was recently challenged. It was proposed instead that ground state $\mathrm{O}_{3}$ is a genuine closed shell singlet species formed when two excited fragments are held together by a dative bond: $\mathrm{O}_{2}\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right) \rightarrow: \mathrm{O}=\mathrm{O}: \rightarrow$ $\mathrm{O}:(\leftrightarrow: \mathrm{O} \leftarrow: \mathrm{O}=\mathrm{O}:$ ) [37]. This conclusion triggered a number of interpretational studies. A QUAOS analysis [38] reported a $\sim 44 \%$ of diradical character while the most recent numbers are $19 \%$ [39] and $18 \%$ [40]. In the latter study the authors concluded that the ground state
originates from $\mathrm{O}_{2}\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)$ as first proposed in Ref. [37]

A recent SCGVB study [41] concluded on its almost complete diradical character based on the low overlap ( $\mathrm{S}=0.16$ ) of the terminal orbitals as found in previous SCGVB calculations [33,34,36]. As it [41] was tailored only for the $\mathrm{O}_{2}\left(X^{3} \Sigma_{\mathrm{g}}{ }^{-}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)$ interaction it could not consider the mixing with $\mathrm{O}_{2}\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)[42,43]$ and the ensuing dative bond.

In (the inset of) Figure 5 we display the diabatic and adiabatic potential curves of all ${ }^{1} \mathrm{~A}^{\prime}$ states resulting from the asymmetric combination $\mathrm{O}_{2}\left(X^{3} \Sigma_{\mathrm{g}}{ }^{-}\right)+\mathrm{O}$ $\left({ }^{3} \mathrm{P}\right)$ and $\mathrm{O}_{2}\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)$. The repulsive character of the lowest adiabatic potential curve ( $\leftarrow \mathrm{O}_{2}(X$ $\left.\left.{ }^{3} \Sigma_{\mathrm{g}}{ }^{-}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)\right)$ up to $1.8 \AA$ is pretty obvious but beyond this point it plummets due to the interaction with the $3{ }^{1} \mathrm{~A}^{\prime}$ state issued from $\mathrm{O}_{2}\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)$. The diabatic curves show the purely repulsive interaction of $\mathrm{O}_{2}$


Figure 5. NACMEs of the 1 st and 3 rd ${ }^{1} \mathrm{~A}^{\prime}$ adiabatic states of $\mathrm{O}_{3}$ along the asymmetric dissociation to their asymptotic products $\mathrm{O}_{2}\left(X^{3} \Sigma_{\mathrm{g}}{ }^{-}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)$ and $\mathrm{O}_{2}\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)$, respectively. Adiabatic (black curves) and diabatic (red curves) potential energy curves are shown in the inset. Numerical results at the MRCI/aug - cc - pVQZ computational level. Diabatization is treated as a $5 \times 5$ problem.
$\left(X^{3} \Sigma_{\mathrm{g}}{ }^{-}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)$ and the purely attractive interaction of $\mathrm{O}_{2}\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)$. Finally, the evolution of the NACMEs is in complete agreement with the form of the adiabatic/diabatic curves. Our present results show that the formation of ground $\mathrm{O}_{3}$ results from the $\mathrm{O}_{2}$ $\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)$ interaction $[37,42]$.

By symmetrically dissociating $\mathrm{O}_{3}$ to three O atoms we get mutatis mutandis an identical picture for the bonding character. The $\mathrm{O}\left({ }^{3} \mathrm{P}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)$ interaction is initially repulsive for all states, see Figure 6. For the ground potential profile and for bond distances less than $\sim 4$ bohr the interaction becomes attractive due to the intervening states correlating to $\mathrm{O}\left({ }^{3} \mathrm{P}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)+\mathrm{O}$ $\left({ }^{1} \mathrm{D}\right)$. Its potential barrier (see inset of Figure 6) is similar to the one displayed in the ground potential profile of the $\mathrm{O}_{2}\left(X^{3} \Sigma_{\mathrm{g}}{ }^{-}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)$ interaction (see Figure 5). Both reaction paths, $\mathrm{O}+\mathrm{O}+\mathrm{O}$ and $\mathrm{O}_{2}+\mathrm{O}$ offer a complementary (and identical) analysis of the bond formation. In the $\mathrm{O}_{2}+\mathrm{O}$ case the diabatic origin is the excited $\mathrm{O}_{2}\left(a^{1} \Delta_{\mathrm{g}}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)$ channel that correlates to O $\left({ }^{3} \mathrm{P}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)+\mathrm{O}\left({ }^{1} \mathrm{D}\right)$, that is the diabatic origin of the $\mathrm{O}+\mathrm{O}+\mathrm{O}$ combination.


Figure 6. Potential energy profiles of the symmetric dissociation $\mathrm{O}_{3}\left({ }^{1} \mathrm{~A}^{\prime}\right) \rightarrow 30$ at the SACASSCF/cc - pVQZ computational level.

The last molecular species to be presently examined is the ground state of the atmospherically important $\mathrm{CO}_{3}$; see e.g. Ref. [44]. It is considered as an important reaction intermediate for the quenching of electronically excited $\mathrm{O}\left({ }^{1} \mathrm{D}\right)$ atoms in the atmospheres of Earth and Mars and it also contributes to the anomalous ${ }^{13} \mathrm{O}$ isotope enrichment. It was first postulated in 1962 by Katakis and Taube [45] as an unstable kinetic intermediate in the exchange of oxygen between $\mathrm{CO}_{2}$ and $\mathrm{O}\left({ }^{1} \mathrm{D}\right)$ and isolated and characterized by Moll et al., [46] in 1966 and by Weissberger et al., [47] in 1967. Since then it has been the subject of numerous experimental and theoretical studies; see e.g. Refs. [48-64], while an historical overview is given in Refs. [60], [61], and [65]. The theoretical studies [48,49,51-55,59-64] were focused primarily on its energetic and geometrical features while some [59,61,63,64] also considered the vibronic effects through a Jahn - Teller and pseudo Jahn - Teller formalism. All computational studies agree on a singlet $\mathrm{C}_{2 v}$ global minimum with a $\mathrm{D}_{3 h}$ local minimum at $3.03 \mathrm{kcal} / \mathrm{mol}$ (CCSDT/aug - cc - pVQZ) [56], 6.45 $\mathrm{kcal} / \mathrm{mol}(\mathrm{CCSD}(\mathrm{TQ}) / \mathrm{cc}-\mathrm{pVTZ})$ [61], and $5.5 \mathrm{kcal} / \mathrm{mol}$ (CCSD $(\mathrm{T}) /$ aug $-\mathrm{cc}-\mathrm{pVTZ})$ [63] higher.

In this work we will focus on the bonding features of the (global) $\mathrm{C}_{2 v}$ minimum by detailing the adiabatic transformations $\mathrm{CO}+\mathrm{O}_{2} \leftarrow \mathrm{CO}_{3} \rightarrow \mathrm{CO}+2 \mathrm{O}$. Also of interest is the bonding analysis of the related $\mathrm{H}_{2} \mathrm{CO}_{3}$ $\left((\mathrm{HO})_{2} \mathrm{CO}\right)$ molecular species. As previously found [15] its minimum results from the interaction of $\mathrm{C}(\mathrm{OH})_{2}$ $\left(\tilde{a}^{3} \mathrm{~B}_{1}\right)+\mathrm{O}\left({ }^{3} \mathrm{P}\right)$ or $\mathrm{CO}\left(a^{3} \Pi\right)+2 \mathrm{OH}\left(X^{2} \Pi\right)$. By removing the hydrogen atoms of the two OH groups a singlet $\mathrm{CO}_{3}\left(\Delta \mathrm{E}\left(\tilde{a}^{3} \mathrm{E}^{\prime \prime} \leftarrow \tilde{X}^{1} \mathrm{~A}_{1}\right)=25.63 \mathrm{kcal} / \mathrm{mol}\right)$ species arises with a cyclic $\mathrm{C}_{2 v}$ structure where the OCO angle drops from $108.63^{\circ}\left(\mathrm{H}_{2} \mathrm{CO}_{3}\right)$ [15] to $75.25{ }^{\circ}\left(\mathrm{CO}_{3}\right)$, apparently due to the formation of a loose chemical bond between the two terminal O atoms (but see below).

Let us first consider the $\mathrm{CO}+\mathrm{O}_{2}$ dissociation path (Figure 7). We adiabatically dissociate the species by retaining the CO and $\mathrm{O}_{2}$ distances at the $\mathrm{CO}_{3}$ equilibrium values $\left(\mathrm{O}_{(\text {axial })} \mathrm{CO}_{2} ; \mathrm{CO}_{(\text {axial })}=1.169 \AA\right.$, $\left.\mathrm{CO}_{(\text {terminal })}=1.325 \AA, \mathrm{O}_{(\text {term })} \mathrm{CO}_{(\text {term })}=75.25^{\circ}\right)$. The (adiabatic) ground exit channel is $\mathrm{CO}\left(X^{1} \Sigma^{+}\right)+\mathrm{O}_{2}$ $\left(a^{1} \Delta_{g}\right)$ that gives rise to an initial repulsive interaction until around 3.5 bohr. Two closed shell singlet CO and $\mathrm{O}_{2}$ moieties cannot form any bonds and they repel each other but beyond the maximum of their repulsive interaction ( $\sim 3.5$ bohr) the triplet CO and $\mathrm{O}_{2}$ species enter into the chemical scene. The only possible candidate is $\mathrm{CO}\left(a^{3} \Pi\right)$ while the lowest triplet $\mathrm{O}_{2}$ candidate is $\mathrm{O}_{2}$ $\left(X^{3} \Sigma_{g}^{-}\right)$. There is thus a formation of two $\mathrm{C}-\mathrm{O}$ bonds between the four electrons of the two triplet coupled fragments ( $a^{3} \Pi+X^{3} \Sigma_{g}^{-}$). The global $\mathrm{C}_{2 v}$ minimum of $\mathrm{CO}_{3}$ is fully understood through this formation channel, i.e.


Figure 7. Potential energy profiles of the ground $\mathrm{CO}_{3}$ state along the $\mathrm{CO}+\mathrm{O}_{2}$ dissociation path at the SACASSCF/cc - pVQZ computational level. The geometry of the molecular fragments (CO and $\mathrm{O}_{2}$ ) is at the equilibrium structure of $\mathrm{CO}_{3}$ (see text for numerical values). The CO moiety approaches O - O vertically along an axis passing from its midpoint.
through the combination of an elongated singly bonded $\mathrm{O}_{2}$ species with two tripled coupled electrons that are ready to combine with the tripled coupled electrons of an excited CO $\left(a^{3} \Pi\right)$ fragment. In agreement with the above picture is the Mulliken atomic population of the $2 s^{0.90}$ orbital of carbon at its equilibrium geometry.

The $\mathrm{CO}+2 \mathrm{O}$ path confirms the excited in situ character of CO. The ground exit channel finds all of its constituents at their respective ground states, i.e, CO $\left(X^{1} \Sigma^{+}\right)$and $\mathrm{O}\left({ }^{3} \mathrm{P}\right)$ that initially have a repulsive interaction (see Figure 8). At around 4 bohr the ground potential energy curve presents an energy barrier but beyond this point its energy drops due to its interaction with a remote potential curve arising from $\mathrm{CO}\left(a^{3} \Pi\right)+2$ O $\left({ }^{3} \mathrm{P}\right)$. The evolution of the Mulliken populations of the C $2 s$ orbital is indicative of the participation of the excited $a^{3} \Pi$ state in the formation process as it plummets from 1.80 (at infinity) to only 0.96 (at equilibrium). Both formation/dissociation paths $\left(\mathrm{CO}+2 \mathrm{O} \leftarrow \mathrm{CO}_{3}\right.$ $\rightarrow \mathrm{CO}+\mathrm{O}_{2}$ ) provide an insightful view of its bonding


Figure 8. Potential energy profiles of the ground $\mathrm{CO}_{3}$ state along the $\mathrm{CO}+20$ dissociation path at the SACASSCF/cc - pVQZ computational level.
status with the main characteristic being the $2 s^{1} 2 p^{3} \mathrm{C}$ configuration.

## 4. Conclusions

A discussion on the chemical bonding implies tacitly or explicitly that molecules are made out of atoms bound together when their valence electrons are arranged in such a way as to decrease their kinetic energy. Ground and excited states of the atomic entities may contribute as well to the formation of the ground molecular states. Within this work we have constructed diabatic curves and NACMEs that show the excited character of the fragments in some simple species like $\mathrm{BeH}\left(X^{2} \Sigma^{+}\right), \mathrm{BeH}^{-}$ $\left(X^{1} \Sigma^{+}\right), \mathrm{Be}_{2}\left(X^{1} \Sigma_{g}^{+}\right), \mathrm{O}_{3}\left(\tilde{X}^{1} \mathrm{~A}_{1}\right)$. In all Be containing diatomics the Be atom is in situ found in its excited ${ }^{3} \mathrm{P}$ $\left(2 s^{1} 2 p^{1}\right)$ state while in $\mathrm{O}_{3}$ both $\mathrm{O}_{2}$ and O are in situ found in their first excited $a^{1} \Delta_{\mathrm{g}}$ and ${ }^{1} \mathrm{D}$ states, respectively. Finally, in $\mathrm{CO}_{3}$ the carbon atom uses all its four valence electrons through an excited $2 s^{1} 2 p^{3}$ carbon electronic configuration.

## Disclosure statement

No potential conflict of interest was reported by the author(s).

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