Electronic structure determination of chromium boride cation, CrB⁺

Apostolos Kalemos and Aristides Mavridis^{a)}

Laboratory of Physical Chemistry, Department of Chemistry, National and Kapodistrian University of Athens, P.O. Box 64 004, 157 10 Zografou, Athens, Greece

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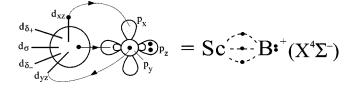
The CrB⁺ cation molecular system has been investigated with the help of semi-quantitative basis sets $[(7s6p4d3f)_{Cr}/(4s3p2d1f)_B]$ and highly correlated (valence) multi-reference wave functions. Out of a possible manifold of 70 states correlating to the Cr⁺(⁶S, ⁶D, ⁴D, ⁴G) + $B(^2P)$ atomic states, we have explored a total of 35 states spanning an energy range of about 3.4 eV. The ground state is of $X^7\Sigma^+$ symmetry with a binding energy of 28.8 kcal/mol at an internuclear distance of 2.242 Å. The next three excited states $1^5\Sigma^+$, $2^5\Pi$, and $3^7\Pi$ with energy splittings 7.1, 12.9, and 24.3 kcal/mol from the X state, have binding energies of 21.8, 16.5, and 5.1 kcal/mol, respectively. For practically all states we report potential energy curves, total energies, the most common spectroscopic parameters, while we discuss the binding modes using simple chemical diagrams based on valence-bond concepts. © 2000 American Institute of Physics. [S0021-9606(00)30630-4]

I. INTRODUCTION

With the present report on CrB^+ we conclude our tetralogy on the boride cationic systems MB^+ , M=Sc, Ti, V, and $Cr.^1$ As in our previous work in these systems we investigate by *ab initio* quantum mechanical methods, the electronic structure of the ground and of a series of low-lying excited states of the CrB^+ molecule. In particular, we focus our attention on the accurate determination of binding energies, and on interpreting the binding modes of the states studied by simple pictures based on a valence-bond conceptual approach.

All states examined correlate to the ground ²*P* state of the *B* atom, and to the ground ⁶*S*(3*d*⁵) and first three excited states ⁶*D*(4*s*3*d*⁴), ⁴*D*(4*s*3*d*⁴), ⁴*G*(3*d*⁵) of the Cr⁺ cation. The Wigner–Witmer rules dictate that the (adiabatic) interactions (⁶*S*, ⁶*D*, ⁴*D*, ⁴*G*)_{Cr}+ \otimes ²*P*_{*B*</sup> give rise to {^{5,7}Σ⁺, ^{5,7}Π}, {^{5,7}Σ⁺(2), ^{5,7}Σ⁻, ^{5,7}Π(3), ^{5,7}Δ(2), ^{5,7}Φ}, {^{3,5}Σ⁺(2), ^{3,5}Σ⁻, ^{3,5}Π(3), ^{3,5}Δ(2), ^{3,5}Φ}, {^{3,5}Σ⁺(2), ^{3,5}Σ⁻, ^{3,5}Π(3), ^{3,5}Δ(3), ^{3,5}Φ(3), ^{3,5}Γ(2), ^{3,5}*H*} molecular states spanning an energy range of about 4 eV. Out of the above 70 molecular states we have examined a total of 35, i.e., all of the first (4) and of the second (18) group, all of the triplets (9) of the third group and 4 states (³Σ⁻, ³Φ, ³Γ, ³Δ) of the last group. Due to the rather large ⁶*D*←⁶*S* Cr⁺ energy splitting (1.522 eV),² only the first four states (*X*⁷Σ⁺, 1⁵Σ⁺, 2⁵Π, 3⁷Π) are bound with respect to the ground state atoms (*vide infra*).}

It is of interest to recall at this point that the ground states of ScB⁺, TiB⁺, and VB⁺ are of high spin symmetry, namely $X^{4}\Sigma^{-}$, $X^{5}\Delta$, and $X^{6}\Sigma^{+}$, with D_{e} 's and R_{e} 's of 44.9, 47.6, 42.7 kcal/mol and 2.160, 2.102, and 2.061 Å, respectively,¹ implying similar binding schemes. Indeed, the bonding of the five valence electron ScB⁺ system in its ground state is succinctly represented by the following valence-bond Lewis (vbL) icon,^{1(a)}



suggesting three half bonds: one σ and two π . The ground states of TiB⁺ and VB⁺ are obtained by adding one electron in the $d_{\delta_{-}}$ (or $d_{\delta_{+}}$) orbital ($X^{5}\Delta$), and a second one in the $d_{\delta_{+}}$ (or $d_{\delta_{-}}$) orbital ($X^{6}\Sigma^{+}$), high spin coupled with the rest $\sigma^{1}\pi_{x}^{1}\pi_{y}^{1}$ electrons. The two $d_{\delta_{\pm}}$ electrons do not participate in the bonding process being completely localized on the metal, something that is rather obvious judging from the similarities of D_{e} 's and R_{e} 's of the three diatomics ScB⁺, TiB⁺, and VB⁺. Similarly, the ground CrB⁺ state is obtained by grafting an additional electron on the d_{σ} orbital, high spin coupled to the $\sigma^{1}\pi_{x}^{1}\pi_{y}^{1}\delta_{+}^{1}\delta_{-}^{1}$ electron distribution, thus resulting in a $X^{7}\Sigma^{+}$ state (*vide infra*).

For all 35 states examined in the present work we report potential energy curves (PEC), total energies (E), binding energies (D_e), spectroscopic parameters, and charge distributions. In Sec. II we outline some technical details, while in Sec. III we touch upon results on the atomic fragments; results and final conclusions are presented in Secs. IV and V.

II. METHODS

The same basis set was used as in our previous work.¹ For the Cr atom the ANO basis set 20s15p10d6f4g of Bauschlicher³ was used, but without the *g* functions, generally contracted to 7s6p4d3f. The triple- ζ correlation consistent basis, cc-pVTZ, 10s5p2d1f of Dunning⁴ was employed for the B atom, similarly contracted to 4s3p2d1f. The resulting one-electron orbital space contains 96 spherical Gaussian functions.

^{a)}Electronic mail: amav@arnold.chem.uoa.gr

Considering the Cr⁺ $1s^22s^22p^63s^23p^6$ and the $B 1s^2$ electrons as the "core," we are confronted with a 8 "valence'' (active) electron problem. This $8 e^-$ system generates ${}^{2S+1}|\Lambda|$ states with multiplicities 1, 3, 5, 7, and 9. Disregarding the singlet states which correlate to higher excited states of Cr⁺ than the ones' considered here, and the nonet states which correlate to the first excited ${}^{4}P$ state of the B atom, all other multiplicities have been examined. Now with the exception of the septets which, in principle, can be described by a Hartree-Fock wave function, all other states require a multi-reference approach. Moving along the same line as in our previous work,¹ a Complete Active Space SCF (CASSCF) approach was adopted followed by (valence) singles and doubles configuration interaction within the philosophy of the internal contraction.⁵ We believe that this multi-reference configuration interaction (MRCI) methodology is the only general method for describing complicated bonded systems,^{6,7} particularly if one wishes to construct potential energy curves. We remind that the MRCI method is variational, size consistent and practically size extensive^{8,9} for a relatively small number of active electrons.

Our reference space is composed of 10 orbital functions, related asymptotically to the valence occupied spaces of $Cr^+ (4s+3d)$ and B(2s+2p) atoms. The number of configuration functions (CF) ensuing from distributing eight electrons among a 10 orbital function space ranges from $268(^7\Sigma^-)$ to $5200(^3\Pi)$, according to the symmetry of the state. Our largest MRCI expansion of 15 623 942 CFs is reduced to 815 020 CFs through the internal contraction technique.⁵ No significant hazard is caused by the internal contraction strategy; as we are taught from our previous experience^{1(b)} total energy losses are of the order of 1 mhartree.

Notwithstanding the $C_{2\nu}$ symmetry constraints imposed on our computations, the CASSCF wave functions display symmetry and equivalency restrictions. Except otherwise stated all states have been calculated using the state-average technique.¹⁰ Judging as adequate the size of the one particle function space no corrections for basis set superposition errors were applied.

All calculations were done with the MOLPRO 96.4 suite of codes. 11

III. THE Cr⁺ AND B FRAGMENTS

In Table I we report total energies of the $\operatorname{Cr}^{+6}S(3d^5)$, ${}^{6}D(4s3d^4)$, ${}^{4}D(4s3d^4)$, ${}^{4}G(3d^5)$, and of the B atom ${}^{2}P(2s^22p)$ and ${}^{4}P(2s2p^2)$ spectroscopic terms in different methodologies, as well as corresponding energy splittings. For reasons of completeness calculations on the $\operatorname{Cr}^{7}S(4s3d^5)$, ${}^{5}S(4s3d^5)$, and ${}^{5}D(4s^23d^4)$ states are also reported along with their energy gaps. With the exception of the $\operatorname{Cr}^{+4}G \leftarrow {}^{4}D$ energy splitting the rest of the energy gaps are in fair harmony with the experimental values.²

IV. RESULTS AND DISCUSSION

In the following discussion we examine the 35 computed states in ascending energy order and according to their asymptotic products. Figure 1 presents full potential energy curves (PEC) of all states examined and Fig. 2 the corresponding energy level diagram. The ground state is marked with X while the rest of the states have been tagged with numbers in accord with their energy position, i.e., "1" for the first, "34" for the highest state, 77 kcal/mol above the X-state. Table II summarizes our numerical findings, namely, absolute energies (E), bond lengths (R_e), dissociation energies (D_e), harmonic frequencies (ω_e), and energy gaps (T_e) of the 35 examined states at the CASSCF, MRCI, and MRCI+Q (MRCI+multireference Davidson correction for unlinked clusters¹⁴).

A. The $X^7\Sigma^+$, $1^5\Sigma^+$, $2^5\Pi$, and $3^7\Pi$ states

The PECs (at the MRCI level) of the titled states are shown in Fig. 3 correlating to $Cr^+({}^{6}S) + B({}^{2}P)$.

1. *X* ⁷Σ⁺

As was already mentioned in the Introduction, the ground state of the CrB⁺ molecule is obtained by distributing three electrons to the remaining *d*-like holes of the ScB⁺ ($X^{4}\Sigma^{-}$) system, all of them high spin coupled. Due to the maximal spin this state is adequately described within the Hartree–Fock ansatz. Indeed, the leading CAS equilibrium configuration (HF) is

$$|X^{7}\Sigma^{+}\rangle \sim 0.97 |1\sigma^{2}2\sigma^{1}3\sigma^{1}1\delta^{1}_{+}1\pi^{1}_{x}1\pi^{1}_{y}1\delta^{1}_{-}\rangle,$$

with the 1σ being practically the 2s boron atomic orbital. At infinity the $X^7\Sigma^+$ state is described by the product wave function $|Cr^+(3d^5), {}^6S\rangle \otimes |B(2s^22p), {}^2P; M=0\rangle$.

To investigate the consistency of our calculations different approaches were tried for the titled four states, ranging from (single reference) CISD to MRCI including the "core" $3s^23p^6$ Cr⁺ e^- (c-MRCI), and increasing also the basis set of boron from triple- to quadruple- ζ . The results are similar for all four states; a representative sample of these calculations is given in Table III for the $X^7\Sigma^+$ state. We conclude that the 10 active orbital space (8/10) is necessary even for these states where the 4s function of Cr⁺ is not required asymptotically, the resulting gain in D_e being 1.8 kcal/mol. Going from MRCI to c-MRCI the binding is increased by another 1.3 kcal/mol, despite the fact that the ANO-Cr basis set used is not tuned for the $3s^2 3p^6 e^-$ to be included in the CI treatment.³ However, we choose not to pursue this point any further due to the disproportional increase of the calculation (92265 CFs at the MRCI vs 3849489 CFs at the c-MRCI for the $X^7\Sigma^+$ state). Finally, the gain in D_e is rather insignificant, 0.3 kcal/mol by increasing the boron basis from triple- to quadruple- ζ .

An observation is needed at this point for the state average (sa-MRCI) D_e number: the 2.5 kcal/mol D_e difference between the sa-MRCI and MRCI (Table III), is an artifact due to the inappropriateness of the sa-orbitals at infinity as evidenced by the size extensivity error, 7.6 mhartree at the sa-MRCI level. This is not observed to the rest 31 molecular states correlating to the excited Cr⁺ atomic states. The foregoing discussion justifies our basis set active space (8/10) and MRCI choices.

Now at equilibrium the atomic CASSCF Mulliken populations are (Cr/B)

TABLE I. Total energies (hartree) of the Cr⁷S(4s3d⁵), ${}^{5}S(4s3d^5)$, and ${}^{5}D(4s^23d^4)$ states, of the Cr⁺ ${}^{6}S(3d^5)$, ${}^{6}D(4s3d^4)$, ${}^{4}D(4s3d^4)$, and ${}^{4}G(3d^5)$ states, of the B ${}^{2}P(2s^22p)$ and ${}^{4}P(2s2p^2)$ states, and corresponding energy splittings (eV) in different methodologies.

	Cr							
Method	⁷ S	⁵ S	⁵ D		${}^{5}D \leftarrow {}^{5}S$			
NHF ^a	-1043.356 38		-1043.309 82					
SA-SCF ^b	-1043.355 90	-1043.316 61	-1043.309 39	1.069	0.197			
CISD(6e ⁻)	$-1043.455\ 60$	$-1043.420\ 80$	-1043.411 23	0.947	0.260			
$CISD(14e^{-})^{c}$	-1043.74295	-1043.703 19	-1043.693 85	1.082	0.254			
SA-CASSCF ^b			-1043.34277					
MRCI(6e ⁻)			-1043.41703		0.103			
Expt. ^d				0.941	0.062			
	Cr ⁺							
Method	⁶ S	⁶ D	^{4}D		${}^{4}G$			
NHF ^e	-1043.139 39							
SA-SCF ^b	-1043.138 83	-1043.09649	-1043.056 01		-1043.018 90			
$CISD(5e^{-})$	-1043.220 89	-1043.157 42	-1043.124 28		-1043.111 52			
CISD(13e ⁻) ^c	-1043.50648	-1043.45022	-1043.411 99		-			
	Cr ⁺ energy splittings							
Method	$^{6}D \leftarrow ^{6}S$		$^4D \leftarrow ^6D$		${}^{4}G {\leftarrow} {}^{4}D$			
SA-SCF ^b	1.152		1.102		1.010			
CISD	1.727		0.902		0.347			
CISD ^c	1.531		1.040		-			
Expt. ^d	1.522		0.936	0.085				
			В					
Method	^{2}P		^{4}P		${}^{4}P \leftarrow {}^{2}P$			
NHF ^a	-24.52	9 06						
SCF	-24.52	28 15	-24.451 29		2.091			
CISD	-24.59	6 63	-24.467 24		3.521			
SA-SCF ^b	-24.52	28 10	-24.44931		2.144			
CISD	-24.59	6 55	-24.467 21					
SA-CASSCF ^b	-24.55	9 33						
MRCI	-24.59	98 40			3.570			
Expt. ^d					3.571			

^aNumerical Hartree-Fock, Ref. 12.

^bSpherically averaged SCF or CASSCF.

"The $3s^2 3p^6$ "core" electrons have been added in the CI treatment.

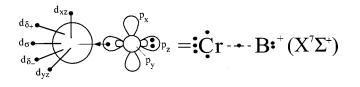
^dExperimental values, Ref. 2.

^eReference 13.

$$4s^{0.36}4p_z^{0.10}3d_{z^2}^{0.95}3d_{xz}^{0.95}3d_{yz}^{0.95}3d_{x^2-y^2}^{1.0}3d_{xy}^{1.0} /$$

 $2s^{1.73}2p_z^{0.79}2p_x^{0.08}2p_y^{0.08}$

suggesting the following valence-bond Lewis (vbL) bonding picture:



The diagram indicates that the two atoms are held by a half σ -bond, with five nonparticipating, strictly localized on the metal (observer), electrons; about $0.3 e^-$ are transferred from B to Cr⁺ via the σ -frame. The complete localization of the

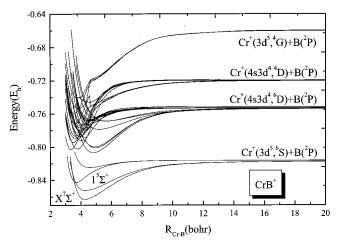


FIG. 1. Potential energy curves of the CrB^+ molecule of all 35 states studied at the MRCI level of theory.

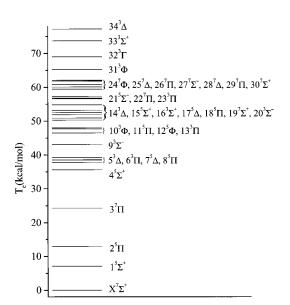


FIG. 2. Relative energy splittings (T_e) of all computed states at the MRCI level.

 d_{π} electrons as compared to the ScB⁺, TiB⁺, and VB⁺ species,¹ can be rationalized by realizing that the ionization potential (I.P.) of the Cr⁺ cation is 3.6, 2.9, and 2.3 eV higher than the I.P. of Sc⁺, Ti⁺, and V⁺, respectively.² As a result the D_e of CrB⁺ is abruptly reduced to 29 kcal/mol (MRCI) from a mean value of 45 kcal/mol in the earlier borides,¹ with a concomitant bond length increase ranging from 0.08 (ScB⁺) to 0.14 (TiB⁺) to 0.18 (VB⁺)Å.

2. 1⁵Σ⁺

By a single spin flipping of the $X^7\Sigma^+$ the $1^{5}\Sigma^+$ state obtains. Conceptually, we can think that the B atom approaches from infinity to the Cr⁺ ${}^{6}S$ ($M_s = +5/2$) state, with its p_{σ} spin in a β -like fashion. The bonding is captured by the same vbL icon given previously for the ground state, in agreement with the following dominant CASSCF equilibrium configurations and Mulliken population distributions:

$$\begin{split} |1 \,{}^{5}\Sigma^{+}\rangle &\sim -0.67 |1 \,\sigma^{2} 2 \,\sigma^{2} 1 \,\delta^{1}_{+} 1 \,\pi^{1}_{x} 1 \,\pi^{1}_{y} 1 \,\delta^{1}_{-}\rangle \\ &+ 0.43 |1 \,\sigma^{2} 1 \,\delta^{1}_{+} 3 \,\sigma^{2} 1 \,\pi^{1}_{x} 1 \,\pi^{1}_{y} 1 \,\delta^{1}_{-}\rangle \\ &+ 0.32 |1 \,\sigma^{2} 2 \,\sigma^{1} 1 \,\delta^{1}_{+} 3 \,\overline{\sigma}^{1} 1 \,\pi^{1}_{x} 1 \,\pi^{1}_{y} 1 \,\delta^{1}_{-}\rangle \\ &+ 0.31 |1 \,\sigma^{2} 2 \,\overline{\sigma}^{1} 1 \,\delta^{1}_{+} 3 \,\sigma^{1} 1 \,\pi^{1}_{x} 1 \,\pi^{1}_{y} 1 \,\delta^{1}_{-}\rangle , \\ 4s^{0.13} 4p^{0.09}_{z} 3 d^{1.03}_{z^{2}} 3 d^{0.97}_{xz} 3 d^{0.97}_{yz} 3 d^{1.0}_{x^{2}-y^{2}} 3 d^{1.0}_{xy} / \\ 2s^{1.72} 2p^{0.95}_{z} 2p^{0.06}_{x} 2p^{0.06}_{y} . \end{split}$$

From the B atom $0.2 e^-$ are transferred to the Cr⁺ atom via the σ -frame. At the equilibrium distance of 2.260 Å the binding energy is $D_e = 21.8 \text{ kcal/mol}$, 7.1 kcal/mol less than the binding energy of the $X^7 \Sigma^+$ state due to the spin flip.

*3. 2⁵П, 3⁷*П

The potential curves are shown in Fig. 3 with asymptotic wave functions whose symmetry is carried by the $p_{\pi}e^-$ of the B atom. The dominant equilibrium CASSCF (B_1 symmetry) configurations,

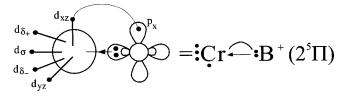
$$\begin{split} |2^{5}\Pi\rangle &\sim -0.79 |1\sigma^{2}1\delta_{+}^{1}2\sigma^{1}1\pi_{x}^{2}1\pi_{y}^{1}1\delta_{-}^{1}\rangle \\ &+ 0.24 |1\sigma^{2}1\delta_{+}^{1}2\sigma^{1}2\pi_{x}^{2}1\pi_{y}^{1}1\delta_{-}^{1}\rangle \\ &+ 0.50 |1\sigma^{2}1\delta_{+}^{1}2\sigma^{1}1\pi_{x}^{1}2\overline{\pi}_{x}^{1}1\pi_{y}^{1}1\delta_{-}^{1}\rangle, \end{split}$$

in conjunction with the Mulliken distribution,

$$4s^{0.17}4p_{z}^{0.11}3d_{z^{2}}^{0.88}3d_{xz}^{1.0}3d_{yz}^{1.0}3d_{x^{2}-y^{2}}^{1.0}3d_{xy}^{1.0}/$$

$$2s^{1.54}2p_{z}^{0.25}2p_{x}^{1.0}2p_{y}^{0.06},$$

imply the following bonding picture:



The two atoms are kept together by a π -bond and a dative σ -bond originating from the B atom; the character of the double bond is reflected to the rather short bond length, $R_e = 1.970$ Å at the MRCI level, despite the low D_e of 16.5 kcal/mol (Table II). Notice that no electrons are transferred through the π system, with 0.18 e^- migrating from B to Cr⁺ via the σ -frame.

In the next 3 $^{7}\Pi$ state, the six "parallel" electrons *a* priori preclude any real bonding, and indeed a D_{e} of 5.1 kcal/mol is computed at $R_{e}=2.435$ Å with a total charge transfer from B to Cr⁺ of a mere $0.1 e^{-}$.

B. In what follows next we discuss all molecular states stemming from $Cr^+(4s3d^4; {}^6D) + B({}^2P)$, i.e., $4\,{}^5\Sigma^+$, $7\,{}^5\Delta$, $8\,{}^5\Pi$, $11\,{}^5\Pi$, $12\,{}^5\Phi$, $15\,{}^5\Sigma^+$, $17\,{}^5\Delta$, $18\,{}^5\Pi$, $19\,{}^7\Sigma^+$, $21\,{}^5\Sigma^-$, $22\,{}^7\Pi$, $24\,{}^7\Phi$, $25\,{}^7\Delta$, $26\,{}^7\Pi$, $27\,{}^7\Sigma^-$, $28\,{}^7\Delta$, $29\,{}^7\Pi$, and $30\,{}^7\Sigma^+$

1. $4^{5}\Sigma^{+}$, $15^{5}\Sigma^{+}$

The PECs of both states are shown in Fig. 4 correlating to $Cr^+({}^6D; M=0,\pm 1)+B({}^2P; M=0,\mp 1)$. The leading CASSCF equilibrium configurations and corresponding Mulliken populations are

$$\begin{split} |4\,{}^{5}\Sigma^{+}\rangle &\sim 0.83 |1\,\sigma^{2}2\,\sigma^{2}1\,\delta^{1}_{+}1\,\pi^{1}_{x}1\,\pi^{1}_{y}1\,\delta^{1}_{-}\rangle, \\ |15\,{}^{5}\Sigma^{+}\rangle &\sim 0.53 |1\,\sigma^{2}2\,\sigma^{1}1\,\delta^{1}_{+}3\,\bar{\sigma}^{1}1\,\pi^{1}_{x}1\,\pi^{1}_{y}1\,\delta^{1}_{-}\rangle \\ &- 0.40 |1\,\sigma^{2}2\,\sigma^{1}1\,\delta^{1}_{+}3\,\sigma^{1}(1\,\pi^{1}_{x}1\,\bar{\pi}^{1}_{y}) \\ &+ 1\,\bar{\pi}^{1}_{x}1\,\pi^{1}_{y})1\,\delta^{1}_{-}\rangle \\ &+ 0.26 |1\,\sigma^{2}2\,\sigma^{1}1\,\delta^{1}_{+}3\,\sigma^{1}(1\,\pi^{1}_{x}2\,\bar{\pi}^{1}_{y}) \\ &+ 2\,\bar{\pi}^{1}_{x}1\,\pi^{1}_{y})1\,\delta^{1}_{-}\rangle, \\ 4\,{}^{5}\Sigma^{+}:4s^{1.06}4p^{0.07}_{z}3\,d^{0.10}_{z^{2}}3\,d^{1.0}_{xz}3\,d^{1.0}_{yz}3\,d^{1.0}_{x^{2}-y^{2}}3\,d^{1.0}_{xy}/ \\ &2s^{1.80}2p^{0.83}_{z}2p^{0.05}_{x}2p^{0.05}_{y}, \\ 15\,{}^{5}\Sigma^{+}:4s^{0.79}4p^{0.09}_{z}3\,d^{0.88}_{z^{2}}3\,d^{0.75}_{xz}3\,d^{1.0}_{yz}3\,d^{1.0}_{x^{2}-y^{2}}3\,d^{1.0}_{xy}/ \\ &2s^{1.60}2p^{0.59}_{z}2p^{0.26}_{x}2p^{0.26}_{y}. \end{split}$$

TABLE II. Total energies E (hartree), bond distances R_e (Å), dissociation energies D_e (kcal/mol), harmonic frequencies ω_e (cm⁻¹), and energy gaps T_e (kcal/mol) of the CrB⁺ states studied in ascending energy order.

State ^a	Method ^{b,c}	-E	R_{e}	D_e^{d}	ω_e	T_{e}	State ^a	Method ^{b,c}	-E	R_{e}	D_e^{d}	ω_e	T_{e}
MRCI	CASSCF	1067.740 67	2.606	18.8	257		18 ⁵ П	MRCI	1067.778 72	2.224	16.2	675	53.2
		1067.863 45	2.242	28.8	436	0.0		MRCI+Q	1067.7862	2.225	18.1	655	
	MRCI+Q	1067.870 5	2.229	30.6	462		$19^{7}\Sigma^{+}$	CASSCF	1067.664 61	3.124	8.4	125	
$1 {}^{5}\Sigma^{+}$ CASS	CASSCF	1067.73275	2.702	13.8	173			MRCI	1067.778 64	2.757	16.2	195	53.2
	MRCI	1067.852 16	2.260	21.8	239	7.1		MRCI+Q	1067.7857	2.734	17.7	199	
	MRCI+Q	1067.8591	2.242	23.5	248		$20^{3}\Sigma^{-}$	CASSCF	1067.641 96	2.048	54.6	788	
2 ⁵ П	CASSCF	1067.709 11	2.060	3.8	203			MRCI	1067.776 18	2.075	73.0	559	54.8
	MRCI	1067.842 84	1.970	16.5	494	12.9		MRCI+Q	1067.784 8	2.111	74.5	526	
	MRCI+Q	1067.850 5	1.970	18.1	507		$21 {}^{5}\Sigma^{-}$	MRCI	1067.773 21	2.203	12.3	434	56.6
3 ⁷ П	CASSCF	1067.705 82	2.893	1.8	115			MRCI+Q	1067.781 6	2.195	14.8	452	2010
	MRCI	1067.82473	2.435	5.1	182	24.3	$22^{7}\Pi(g)$	CASSCF	1067.661 52	3.075	6.8	161	
	MRCI+Q	1067.831 2	2.367	6.0	202		22 11(8)	MRCI	1067.772 97	2.381	13.0	352	56.8
$4 {}^5\Sigma^+$	CASSCF	1067.690 29	2.677	24.5	284			MRCI+Q	1067.781 0	2.359	15.0	374	50.0
. –	MRCI	1067.806 77	2.551	33.8	315	35.6	$22^{7}\Pi(l)$	MRCI	1067.768 78	2.993	10.4	164	
	MRCI+Q	1067.813 6	2.540	35.3	315	2210	22 11(1)	MRCI+Q	1067.775 0	2.979	11.2	176	
$5^{3}\Delta$	CASSCF	1067.668 19	1.779	33.6	747		23 ³ П	CASSCF	1067.633 05	1.920	11.2	637	
5 4	MRCI	1067.803 18	1.779	52.9	725	37.8	25 11	MRCI	1067.772 20	1.920	33.0	631	57.3
	MRCI+Q	1067.810 8	1.784	54.2	715	57.0		MRCI+Q	1067.781 2	1.911	35.1	620	57.5
6 ³ П	CASSCF	1067.669 39	2.041	34.6	499		$24^{7}\Phi$	CASSCF		2.770	1.2	120	
0 11	MRCI	1067.802 42	2.003	52.3	547	38.3	24Ψ	MRCI	1067.655 22	2.770	1.2 9.9	312	50.4
	MRCI+Q	1067.810 8	2.005	53.9	551	56.5			1067.768 72				59.4
7 $^5\Delta$	CASSCF	1067.694 51	2.000	21.3	256		257A(x)	MRCI+Q	1067.777 1	2.338	12.4	344	
$/\Delta$	MRCI	1067.801 75	2.733	21.3	285	38.7	$25 \ ^7\Delta(g)$	CASSCF	1067.666 91	3.234	6.6	120	50.5
		1067.807 6	2.595	29.5 30.6	285 288	38.7		MRCI	1067.768 69	3.015	9.5	156	59.5
$8^{5}\Pi(g)$	MRCI+Q						2574(1)	MRCI+Q	1067.773 9	2.974	10.1	137	
8 II(g)	CASSCF	1067.687.08	2.720	22.9	287	20.0	$25 \ ^7\Delta(l)$	MRCI	1067.768 34	2.440	9.3	277	
	MRCI	1067.801 00	2.623	30.6	297	39.2	a (711 ()	MRCI+Q	1067.7763	2.401	11.6	325	
0.511(1)	MRCI+Q	1067.807 8	2.616	31.8	307		$26 {}^{7}\Pi(g)$	MRCI	1067.767 67	2.393	9.3	302	60.1
$8 {}^{5}\Pi(l)$	MRCI	1067.792 14	2.126	25.0	445		7	MRCI+Q	1067.775 6	2.363	11.6	327	
o 311-	MRCI+Q	1067.8014	2.122	27.8	498		$26^{7}\Pi(l)$	CASSCF	1067.657 74	2.75	2.7		
$9^{3}\Sigma^{-}$	CASSCF	1067.654 05	1.869	24.3	777			MRCI	1067.766 79	2.75	8.8		
	MRCI	1067.794 79	1.864	47.3	675	43.1	7	MRCI+Q	1067.773 2	2.75	10.0		
2 -	MRCI+Q	1067.803 8	1.869	49.5	664		$27 \ ^7\Sigma^-$	CASSCF	1067.656 81	2.901	0.7	110	
$10^{3}\Phi$	CASSCF	1067.658 04	1.924	26.4	492			MRCI	1067.766 56	2.453	8.2	282	60.8
	MRCI	1067.789 38	1.923	43.6	501	46.5	_	MRCI+Q	1067.7743	2.418	10.2	313	
~	MRCI+Q	1067.797 0	1.936	44.9	488		$28 \ ^7\Delta$	CASSCF	1067.657 23	2.863	1.0	120	
$11 {}^{5}\Pi$	CASSCF	1067.6603	~ 2.3	4.4				MRCI	1067.764 92	2.710	7.1	340	61.8
	MRCI	1067.789 31	~ 2.3	22.9		46.5		MRCI+Q	1067.770 8	2.716	8.0	357	
	MRCI+Q	1067.7984	~ 2.3	25.9			29 ⁷ Π	CASSCF	1067.654 86	2.827	0.9	113	
$12 {}^{5}\Phi$	CASSCF	1067.658 29	2.129	3.1	383			MRCI	1067.764 60	2.65	7.3		62.0
	MRCI	1067.787 36	2.079	21.6	501	47.7		MRCI+Q	1067.771 2	2.65	8.7		
	MRCI+Q	1067.7957	2.085	24.1	501		$30^{7}\Sigma^{+}$	CASSCF	1067.645 97	2.977	0.6	122	
13 ³ П	CASSCF	1067.653 65	1.968	23.6	515			MRCI	1067.764 55	2.613	8.2	256	62.1
	MRCI	1067.786 89	1.931	42.1	560	48.0		MRCI+Q	1067.773 6	2.573	13.9	279	
	MRCI+Q	1067.794 9	1.934	43.6	547		$31 {}^{3}\Phi$	CASSCF	1067.618 97	1.877	40.2	691	
$14 \ {}^{3}\Delta$	CASSCF	1067.649 62	1.980	21.5	880			MRCI	1067.759 53	1.888	62.5	646	65.2
	MRCI	1067.783 36	1.985	39.9	792	50.3		MRCI+Q	1067.7693	1.898	64.8	624	
	MRCI+Q	1067.791 5	1.988	41.6	782		32 ³ Γ	CASSCF	1067.609 32	1.955	33.6	595	
15 $^5\Sigma^+$	CASSCF	1067.647 58	2.243	1.7	268			MRCI	1067.753 43	2.020	58.7	456	69.0
	MRCI	1067.782 34	2.163	19.4	456	50.9		MRCI+Q	1067.765 2	2.072	62.4	377	
	MRCI+Q	1067.7920	2.167	22.0	402		$33^{3}\Sigma^{+}$	CASSCF	1067.626 31	2.580	6.8	397	
$16^{3}\Sigma^{+}$	CASSCF	1067.646 61	2.131	19.0	463			MRCI	1067.745 96	2.423	16.5	355	73.7
	MRCI	1067.780 77	2.090	38.0	501	51.9	$34 {}^{3}\Delta$	CASSCF	1067.601 79	2.002	29.4	577	
	MRCI+Q	1067.789 7	2.096	40.3	511		J. A	MRCI	1067.740 39	1.986	50.5	474	77.2
$17 {}^5\Delta$	MRCI	1067.779 80	2.231	16.5	588	52.5		MRCI+Q	1067.750 8	1.976	53.2	561	, , .2
- /	MRCI+Q	1067.788 3	2.231	19.0	603	02.0		MILLER V	1007.750.0	1.770	55.4	501	

a'''g'' and ''l'' refer to global and local minima.

^bWith the exception of $X^7\Sigma^+$, $1^5\Sigma^+$, $2^5\Pi$, $3^7\Pi$, and $7^5\Delta$, all other states have been computed by the state average technique.

 $^{c}+Q$ refers to the multi-reference Davidson correction, Ref. 14.

^dDissociation energies with respect to the adiabatic fragments.

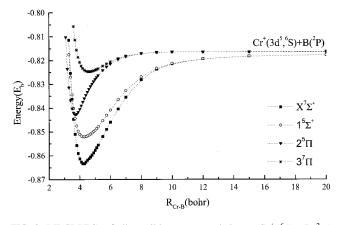
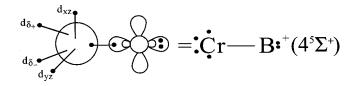
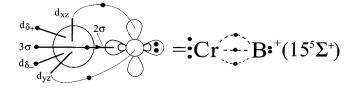


FIG. 3. MRCI PECs of all possible states correlating to $Cr^+({}^6S) + B({}^2P)$.

Clearly, for the $4 {}^{5}\Sigma^{+}$ state $4 e^{-}$ are completely localized to the d_{π} and d_{δ} orbitals; 0.15 and 0.10 e^{-} are transferred from the $2p_{z}$ and 2s functions of the B atom to a hybrid $(4s4p_{z}3d_{z}2)^{1.23}$ orbital of the Cr⁺ cation creating a σ -bond $(\sim 2\sigma^{2})$. The bonding is captured by the following vbL icon:



In the $15^{5}\Sigma^{+}$ state the bonding is comprised of two half π -bonds and one half σ -bond. In particular, from the distributions $4s^{1}3d_{z2}^{1}3d_{xz}^{0.50}3d_{yz}^{0.50}3d_{x^{2}-y^{2}}^{1.0}3d_{xy}^{1.0}$ (⁶*D*), and $2s^{1.89}2p_{z}^{0.05}2p_{x}^{0.53}2p_{y}^{0.53}$ (²*P*) of Cr⁺ and B at infinity, it is obvious that $0.5e^{-}$ are transferred from B to Cr⁺ through the π skeleton forming the two half π -bonds, while via the σ -frame a migration of $0.24e^{-}$ occurs from Cr⁺ to B resulting to two hybrid orbitals $(4s4p_{z}3d_{z}2)_{Cr^{+}}^{1.76}/(2s2p_{z})_{B}^{2.20}$ and the formation of a half σ -bond. The bonding is summarized nicely in the vbL picture,



From Table II we read that, at the MRCI level, the 4th and $15^{5}\Sigma^{+}$ states are characterized by $D_{e}=33.8$ and 19.4 kcal/mol at $R_{e}=2.551$ and 2.163 Å, respectively.

2. $7^{5}\Delta$, $17^{5}\Delta$

Their origin is traced to the product $|{}^{6}D;M=\pm 2$, $\pm 1\rangle_{Cr^{+}}\otimes|{}^{2}P;M=0,\pm 1\rangle_{B}$. In both states the asymptotic character of the fragments is maintained along the bonding process. As is evidenced from the leading CASSCF equilibrium CFs as well as from the atomic population analysis,

TABLE III. Total energy E (hartree), bond length R_e (Å), dissociation energy D_e (kcal/mol), and harmonic frequency ω_e (cm⁻¹) of the ground $X^7\Sigma^+$ state of CrB⁺ in different methods.

Method	-E	R _e	D_e	ω _e
SCF	1067.698 33	2.564	19.6	248
CISD	1067.853 29	2.350	26.5	303
CISD+Q ^a	1067.868 6	2.30	29	326
CASSCF(8/9) ^b	1067.730 26	2.624	18.1	224
MRCI	1067.859 63	2.335	27.0	300
MRCI+Q ^a	1067.8684	2.29	29	322
sa-CASSCF(8/10) ^{c,d}	1067.719 11	2.282	27.7	345
MRCI	1067.861 64	2.265	31.3	356
MRCI+Q ^a	1067.872 5	2.27	32	350
CASSCF(8/10) ^d	1067.740 67	2.606	18.8	257
MRCI	1067.863 45	2.242	28.8	436
MRCI+Q ^a	1067.870 5	2.23	31	462
c-MRCI ^e	1068.146 67	2.230	30.1	
c-MRCI+Q ^a	1068.178 5	2.20	34	
CASSCF(8/10) ^{d,f}	1067.741 94	2.593	18.8	271
MRCI	1067.866 56	2.242	29.1	392
MRCI+Q ^a	1067.873 7	2.23	31	410

 $^{a}+Q$ refers to the Davidson correction, Ref. 14.

S

C

Ν

N

^b8/9 means 8 active e^- distributed to 9 orbitals, $(3d)_{\rm Cr}/(2s+2p)_{\rm B}$. ^cState average CASSCF.

^d8 active e^- distributed to 10 orbitals, $(4s+3d)_{Cr}/(2s+2p)_B$. ^eThe "core" $3s^23p^6$ Cr⁺ e^- are included in the CI.

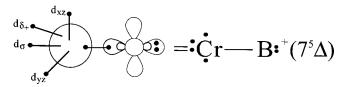
^fThe cc-pVQZ basis was employed for the B atom.

$$\begin{split} |7\ {}^{5}\Delta\rangle &\sim 0.86 |1\ \sigma^{2}2\ \sigma^{2}3\ \sigma^{1}1\ \delta^{1}_{+}1\ \pi^{1}_{x}1\ \pi^{1}_{y}\rangle, \\ 4s^{1.13}4p^{0.08}_{z}3d^{1.04}_{z^{2}}3d^{1.0}_{xz}3d^{1.0}_{yz}3d^{1.0}_{x^{2}-y^{2}/}\\ 2s^{1.89}2p^{0.81}_{z}2p^{0.06}_{x}2p^{0.06}_{y}, \\ |17\ {}^{5}\Delta\rangle &\sim 0.44 |1\ \sigma^{2}2\ \sigma^{1}3\ \sigma^{1}1\ \delta^{1}_{+}(1\ \pi^{2}_{x}-1\ \pi^{2}_{y})1\ \delta^{1}_{-}\rangle \\ &\quad + 0.37 |1\ \sigma^{2}2\ \sigma^{1}3\ \sigma^{1}1\ \delta^{1}_{+}(1\ \pi^{1}_{x}2\ \pi^{1}_{x})\\ &\quad - 1\ \pi^{1}_{y}2\ \pi^{1}_{y})1\ \delta^{1}_{-}\rangle, \end{split}$$

$$4s^{0.88}4p_z^{0.08}3d_{z^2}^{1.0}3d_{xz}^{0.60}3d_{yz}^{0.60}3d_{x^2-y^2}^{1.0}3d_{xy}^{1.0}/$$

$$2s^{1.58}2p_z^{0.45}2p_x^{0.40}2p_y^{0.40},$$

the bonding is comprised of a σ -bond and a π -bond in the 7 ${}^{5}\Delta$ and 17 ${}^{5}\Delta$ states, respectively. In the 7 ${}^{5}\Delta$ state 4 e^{-} are fully localized on the d_{π} , d_{σ} , and $d_{\delta_{+}}$ (or $d_{\delta_{-}}$ in the A_{1} symmetry) orbitals, with $0.20 e^{-}$ moving from the B $(2s2p_{z})^{2.89}$ hybrid orbital (at infinity) to Cr⁺ via the σ frame. The vbL bonding icon is



The corresponding bonding icon for the $17^{5}\Delta$ can be drawn as follows:

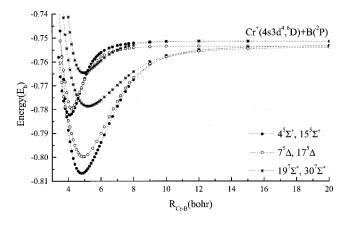
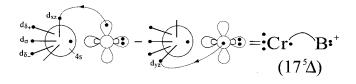


FIG. 4. MRCI PECs of the states 4 ${}^5\Sigma^+$, 7 ${}^5\Delta$, 15 ${}^5\Sigma^+$, 17 ${}^5\Delta$, 19 ${}^7\Sigma^+$, and 30 ${}^7\Sigma^+$.



with $0.20 e^-$ moving along the π frame from B to Cr⁺. The PECs of the above two states are given in Fig. 4; dissociation energies are 29.3 and 16.5 kcal/mol, with corresponding bond distances of 2.611 and 2.231 Å for the 7th and 17⁵ Δ states, respectively.

3. 8⁵П, 11⁵П, 18⁵П, 12⁵Ф

The three ⁵ Π states correlate to $|{}^{6}D; M = \pm 1, 0, \pm 2\rangle_{Cr^+} \otimes |{}^{2}P; M = 0, \pm 1, \mp 1\rangle_{B}$. Their PECs shown in Fig. 5 interact strongly in the inter-atomic region of 4–4.5 bohr. The 8 ⁵ Π state, due to an avoided crossing around 4.3 bohr with the 11 ⁵ Π state, presents a global (g) and a local (l) minimum at distances of 2.623 and 2.126 Å, and $D_e = 30.6$ and 25.0 kcal/mol, respectively (Table II). The energy barrier measured from the g-minimum is 6.3 kcal/mol. At the g-minimum the dominant CASSCF configurations,

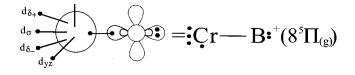
$$\begin{split} |8\,^{5}\Pi\rangle &\sim 0.77 |1\,\sigma^{2}2\,\sigma^{2}1\,\delta^{1}_{+}3\,\sigma^{1}1\,\pi^{1}_{y}1\,\delta^{1}_{-}\rangle \\ &- 0.40 |1\,\sigma^{2}2\,\sigma^{1}1\,\delta^{1}_{+}3\,\sigma^{1}4\,\bar{\sigma}^{1}1\,\pi^{1}_{y}1\,\delta^{1}_{-}\rangle, \end{split}$$

coupled with the atomic Mulliken distributions,

$$4s^{1.07}4p_{z}^{0.07}3d_{z^{2}}^{1.05}3d_{xz}^{0.04}3d_{yz}^{1.0}3d_{x^{2}-y^{2}}^{1.0}3d_{xy}^{1.0}/$$

$$2s^{1.82}2p_{z}^{0.80}2p_{x}^{0.09}2p_{y}^{0.06},$$

indicate the formation of a σ -bond and four nonbonded (observer) d_{σ} , d_{π} , and d_{δ} electrons,



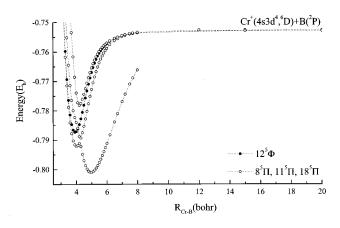


FIG. 5. MRCI PECs of the states 8 ${}^{5}\Pi$, 11 ${}^{5}\Pi$, 12 ${}^{5}\Phi$, and 18 ${}^{5}\Pi$.

At the *l*-minimum the wave function carries the character of the 115Π and 185Π states, due to the strong interaction of the latter with the former.

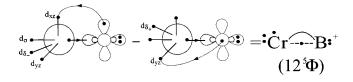
The minimum of the $11 \,{}^{5}\Pi$ state occurs at 2.27 Å (= 4.3 bohr), the interaction point of the three Π states. At this distance its binding energy is 23 kcal/mol but obviously with a very fuzzy binding mode.

The 18 ⁵ Π state has a binding energy of 16.2 kcal/mol at $R_e = 2.224$ Å and a very unclear binding mode due to its entanglement with the 8th and 11 ⁵ Π states.

The $M = \pm 2$ and $M = \pm 1$ combination of Cr⁺ and B atoms creates the 12⁵ Φ state whose PEC is also shown in Fig. 5. The main CASSCF CFs, defining in essence the binding scheme, are

$$\begin{split} |12\,^{5}\Phi\rangle &\sim 0.56(|1\sigma^{2}2\sigma^{1}3\sigma^{1}1\,\pi_{x}^{2}1\,\pi_{y}^{1}1\,\delta_{-}^{1}\rangle \\ &- |1\sigma^{2}2\sigma^{1}1\,\delta_{+}^{1}3\sigma^{1}1\,\pi_{x}^{1}1\,\pi_{y}^{2}\rangle), \end{split}$$

leading to a binding picture of a half σ - and one π -bond,



The above icon is corroborated by the Mulliken CASSCF atomic densities,

$$4s^{0.84}4p_{z}^{0.09}3d_{z^{2}}^{0.98}3d_{xz}^{1.12}3d_{yz}^{1.12}3d_{x^{2-y^{2}}}^{0.52}3d_{xy}^{0.52}$$

$$2s^{1.53}2p_{z}^{0.52}2p_{x}^{0.35}2p_{y}^{0.35}.$$

A migration of $0.10 e^-$ is observed from Cr⁺ to B along the σ skeleton resulting in the B hybrid $(2s2p_z)^{2.05}$ orbital, followed by a back donation of $0.30 e^-$ via the π frame. At the MCRCI level Table II records a $D_e = 21.6$ kcal/mol at $R_e = 2.079$ Å.

4. 19⁷Σ⁺, 30⁷Σ⁺

The $19^{7}\Sigma^{+}$ is very similar to the ground $X^{7}\Sigma^{+}$ state (*vide supra*), the difference being the replacement of a 3σ with a 4σ molecular orbital,

$$|19^{7}\Sigma^{+}\rangle \sim 0.97 |1\sigma^{2}\sigma^{1}4\sigma^{1}1\delta^{1}_{+}1\pi^{1}_{x}1\pi^{1}_{y}1\delta^{1}_{-}\rangle.$$

The CASSCF populations,

$$4s^{0.79}4p_z^{0.17}3d_{z^2}^{0.24}3d_{xz}^{1.0}3d_{yz}^{1.0}3d_{x^2-y^2}^{1.0}3d_{xy}^{1.0}/$$

$$2s^{1.80}2p_z^{0.90}2p_x^{0.05}2p_y^{0.05}$$

indicate the complete localization of the d_{π} and $d_{\delta}e^-$ on the metal, and the transfer of $0.2 e^-$ from B to Cr⁺ along the σ -route, causing a binding energy of 16.2 kcal/mol at $R_e = 2.757$ Å (Table II, Fig. 4).

The $30^7\Sigma^+$ state tracing its lineage to $Cr^+({}^6D;M = \pm 1) + B({}^2P;M = \mp 1)$, has a shallow minimum of 8.2 kcal/mol at $R_e = 2.613$ Å (Fig. 4, Table II) with the following CASSCF atomic populations:

$$4s^{0.89}4p_{z}^{0.09}3d_{z^{2}}^{1.0}3d_{xz}^{0.58}3d_{yz}^{0.58}3d_{x^{2}-y^{2}}^{1.0}3d_{xy}^{1.0}/$$

$$2s^{1.75}2p_{z}^{0.21}2p_{x}^{0.44}2p_{y}^{0.44}.$$

A $(2s2p_z)^{1.96}$ hybridization is observed on the B atom, but with no charge transfer from B to Cr⁺ through the σ skeleton, and a 0.18 e^- transfer from B $(2p_x^{0.53}2p_y^{0.53}$ at infinity) to Cr⁺ via the π system causing a small π interaction.

5. 21 ⁵Σ⁻, 27 ⁷Σ⁻

Both states correlate to $Cr^+({}^6D; M = \pm 1) + B({}^2P; M = \pm 1)$ with their PECs shown in Fig. 6, and with the following leading CASSCF equilibrium CFs:

$$\begin{split} |21\,^{5}\Sigma^{-}\rangle &\sim 0.41 |1\,\sigma^{2}2\,\sigma^{1}3\,\sigma^{1}1\,\delta^{1}_{+}(1\,\pi^{2}_{x}+1\,\pi^{2}_{y})1\,\delta^{1}_{-}\rangle \\ &+ 0.40 |1\,\sigma^{2}2\,\sigma^{1}3\,\sigma^{1}1\,\delta^{1}_{+}(1\,\pi^{1}_{x}2\,\bar{\pi}^{1}_{x}) \\ &+ 1\,\pi^{1}_{y}2\,\bar{\pi}^{1}_{y})1\,\delta^{1}_{-}\rangle, \\ |27\,^{7}\Sigma^{-}\rangle &\sim 0.69 |1\,\sigma^{2}2\,\sigma^{1}3\,\sigma^{1}1\,\delta^{1}_{+}(1\,\pi^{1}_{x}2\,\pi^{1}_{x}) \\ &+ 1\,\pi^{1}_{y}2\,\pi^{1}_{y})1\,\delta^{1}_{-}\rangle. \end{split}$$

In the $21^{5}\Sigma^{-}$ state we have the development of a weak π -bond giving rise to a $D_{e} = 12.3$ kcal/mol at $R_{e} = 2.203$ Å, while in the $27^{7}\Sigma^{-}$ state the two atoms interact weakly in a rather electrostatic fashion resulting in a $D_{e} = 8.2$ kcal/mol at $R_{e} = 2.453$ Å.

6. 22⁷Π, 26⁷Π, 29⁷Π, 24⁷Φ

The following product wave functions describe the Π and Φ states asymptotically:

$$|22^{7}\Pi, 26^{7}\Pi, 29^{7}\Pi, 24^{7}\Phi\rangle = |{}^{6}D; M = \pm 1, 0, \pm 2,$$

$$\pm 2\rangle_{Cr^{+}} \otimes |{}^{2}P; M = 0, \pm 1,$$

$$\mp 1, \pm 1\rangle_{B}.$$

The PECs shown in Fig. 7 indicate low dissociation energies, and also the interwoven nature of the Π states due to avoided crossings resulting in an interchange of the character of their (global) minima. In particular, the equilibrium of the 22⁷ Π and 26⁷ Π states carry the asymptotic character of the 26th and 29⁷ Π states, respectively. The complete localization of the four 3*d e*⁻ on the Cr⁺ in conjunction with the high spin do not allow for any strong binding: the D_e 's of the 22, 26,

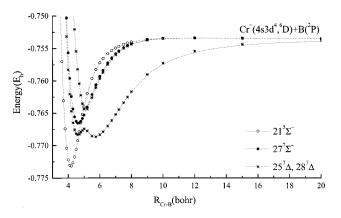


FIG. 6. MRCI PECs of the states $21 {}^{5}\Sigma^{-}$, $25 {}^{7}\Delta$, $27 {}^{7}\Sigma^{-}$, and $28 {}^{7}\Delta$.

29⁷ Π , and 24⁷ Φ states are 13.0, 9.3, 7.3, and 9.9 kcal/mol at 2.381, 2.393, 2.65, and 2.367 Å, respectively (Table II). Only in the 22⁷ Π state there is a 0.20 e^- transfer from B to Cr⁺ via the σ -frame and perhaps the development of a half σ -bond; in the rest of the states the charge transfer is insignificant.

7. 25 ⁷Δ, 28 ⁷Δ

Figure 6 presents the PECs of the titled states correlating to $|{}^{6}D; M = \pm 2, \pm 1\rangle_{Cr^{+}} \otimes |{}^{2}P; M = 0, \pm 1\rangle_{B}$. The 25⁷ Δ suffers an avoided crossing at about 5 bohr with the incoming 28⁷ Δ state resulting in two, practically degenerate, minima at the MRCI level, Table II. Again, the high spin and the *d* localization of the Cr⁺ electrons forbid any significant binding. The asymptotic electron distributions are essentially transferred to the first minimum of the 25⁷ Δ state (R_e = 3.015 Å), while as expected, the minimum of the 28⁷ Δ state being on top of the barrier, is a mélange of the two asymptotes, $0.57|M = \pm 2\rangle \otimes |M = 0\rangle + 0.53|M = \pm 1\rangle \otimes |M$ = $\pm 1\rangle$. From Table II we read that the D_e 's and R_e 's are 9.5, 7.1 kcal/mol and 3.015, 2.710 Å for the 25 and 28⁷ Δ states, respectively.

C. 5 ${}^{3}\Delta$, 6 ${}^{3}\Pi$, 9 ${}^{3}\Sigma^{-}$, 10 ${}^{3}\Phi$, 13 ${}^{3}\Pi$, 14 ${}^{3}\Delta$, 16 ${}^{3}\Sigma^{+}$, 23 ${}^{3}\Pi$, and 33 ${}^{3}\Sigma^{+}$ states

All the above triplet states correlate to $\operatorname{Cr}^+(4s3d^4, {}^4D) + \operatorname{B}(2s^22p, {}^2P).$

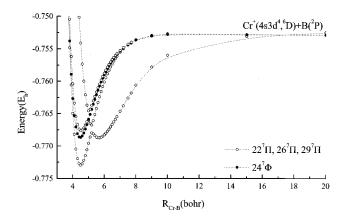


FIG. 7. MRCI PECs of the states $22^{7}\Pi$, $24^{7}\Phi$, $26^{7}\Pi$, and $29^{7}\Pi$.

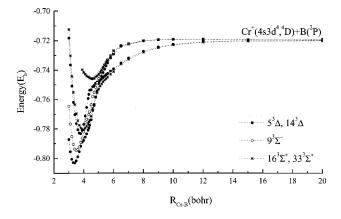


FIG. 8. MRCI PECs of the states 5 $^3\Delta,$ 9 $^3\Sigma^-,$ 14 $^3\Delta,$ 16 $^3\Sigma^+,$ and 33 $^3\Sigma^+.$

1. $5^{3}\Delta$, 14 $^{3}\Delta$

The adiabatic fragments of the Δ states are described by the combination $|{}^{4}D;M=\pm 2,\pm 1\rangle_{Cr^{+}}\otimes|{}^{2}P;M=0,\pm 1\rangle_{B}$ with MRCI PECs given in Fig. 8. Around 5 bohr a character change of the 5 ${}^{3}\Delta$ state is observed ($M=\pm 2,0$ to $\pm 1, \pm 1$) due to an avoided crossing with the 14 ${}^{3}\Delta$ state; a second avoided crossing follows at about 4 bohr responsible for the equilibrium personality of this state, i.e., that of a triple bond (*vide infra*). The leading CASSCF configurations are

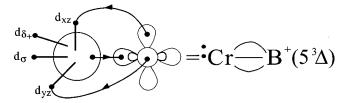
$$\begin{split} |5^{3}\Delta\rangle &\sim 0.85 |1\sigma^{2}2\sigma^{1}1\delta^{1}_{+}1\pi^{2}_{x}1\pi^{2}_{y}\rangle \\ &- 0.16 |1\sigma^{2}2\sigma^{1}1\delta^{1}_{+}1\pi^{2}_{x}2\pi^{2}_{y}\rangle \\ &- 0.16 |1\sigma^{2}2\sigma^{1}1\delta^{1}_{+}2\pi^{2}_{x}1\pi^{2}_{y}\rangle, \end{split}$$

with the ''0.16'' components signifying the GVB correlation. The CASSCF atomic Mulliken populations,

$$4s^{0.28}4p_z^{0.12}3d_{z^2}^{0.91}3d_{xz}^{1.36}3d_{yz}^{1.36}3d_{x^2-y^2}^{1.0}3d_{xy}^{0.07}/$$

$$2s^{1.47}2p_z^{0.25}2p_x^{0.55}2p_y^{0.55},$$

reveal the existence of a triple bond, in accord with the "0.85" CASSCF component. We can draw the following vbL picture:



Notice that the *in situ* B atom finds itself in a ⁴P excited state, 3.57 eV above the ground ²P state (Table I). Therefore, through the π frame $2 \times 0.36 = 0.72 e^-$ are transferred from the B to the metal center, with the latter responding back with $0.6 e^-$ via the σ -frame. Our binding energy of 52.9 kcal/mol, with respect to the adiabatic fragments, and bond length of 1.779 Å (Table II), are in remarkable agreement with the isovalent species CrCH⁺ (\tilde{X} ³ Σ^-)^{15(a)} and CrN⁺ (X³ Σ^-)^{15(b)} with corresponding parameters of 53.7 kcal/mol, 1.772 Å and 49.5 kcal/mol, 1.569 Å, respectively. Certainly, all three species have very similar electron distri-

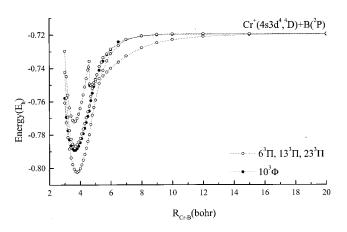


FIG. 9. MRCI PECs of the states 6 $^3\Pi,~10\,^3\Phi,~13\,^3\Pi,$ and 23 $^3\Pi.$

butions, the only difference being the occupation of a δ_{-} orbital (CrB⁺) instead of a d_{σ} orbital (CrCH⁺,CrN⁺). Finally, we report that the 5 ${}^{3}\Delta$ state has the shortest bond length of all states studied (Table II), with an "internal bond strength" of $52.9 + \Delta E({}^{4}P \leftarrow {}^{2}P) = 135$ kcal/mol, in harmony with its triple bond character.

The 14 ${}^{3}\Delta$ suffers three avoided crossings, two of which (the first and the third) at 5.0 and 4.0 bohr have been previously discussed, and another one between the first two (~4.3 bohr) and an incoming ${}^{3}\Delta$ state (not calculated) originating from the ${}^{4}P$ boron state and responsible for the triple bond character in both the 5th and 14 ${}^{3}\Delta$ states. Due to the fact that the 14 ${}^{3}\Delta$ minimum occurs at the interaction region with the 5 ${}^{3}\Delta$ state, it carries the memory of both states. Our main equilibrium CASSCF configurations are

$$\begin{split} |14^{3}\Delta\rangle &\sim 0.53 |1\sigma^{2}2\sigma^{1}1\delta_{+}^{1}1\pi_{x}^{2}1\pi_{y}^{2}\rangle \\ &+ 0.37 |1\sigma^{2}2\sigma^{2}1\delta_{+}^{1}(1\bar{\pi}_{x}^{1}1\pi_{y}^{1}) \\ &- 1\pi_{x}^{1}1\bar{\pi}_{y}^{1})1\delta_{-}^{1}\rangle. \end{split}$$

Clearly, the "0.53" component introduces the triple bond character, while the "0.37" correlates to the $M = \pm 1, \pm 1$ asymptote. At $R_e = 1.985$ Å a $D_e = 39.9$ kcal/mol is calculated at the MRCI level, Table II.

2. 6³Π, 13³Π, 23³Π, 10³Φ

At infinity the 6th, 13th, 23 ${}^{3}\Pi$, and 10 ${}^{3}\Phi$ states correlate to $|{}^{4}D;M=\pm 1,\pm 2,0,\pm 2\rangle_{Cr^{+}}\otimes|{}^{2}P;M=0,\mp 1,\pm 1,$ $\pm 1\rangle_{B}$, respectively, with corresponding PECs shown in Fig. 9. The involved morphology of the Π symmetry curves is caused by consecutive avoided crossings discussed briefly in what follows.

At large distance (~6 bohr) a strong interaction between the 13th and 23 ${}^{3}\Pi$ states changes their character ($M = \pm 2$, $\mp 1 \rightarrow 0, \pm 1$), followed by an avoided crossing at 5.3 bohr between the 6th and the 13 ${}^{3}\Pi$ states, resulting to the character transfer of the latter to the former. The net result is the adoption of the 23 ${}^{3}\Pi$ character ($M = 0, \pm 1$) by the 6 ${}^{3}\Pi$ state. Another avoided crossing occurs between the 13th and the 23 ${}^{3}\Pi$ states, thus the 13th re-enters into its former asymptotic mode. Now, the 23 ${}^{3}\Pi$ state experiences a severe avoided crossing at about 4.5 bohr with an incoming (not calculated) ${}^{3}\Pi$ state stemming from the Cr⁺ ${}^{4}G$ atomic state.

At the equilibrium the predominant parent configuration of the 6 ${}^{3}\Pi$ state is of the type $1 \sigma^{2} (2 \sigma^{1} 1 \delta_{+}^{1} 1 \pi_{x}^{2} 1 \pi_{y}^{1} 1 \delta_{-}^{1})$ combined with a series of spin functions coupled into a triplet. Apart from the formation of a π bond, the localization of two δe^{-} on the metal, and a net transfer of $0.1 e^{-}$ from B to Cr⁺ nothing else can be said about the bonding nature of the 6 ${}^{3}\Pi$ state. From Table II we read that a $D_{e} = 52.3$ kcal/mol is obtained at $R_{e} = 2.003$ Å (MRCI).

The dominant CASSCF equilibrium configurations of the 13 $^3\Pi$ and 23 $^3\Pi$ states are

$$\begin{split} |13^{3}\Pi\rangle &\sim 0.39(|1\sigma^{2}2\sigma^{2}1\delta_{+}^{1}1\pi_{x}^{1}1\pi_{y}^{2}\rangle \\ &-|1\sigma^{2}2\sigma^{2}1\pi_{x}^{2}1\pi_{y}^{1}1\delta_{-}^{1}\rangle) \\ &+ 0.37|1\sigma^{2}2\sigma^{1}1\delta_{+}^{1}1\pi_{x}^{2}1\bar{\pi}_{y}^{1}1\delta_{-}^{1}\rangle \\ &- 0.36|1\sigma^{2}2\bar{\sigma}^{1}1\delta_{+}^{1}1\pi_{x}^{2}1\pi_{y}^{1}1\delta_{-}^{1}\rangle, \\ |23^{3}\Pi\rangle &\sim 0.55|1\sigma^{2}2\sigma^{1}1\delta_{+}^{1}1\pi_{x}^{2}1\bar{\pi}_{y}^{1}1\delta_{-}^{1}\rangle \\ &- 0.31(|1\sigma^{2}2\sigma^{1}1\bar{\delta}_{+}^{1}1\pi_{x}^{2}1\pi_{y}^{1}1\bar{\delta}_{-}^{1}\rangle \\ &+ |1\sigma^{2}2\sigma^{1}1\delta_{+}^{1}1\pi_{x}^{2}1\pi_{y}^{1}1\bar{\delta}_{-}^{1}\rangle). \end{split}$$

In the $13 \,{}^{3}\Pi$ state the "0.39" and "0.37, 0.36" contributions correlate to the $M = (\pm 2, \mp 1)$ and $(0, \pm 1)$ components, respectively, while in the $23 \,{}^{3}\Pi$ state both "0.55" and "0.31" configurations correspond to the $M = 0, \pm 1$ adiabatic fragments. The nature of the configurations involved in the above states and the rather unclear populations obtained from the CASSCF wave functions, forbid the construction of simple bonding images. The binding energies and bond distances at the MRCI level (Table II) of the 13th and $23 \,{}^{3}\Pi$ states are 42.1 and 33.0 kcal/mol, at 1.931 and 1.911 Å, respectively.

The dominant CASSCF equilibrium CFs of the $10^{3}\Phi$ state along with the Mulliken atomic populations are

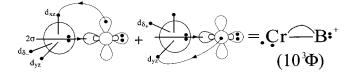
$$\begin{split} |10^{3}\Phi\rangle &\sim 0.53(|1\sigma^{2}2\sigma^{2}1\pi_{x}^{2}1\pi_{y}^{1}1\delta_{-}^{1}\rangle \\ &+ |1\sigma^{2}2\sigma^{2}1\delta_{+}^{1}1\pi_{x}^{1}1\pi_{y}^{2}\rangle), \\ 4s^{0.39}4p_{z}^{0.15}3d_{z^{2}}^{1.26}3d_{xz}^{1.12}3d_{yz}^{1.12}3d_{x^{2}-y^{2}}^{0.54}3d_{xy}^{0.54}/ \\ &2s^{1.45}2p_{z}^{0.70}2p_{x}^{0.34}2p_{y}^{0.34}. \end{split}$$

Taking into account the populations at infinity,

$$4s^{1.03}d_{z^2}^{1.03}d_{xz}^{1.03}d_{yz}^{1.03}d_{x^2-y^2}^{0.50}3d_{xy}^{0.50}/$$

$$2s^{1.89}2p_z^{0.06}2p_x^{0.53}2p_y^{0.53},$$

the following vbL icon can be drawn:



We claim that three π electrons are involved in a single π bond, while a σ bond is formed through the interaction of the hybrid orbital functions $(4s4p_z3d_{z^2})_{Cr^+}^{1.80} + (2s2p_z)_B^{2.15}$, with a net transfer of $0.14 e^-$ from B to Cr⁺.

3. 9³Σ⁻

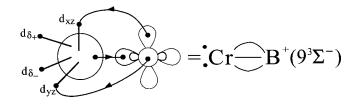
The present state, described at infinity by the wave function $|{}^{4}D;M = \pm 1\rangle_{Cr^{+}} \otimes |{}^{2}P;M = \mp 1\rangle_{B}$, exhibits an avoided crossing at the internuclear distance of 4.0 bohr with the $20 {}^{3}\Sigma^{-}$ state (partially computed) which correlates to the Cr⁺ ${}^{4}G$ atomic state (*vide infra*), Fig. 8. The equilibrium CASSCF CFs and the atomic population densities of the $9 {}^{3}\Sigma^{-}$ state are

$$|9^{3}\Sigma^{-}\rangle \sim 0.78 |1\sigma^{2}1\delta_{+}^{1}1\pi_{x}^{2}1\pi_{y}^{2}1\delta_{-}^{1}\rangle,$$

$$4s^{0.18}4p_{z}^{0.10}3d_{z^{2}}^{0.29}3d_{xz}^{1.26}3d_{yz}^{1.26}3d_{x^{2}-y^{2}}^{1.0}3d_{xy}^{1.0}/$$

$$2s^{1.43}2p_{z}^{0.08}2p_{x}^{0.66}2p_{y}^{0.66}.$$

A vbL bonding picture consistent with the above data is the following:



Notice that the *in situ* B atom finds itself in the ⁴P $(2s^{1}2p_{x}^{1}2p_{y}^{1};M=0)$ excited state. Via the π -frame $0.52(=0.26+0.26)e^{-}$ are moving from the B to the Cr⁺ cation forming two π -bonds; through the σ -frame $0.43e^{-}$ migrate from a $(4s4p_{z}3d_{z})_{Cr^{+}}$ hybrid to the $2s(1.43e^{-})$ of the B atom. The energy content of this triple bond with respect to the adiabatic products is $D_{e}=47.3$ kcal/mol at $R_{e}=1.864$ Å (Table II).

4. 16 ${}^{3}\Sigma^{+}$, 33 ${}^{3}\Sigma^{+}$

The PECs shown in Fig. 8 correlate to $|{}^{4}D;M=0$, $\pm 1\rangle_{Cr^{+}}\otimes|{}^{2}P;M=0,\pm 1\rangle_{B}$, respectively. The equilibrium CASSCF CFs are of the type

$$|16^{3}\Sigma^{+}\rangle \sim 1\sigma^{2}2\sigma^{2}(1\delta_{+}^{1}1\pi_{x}^{1}1\pi_{y}^{1}1\delta_{-}^{1})$$

and

$$|33^{3}\Sigma^{+}\rangle \sim 1\sigma^{2}(2\sigma^{1}3\sigma^{1}1\,\delta_{+}^{1}1\,\pi_{x}^{1}1\,\pi_{y}^{1}1\,\delta_{-}^{1}),$$

combined with a series of triplet coupled spin functions. The corresponding Mulliken atomic distributions are

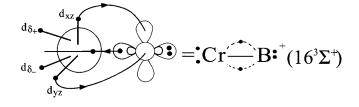
$$16^{3}\Sigma^{+}:4s^{0.49}4p_{z}^{0.15}3d_{z^{2}}^{1.12}3d_{xz}^{0.66}3d_{yz}^{0.66}3d_{x^{2}-y^{2}}^{1.0}3d_{xy}^{1.0}/$$

$$2s^{1.44}2p_{z}^{0.76}2p_{x}^{0.34}2p_{y}^{0.34},$$

$$33^{3}\Sigma^{+}:4s^{0.90}4p_{z}^{0.12}3d_{z^{2}}^{0.50}3d_{xz}^{0.86}3d_{yz}^{0.86}3d_{x^{2}-y^{2}}^{1.0}3d_{xy}^{1.0}/$$

$$2s^{1.62}2p_{z}^{0.80}2p_{x}^{0.16}2p_{y}^{0.16}.$$

The bonding mechanism of the $16^{3}\Sigma^{+}$ state is succinctly represented by the icon



indicating the formation of a σ -bond and two half π -bonds. Via the π -frame 2×0.34=0.68 e^- diffuse from Cr⁺ to B, while 0.8 e^- return to the $(4s4p_z3d_{z^2})^{1.76}_{Cr^+}$ hybrid. At a R_e = 2.090 Å the bond energy content is D_e = 38.0 kcal/mol with respect to the asymptotic products (Table II).

The bonding in the 33 ${}^{3}\Sigma^{+}$ state is not so clear as in the previous state; we can discern two half π -bonds with a synchronous transfer of $0.32 e^{-}$ through the π system, two observer δ_{+} and $\delta_{-} e^{-}$, and the donation of $0.50 e^{-}$ from B to Cr⁺ via the σ -frame. At the equilibrium distance of $R_{e} = 2.423$ Å a rather weak bond of 16.5 kcal/mol is calculated at the MRCI level.

D. 20 ${}^{3}\Sigma^{-}$, 31 ${}^{3}\Phi$, 32 ${}^{3}\Gamma$, and 34 ${}^{3}\Delta$ states

The four titled states correlate adiabatically to $Cr^+({}^4G)$ + B(2P); no complete potential energy curves are available for these states due to severe technical problems encountered during their computations (Fig. 10).

1. 20 ³Σ⁻

As was already discussed in Sec. IV C the $20^{3}\Sigma^{-}$ state suffers an avoided crossing at about 4 bohr with the $9^{3}\Sigma^{-}$ state (*vide supra*). The fact that the interaction between these two PECs practically coincides with the equilibrium distance of the state under discussion, does not allow for an understanding of the binding in terms of simple "chemical pictures." With respect to the adiabatic products we report a binding energy $D_{e} = 73.0$ kcal/mol at a $R_{e} = 2.075$ Å (Table II).

For the 31 ³ Φ state we can only report its binding energy $D_e = 62.5$ kcal/mol and bond length $R_e = 1.888$ Å at the MRCI level of theory, Table II.

*2. 32 ³*Г

This state traces its ancestry to $|{}^{4}G; M = \pm 4\rangle_{Cr^{+}} \otimes |{}^{2}P; M = 0\rangle_{B}$. The leading CASSCF equilibrium configurations (A_{2} symmetry) and corresponding Mulliken densities are

$$|32\,{}^{3}\Gamma\rangle \sim 0.60(|1\,\sigma^{2}2\,\sigma^{2}1\,\pi_{x}^{1}1\,\pi_{y}^{1}1\,\delta_{-}^{2}\rangle \\ -|1\,\sigma^{2}2\,\sigma^{2}1\,\delta_{+}^{2}1\,\pi_{x}^{1}1\,\pi_{y}^{1}\rangle),$$

$$4s^{0.30}4p_{z}^{0.12}3d_{z^{2}}^{1.22}3d_{xz}^{0.73}3d_{yz}^{0.73}3d_{x^{2}-y^{2}}^{1.0}3d_{xy}^{1.0}/ \\ 2s^{1.55}2p_{z}^{0.76}2p_{x}^{0.27}2p_{y}^{0.27}.$$

We clearly see the formation of two half π -bonds with the synchronous transfer of $2 \times 0.27 = 0.54 e^-$ from Cr⁺ to B through the π system, and one σ -bond between the two hybrids $(4s4p_z 3d_{z^2})_{Cr^+}^{1.64}$ and $(2s2p_z)_B^{2.31}$. The emerging vbL icon is the following:

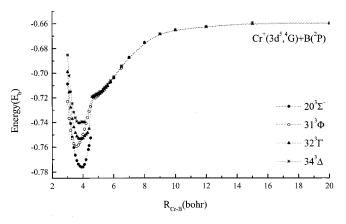
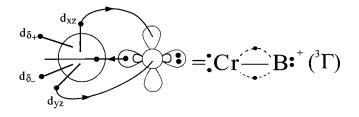


FIG. 10. MRCI PECs of the states $20^{3}\Sigma^{-}$, $31^{3}\Phi$, $32^{3}\Gamma$, and $34^{3}\Delta$.



At the MRCI level the dissociation energy and bond distance are 58.7 kcal/mol and 2.020 Å (Table II).

3. 34 $^{3}\Delta$

This is the highest state reported in the present work, 3.35 eV above the ground $X^{7}\Sigma^{+}$ state. The main CASSCF equilibrium CFs,

$$|34^{3}\Delta\rangle \sim 0.68 |1\sigma^{2}1\delta_{+}^{1}3\sigma^{1}1\pi_{x}^{2}1\pi_{y}^{2}\rangle -0.23 |1\sigma^{2}2\sigma^{1}1\delta_{+}^{1}1\pi_{x}^{2}1\pi_{y}^{2}\rangle$$

in conjunction with the Mulliken CASSCF densities,

$$4s^{0.53}4p_z^{0.13}3d_{z^2}^{0.52}3d_{xz}^{1.41}3d_{yz}^{1.41}3d_{x^2-y^2}^{1.0}3d_{xy}^{0.13}/$$

$$2s^{1.36}2p_z^{0.55}2p_x^{0.45}2p_y^{0.45},$$

dictate the formation of a triple bond; as expected the *in situ* B atom is in its excited ⁴P state. Although the $3d_{xy}$ 0.13 e^- cannot be accounted for, it is rather clear that about 1 e^- is transferred from B to Cr⁺ via the π frame and the formation of two π -bonds, while 0.9 e^- are injected back from the metal to the B atom through the σ -frame. As we can see from Table II the binding energy $D_e = 50.5$ kcal/mol at an $R_e = 1.986$ Å, is very similar to the other triple bonded states $5^{3}\Delta$ and $9^{3}\Sigma^{-}$.

V. SYNOPSIS AND FINAL REMARKS

Employing a $[(7s6p4d3f)_{Cr}/(4s3p2d1f)_B]$ basis in conjunction with CASSCF-CI methods, we have investigated the electronic structure of the molecular cation chromium boride, CrB⁺.

For the ground $(X^7\Sigma^+)$ and thirty four excited states we report MRCI potential curves, absolute energies, and spectroscopic constants $(R_e, D_e, \omega_e, T_e)$. We also tried to interpret the binding interactions by the use of simple chemical diagrams. Our main findings can be condensed as follows:

Given that the *in situ* B atom is in its lowest state, the $X^{7}\Sigma^{+}$ state of CrB⁺ has the maximal spin multiplicity possible, is rather loosely bound ($D_{e} = 28.8 \text{ kcal/mol}$), and the two atoms are held together by a half σ -bond. The complete lack of π interaction stemming from Cr⁺ is interpreted on the basis of the significantly larger ionization potential of Cr⁺ as compared to the earlier transition metal cations. It is reminded that the ground states of the previous borides studied, i.e., ScB⁺($X^{4}\Sigma^{-}$), TiB⁺($X^{5}\Delta$), VB⁺($X^{6}\Sigma^{+}$) have a mean binding energy of 45 kcal/mol, while the bonding is comprised of three half-bonds, one σ , and two π .

We have encountered a variety of binding schemes ranging from a half σ to full three bonds, and bond distances from 2.76(19⁷ Σ^+) to 1.78(5³ Δ) Å.

The state $5^{3}\Delta$, $9^{3}\Sigma^{-}$, and $34^{3}\Delta$ present genuinely three bond character with binding energies of 52.9, 47.3, and 50.5 kcal/mol, respectively.

It is obvious that within the accuracy of our methods the high density of a number of states, for instance the 5 ${}^{3}\Delta$, 6 ${}^{3}\Pi$, 7 ${}^{5}\Delta$, and 8 ${}^{5}\Pi$ with energy differences less than 1 mhartree, preclude the accurate determination of their relative energy ordering.

Drawing on our previous experience, some numerical experiments done in the present report and the indicative results of the Davidson correction, we can claim that on the average, our MRCI D_e values fall short by about 7% as compared to the "true" D_e numbers.

Finally, with the exception of the four first states $X^7\Sigma^+$, $1^5\Sigma^+$, $2^5\Pi$ and $3^7\Pi$ all states are unbound with respect to the ground state atoms.

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